

# On the Exploitation of Non-Radiating Currents to Design Geometry-Constrained Reflectarray Antennas

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## Abstract

In this work, the design of reflectarray surface currents able to meet both radiation and arbitrary geometry constraints is dealt with. Towards this goal, the synthesis problem is formulated as an inverse source one, and a closed-form expression solution is derived to compute the non-radiating current components able to modify the geometry of the reflective surface without altering the desired radiation features. Some representative numerical benchmarks are shown to assess the proposed synthesis methodology, as well as to verify its flexibility in realizing "*forbidden-regions*" of arbitrary shape.

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# 1 Numerical Results

## 1.1 Shape - “O LCD-Like @ Center”

### Parameters

- Number of reflectarray elements:  $M = 81, N = 69$ ;
- Operative frequency:  $f = 3.6$  [GHz];
- Polarization: L-CO;
- Number of elements in the forbidden region:  $Q = 32$ ;

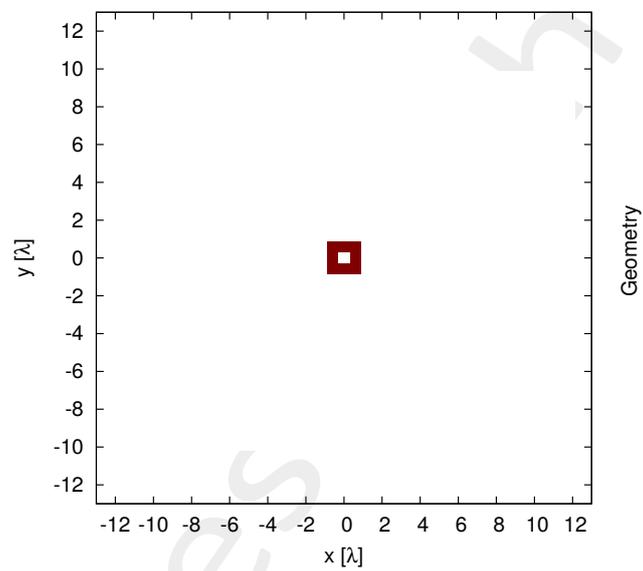


Figure 1: Geometry of forbidden region  $\Omega$ .

## Results

Magnitude and phase of the  $NR$  coefficients.

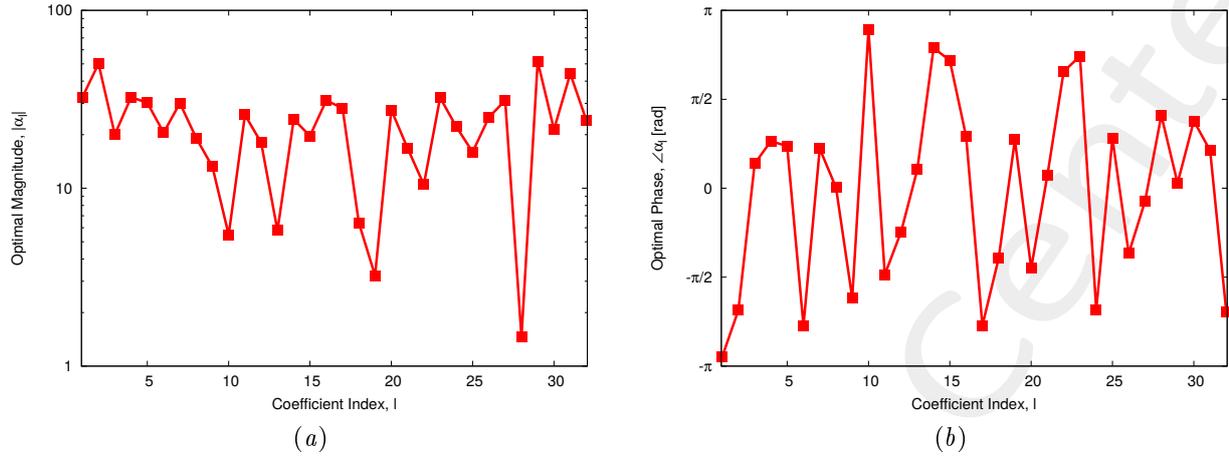


Figure 2: Magnitude (a) and phase (b) of the solution.

Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$	Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$	Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$
1	$-3.20 \times 10^1$	$-5.25$	12	$1.29 \times 10^1$	$-1.26 \times 10^1$	23	$-2.23 \times 10^1$	$2.34 \times 10^1$
2	$-2.77 \times 10^1$	$-4.19 \times 10^1$	13	5.48	1.88	24	$-1.20 \times 10^1$	$-1.86 \times 10^1$
3	$1.82 \times 10^1$	8.42	14	$-1.92 \times 10^1$	$1.50 \times 10^1$	25	$1.02 \times 10^1$	$1.23 \times 10^1$
4	$2.19 \times 10^1$	$2.40 \times 10^1$	15	$-1.25 \times 10^1$	$1.52 \times 10^1$	26	$1.02 \times 10^1$	$-2.29 \times 10^1$
5	$2.23 \times 10^1$	$2.04 \times 10^1$	16	$1.90 \times 10^1$	$2.47 \times 10^1$	27	$3.04 \times 10^1$	$-7.08$
6	$-1.55 \times 10^1$	$-1.35 \times 10^1$	17	$-2.12 \times 10^1$	$-1.85 \times 10^1$	28	$4.07 \times 10^{-1}$	1.40
7	$2.31 \times 10^1$	$1.94 \times 10^1$	18	2.10	$-6.04$	29	$5.14 \times 10^1$	4.58
8	$1.92 \times 10^1$	$2.04 \times 10^{-1}$	19	2.11	2.44	30	7.99	$1.98 \times 10^1$
9	$-4.75$	$-1.23 \times 10^1$	20	4.31	$-2.72 \times 10^1$	31	$3.47 \times 10^1$	$2.72 \times 10^1$
10	$-5.15$	1.85	21	$1.63 \times 10^1$	3.91	32	$-1.39 \times 10^1$	$-1.95 \times 10^1$
11	1.18	$-2.58 \times 10^1$	22	$-4.94$	9.25			

Table I: Solution of the linear system

## Currents Distribution

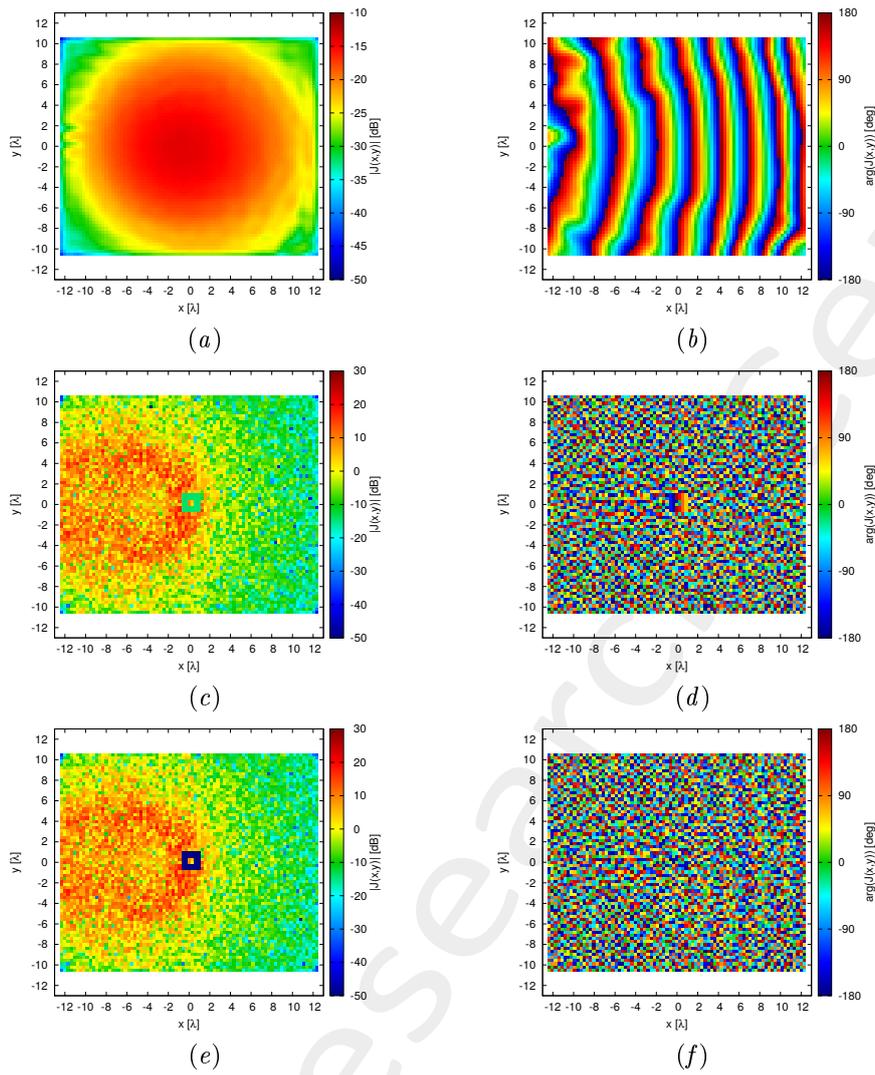


Figure 3: (a)(c)(e) Magnitude and (b)(d)(f) phase (a)(b) of  $J^{MN}(x, y)$ , (c)(d)  $J^{NR}(x, y; \underline{\alpha})$ , and (e)(f)  $J^{TOT}(x, y; \underline{\alpha})$ .

## Radiated Field

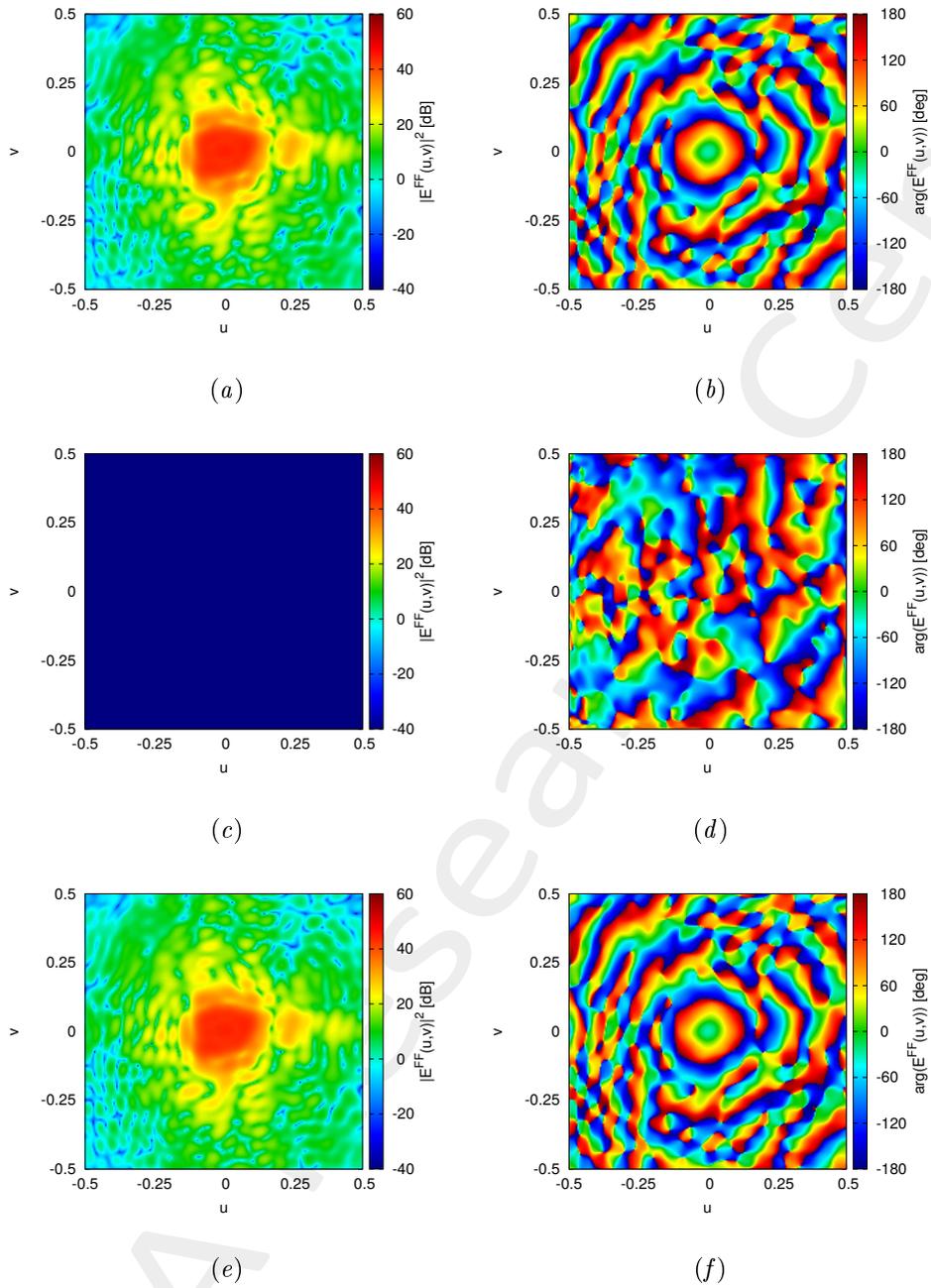


Figure 4: (a)(c)(e) Magnitude and (b)(d)(f) phase of the radiated field by (a)(b),  $J^{MN}(x, y)$ , (c)(d)  $J^{NR}(x, y; \underline{\alpha})$ , and (e)(f)  $J^{TOT}(x, y; \underline{\alpha})$ .

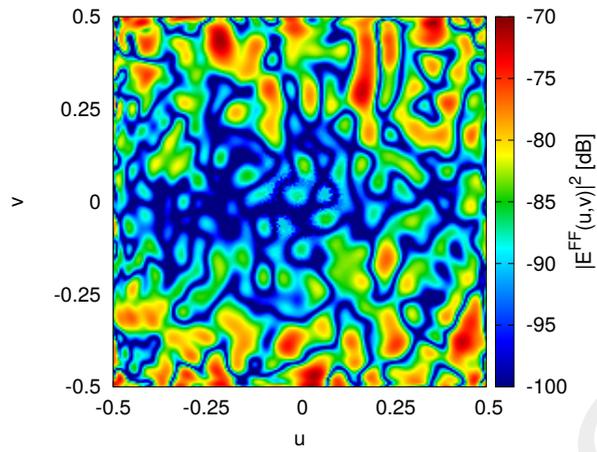


Figure 5: Magnitude of the difference between the radiated fields by  $J^{MN}(x, y)$  and  $J^{TOT}(x, y; \underline{\alpha})$ .

## 1.2 Shape - “2 O LCD-Like @ Center and up right corner”

### Parameters

- Number of reflectarray elements:  $M = 81, N = 69$ ;
- Operative frequency:  $f = 3.6$  [GHz];
- Polarization: L-CO;
- Number of elements in the forbidden region:  $Q = 44$ ;

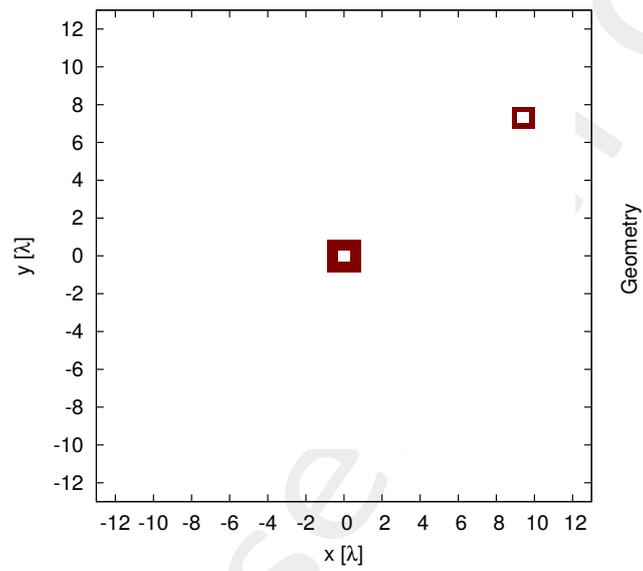


Figure 6: Geometry of forbidden region  $\Omega$ .

## Results

Magnitude and phase of the  $NR$  coefficients.

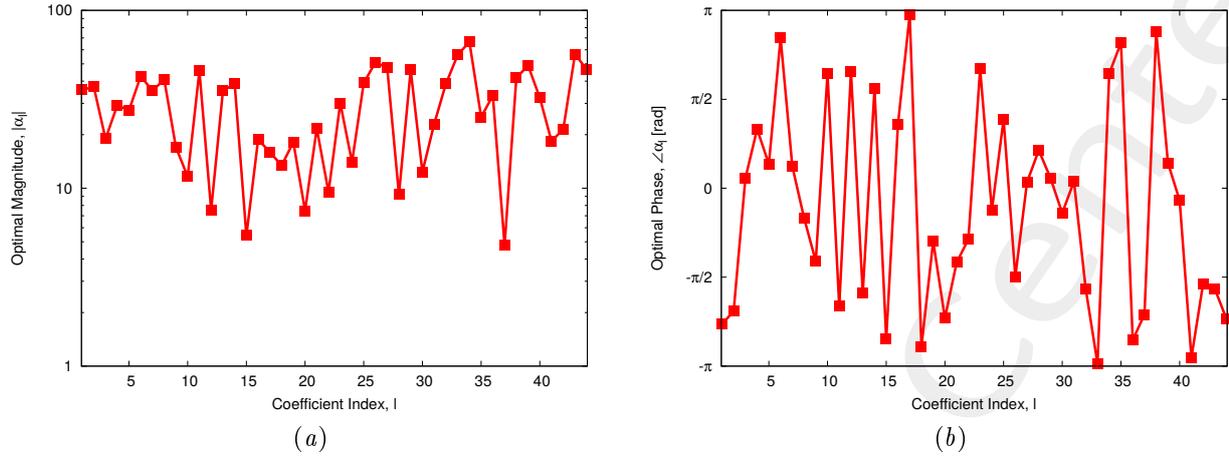


Figure 7: Magnitude (a) and phase (b) of the solution.

Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$	Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$	Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$
1	$-2.64 \times 10^1$	$-2.40 \times 10^1$	16	7.97	$1.70 \times 10^1$	31	$2.28 \times 10^1$	2.78
2	$-2.10 \times 10^1$	$-3.06 \times 10^1$	17	$-1.60 \times 10^1$	1.22	32	-7.82	$-3.77 \times 10^1$
3	$1.87 \times 10^1$	3.30	18	$-1.26 \times 10^1$	-4.58	33	$-5.60 \times 10^1$	-2.44
4	$1.47 \times 10^1$	$2.53 \times 10^1$	19	$1.08 \times 10^1$	$-1.47 \times 10^1$	34	$-2.93 \times 10^1$	$5.98 \times 10^1$
5	$2.50 \times 10^1$	$1.13 \times 10^1$	20	-4.94	-5.61	35	$-2.11 \times 10^1$	$1.36 \times 10^1$
6	$-3.77 \times 10^1$	$2.00 \times 10^1$	21	5.60	$-2.09 \times 10^1$	36	$-2.98 \times 10^1$	$-1.47 \times 10^1$
7	$3.26 \times 10^1$	$1.34 \times 10^1$	22	5.90	-7.46	37	-2.93	-3.77
8	$3.54 \times 10^1$	$-2.05 \times 10^1$	23	$-1.54 \times 10^1$	$2.59 \times 10^1$	38	$-3.89 \times 10^1$	$1.52 \times 10^1$
9	4.70	$-1.63 \times 10^1$	24	$1.29 \times 10^1$	-5.31	39	$4.41 \times 10^1$	$2.12 \times 10^1$
10	-5.08	$1.05 \times 10^1$	25	$1.36 \times 10^1$	$3.66 \times 10^1$	40	$3.15 \times 10^1$	-6.91
11	$-2.25 \times 10^1$	$-3.97 \times 10^1$	26	$4.36 \times 10^{-1}$	$-5.11 \times 10^1$	41	$-1.82 \times 10^1$	-2.73
12	-3.57	6.64	27	$4.73 \times 10^1$	5.10	42	-2.48	$-2.13 \times 10^1$
13	-9.85	$-3.39 \times 10^1$	28	7.22	5.72	43	$-1.19 \times 10^1$	$-5.55 \times 10^1$
14	-7.22	$3.80 \times 10^1$	29	$4.55 \times 10^1$	8.27	44	$-3.14 \times 10^1$	$-3.43 \times 10^1$
15	-4.82	-2.48	30	$1.12 \times 10^1$	-5.25			

Table II: Solution of the linear system

## Currents Distribution

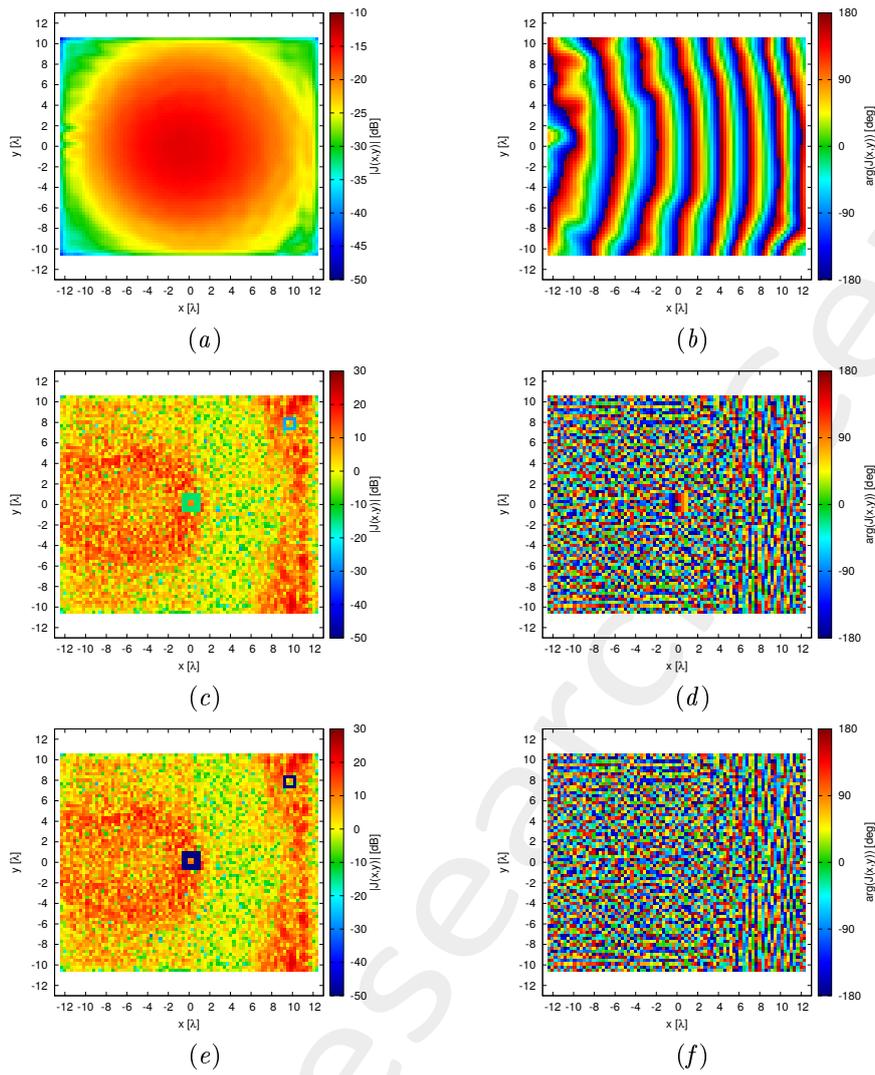


Figure 8: (a)(c)(e) Magnitude and (b)(d)(f) phase (a)(b) of  $J^{MN}(x, y)$ , (c)(d)  $J^{NR}(x, y; \underline{\alpha})$ , and (e)(f)  $J^{TOT}(x, y; \underline{\alpha})$ .

## Radiated Field

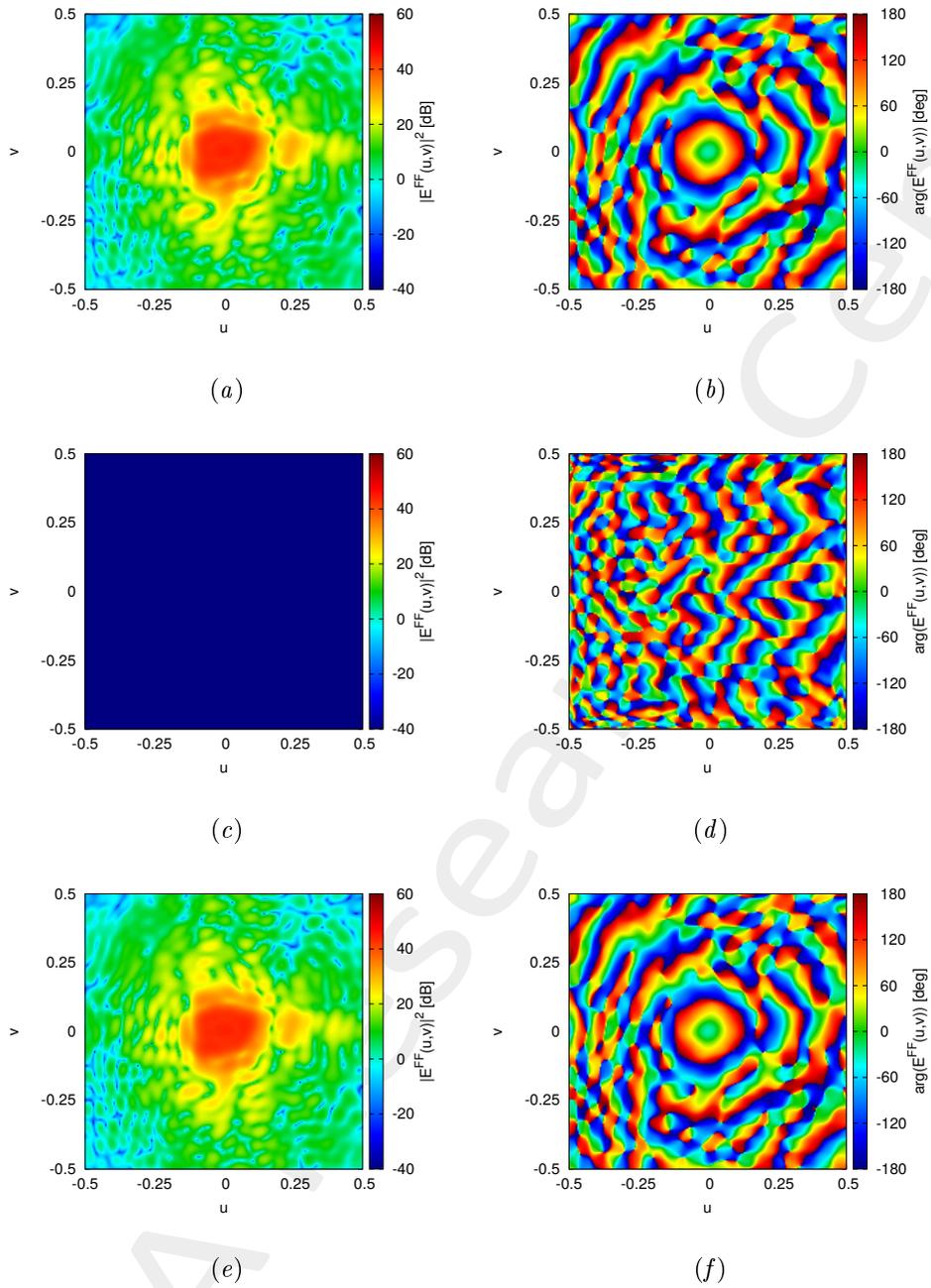


Figure 9: (a)(c)(e) Magnitude and (b)(d)(f) phase of the radiated field by (a)(b),  $J^{MN}(x, y)$ , (c)(d)  $J^{NR}(x, y; \underline{\alpha})$ , and (e)(f)  $J^{TOT}(x, y; \underline{\alpha})$ .

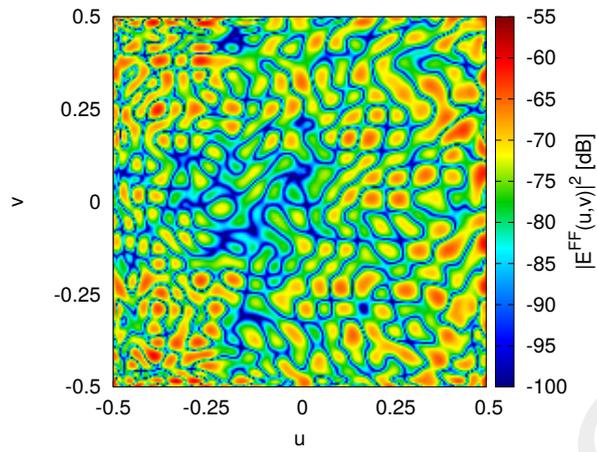


Figure 10: Magnitude of the difference between the radiated fields by  $J^{MN}(x, y)$  and  $J^{TOT}(x, y; \underline{\alpha})$ .

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### 1.3 Shape “O @ Center”

#### Parameters

- Number of reflectarray elements:  $M = 81, N = 69$ ;
- Operative frequency:  $f = 3.6$  [GHz];
- Polarization: L-CO;
- Number of elements in the forbidden region:  $Q = 24$ ;

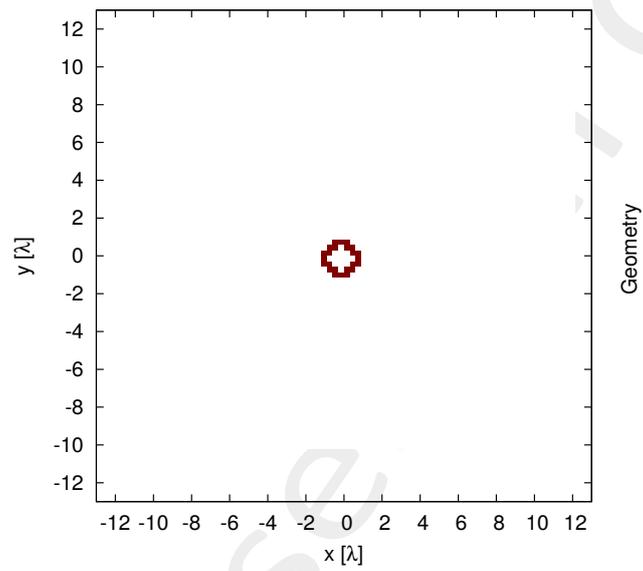


Figure 11: Geometry of forbidden region  $\Omega$ .

## Results

Magnitude and phase of the  $NR$  coefficients.

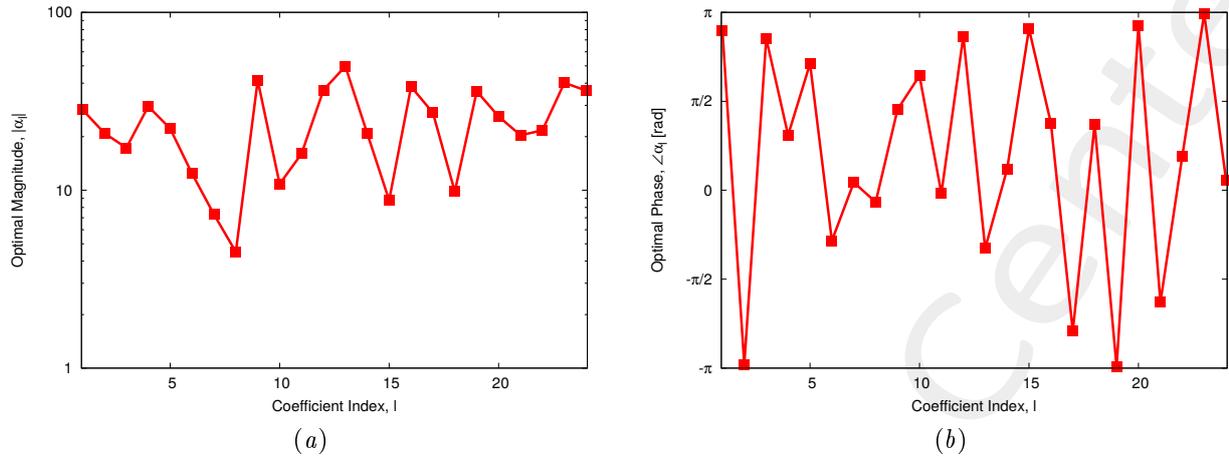


Figure 12: Magnitude (a) and phase (b) of the solution.

Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$	Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$
1	$-2.68 \times 10^1$	9.09	13	$2.58 \times 10^1$	$-4.25 \times 10^1$
2	$-2.09 \times 10^1$	-1.29	14	$1.94 \times 10^1$	7.59
3	$-1.55 \times 10^1$	7.69	15	-8.42	2.52
4	$1.66 \times 10^1$	$2.45 \times 10^1$	16	$1.44 \times 10^1$	$3.54 \times 10^1$
5	$-1.37 \times 10^1$	$1.75 \times 10^1$	17	$-2.16 \times 10^1$	$-1.66 \times 10^1$
6	7.78	-9.64	18	3.90	9.02
7	7.24	1.01	19	$-3.60 \times 10^1$	$-7.66 \times 10^{-1}$
8	4.40	$-9.34 \times 10^{-1}$	20	$-2.53 \times 10^1$	5.98
9	5.94	$4.11 \times 10^1$	21	-8.06	$-1.87 \times 10^1$
10	-4.74	9.75	22	$1.79 \times 10^1$	$1.23 \times 10^1$
11	$1.60 \times 10^1$	$-8.90 \times 10^{-1}$	23	$-4.02 \times 10^1$	$8.72 \times 10^{-1}$
12	$-3.34 \times 10^1$	$1.50 \times 10^1$	24	$3.58 \times 10^1$	6.35

Table III: Solution of the linear system.

## Currents Distribution

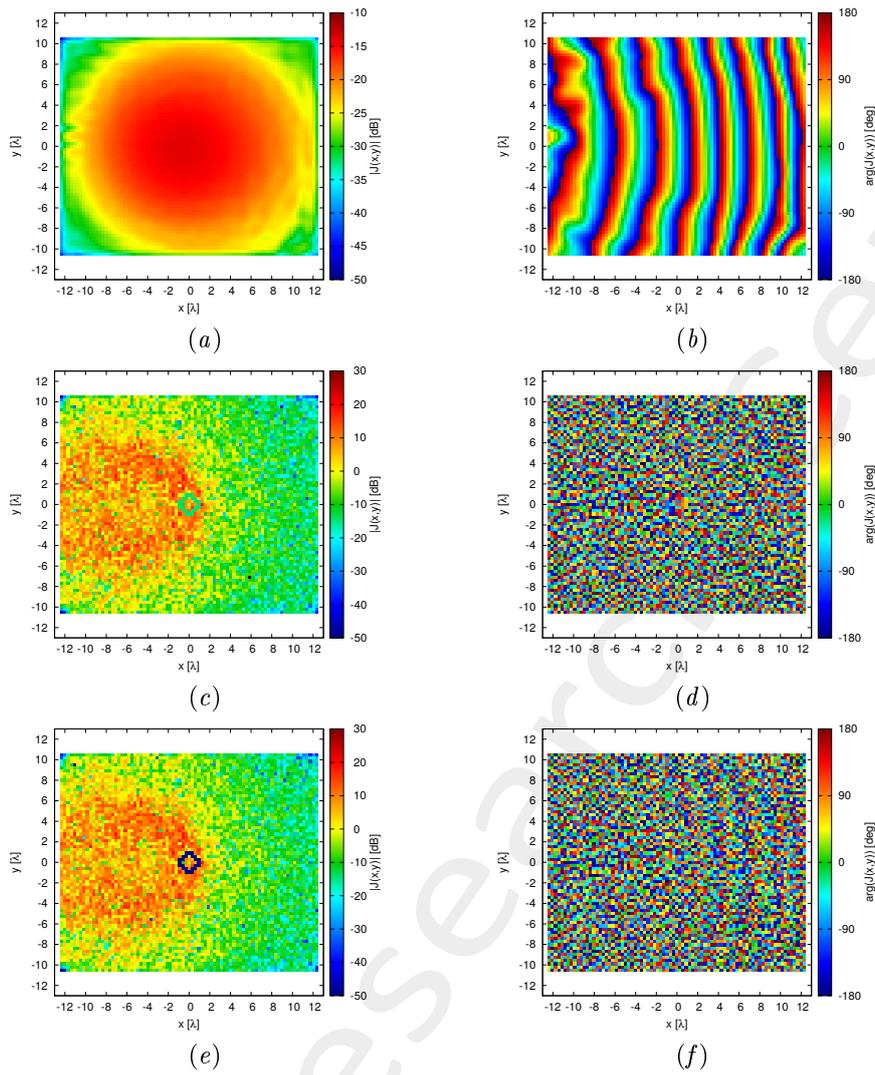


Figure 13: (a)(c)(e) Magnitude and (b)(d)(f) phase (a)(b) of  $J^{MN}(x, y)$ , (c)(d)  $J^{NR}(x, y; \underline{\alpha})$ , and (e)(f)  $J^{TOT}(x, y; \underline{\alpha})$ .

## Radiated Field

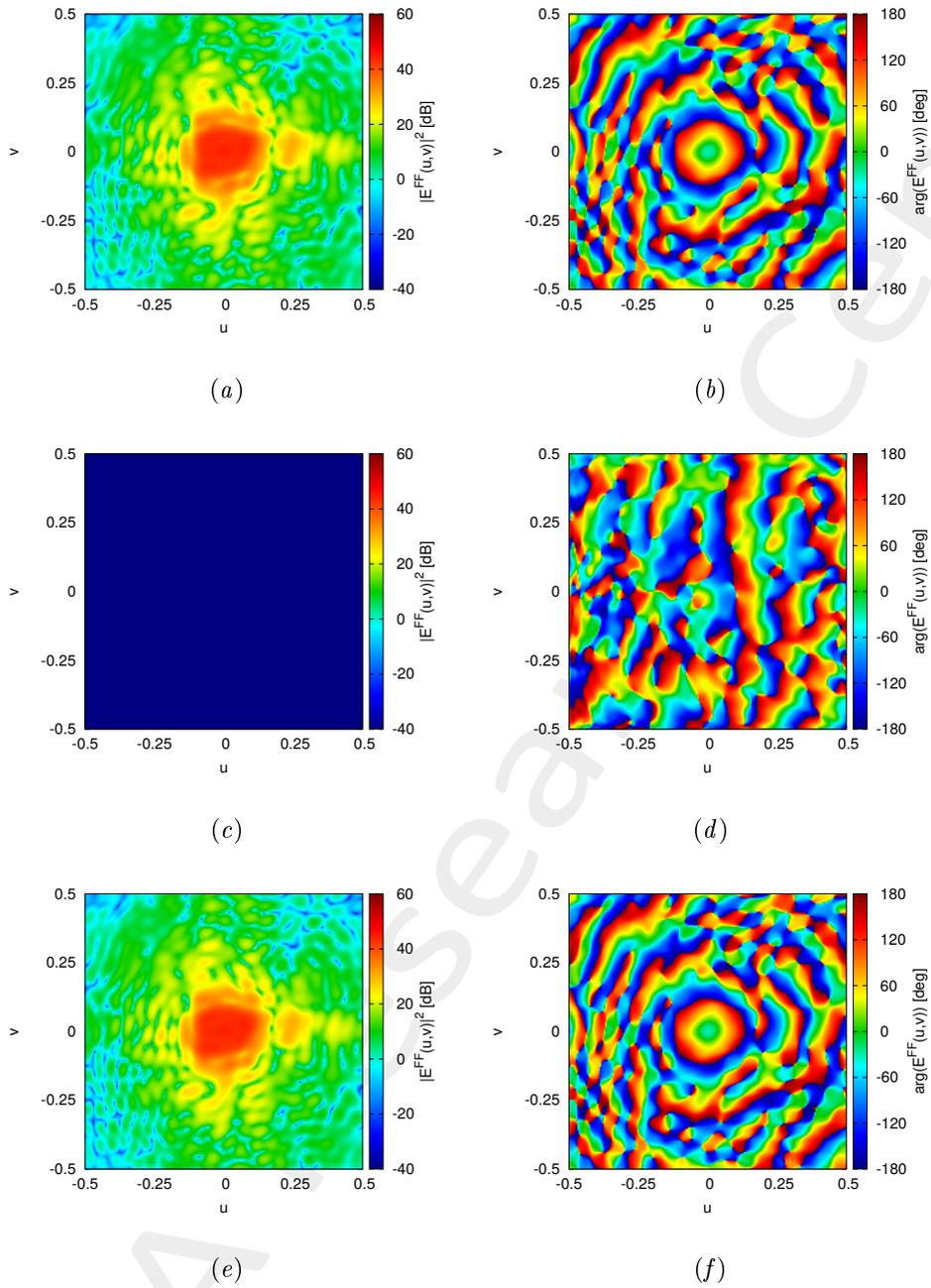


Figure 14: (a)(c)(e) Magnitude and (b)(d)(f) phase of the radiated field by (a)(b),  $J^{MN}(x, y)$ , (c)(d)  $J^{NR}(x, y; \underline{\alpha})$ , and (e)(f)  $J^{TOT}(x, y; \underline{\alpha})$ .

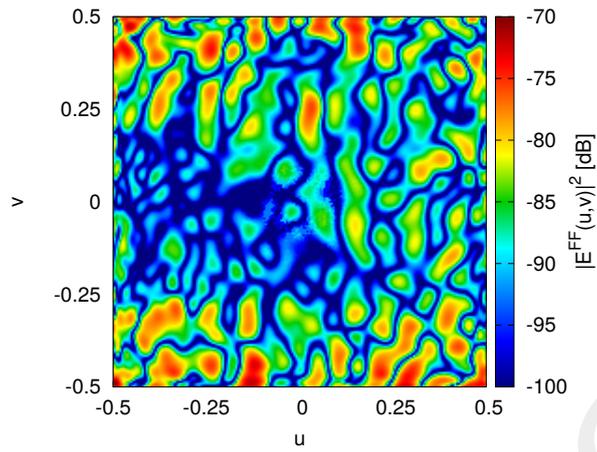


Figure 15: Magnitude of the difference between the radiated fields by  $J^{MN}(x, y)$  and  $J^{TOT}(x, y; \underline{\alpha})$ .

## 1.4 Shape “2 O @ Center and up right corner”

### Parameters

- Number of reflectarray elements:  $M = 81, N = 69$ ;
- Operative frequency:  $f = 3.6$  [GHz];
- Polarization: L-CO;
- Number of elements in the forbidden region:  $Q = 36$ ;

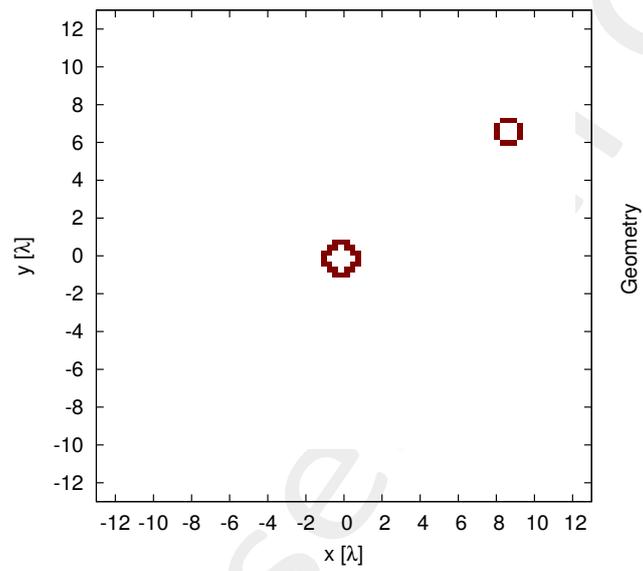


Figure 16: Geometry of forbidden region  $\Omega$ .

## Results

Magnitude and phase of the  $NR$  coefficients.

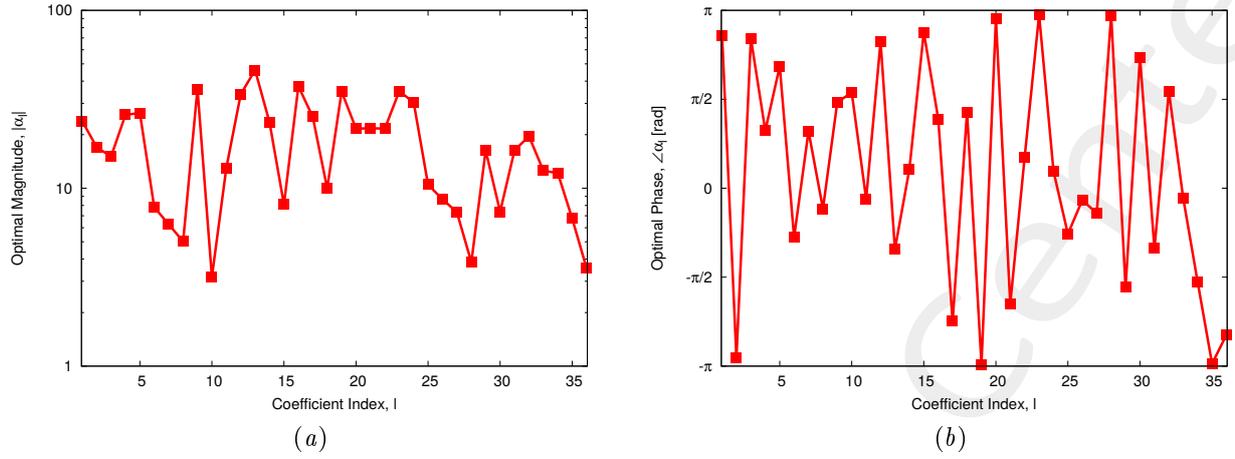


Figure 17: Magnitude (a) and phase (b) of the solution.

Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$	Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$	Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$
1	$-2.15 \times 10^1$	$1.03 \times 10^1$	13	$2.18 \times 10^1$	$-4.06 \times 10^1$	25	7.24	-7.55
2	$-1.69 \times 10^1$	-2.51	14	$2.22 \times 10^1$	7.71	26	8.48	-1.81
3	$-1.32 \times 10^1$	7.15	15	-7.50	3.05	27	6.63	-3.14
4	$1.36 \times 10^1$	$2.20 \times 10^1$	16	$1.27 \times 10^1$	$3.52 \times 10^1$	28	-3.82	$3.26 \times 10^{-1}$
5	$-1.46 \times 10^1$	$2.21 \times 10^1$	17	$-1.77 \times 10^1$	$-1.80 \times 10^1$	29	-2.90	$-1.61 \times 10^1$
6	5.06	-5.96	18	2.23	9.73	30	-5.00	5.43
7	3.35	5.30	19	$-3.49 \times 10^1$	-1.15	31	7.96	$-1.43 \times 10^1$
8	4.69	-1.78	20	$-2.14 \times 10^1$	3.23	32	-2.77	$1.94 \times 10^1$
9	1.93	$3.61 \times 10^1$	21	-9.93	$-1.94 \times 10^1$	33	$1.24 \times 10^1$	-2.18
10	$-3.83 \times 10^{-1}$	3.15	22	$1.84 \times 10^1$	$1.14 \times 10^1$	34	-1.01	$-1.21 \times 10^1$
11	$1.28 \times 10^1$	-2.45	23	$-3.50 \times 10^1$	2.67	35	-6.75	$-2.93 \times 10^{-1}$
12	$-2.88 \times 10^1$	$1.77 \times 10^1$	24	$2.90 \times 10^1$	8.91	36	-3.03	-1.86

Table IV: Solution of the linear system.

## Currents Distribution

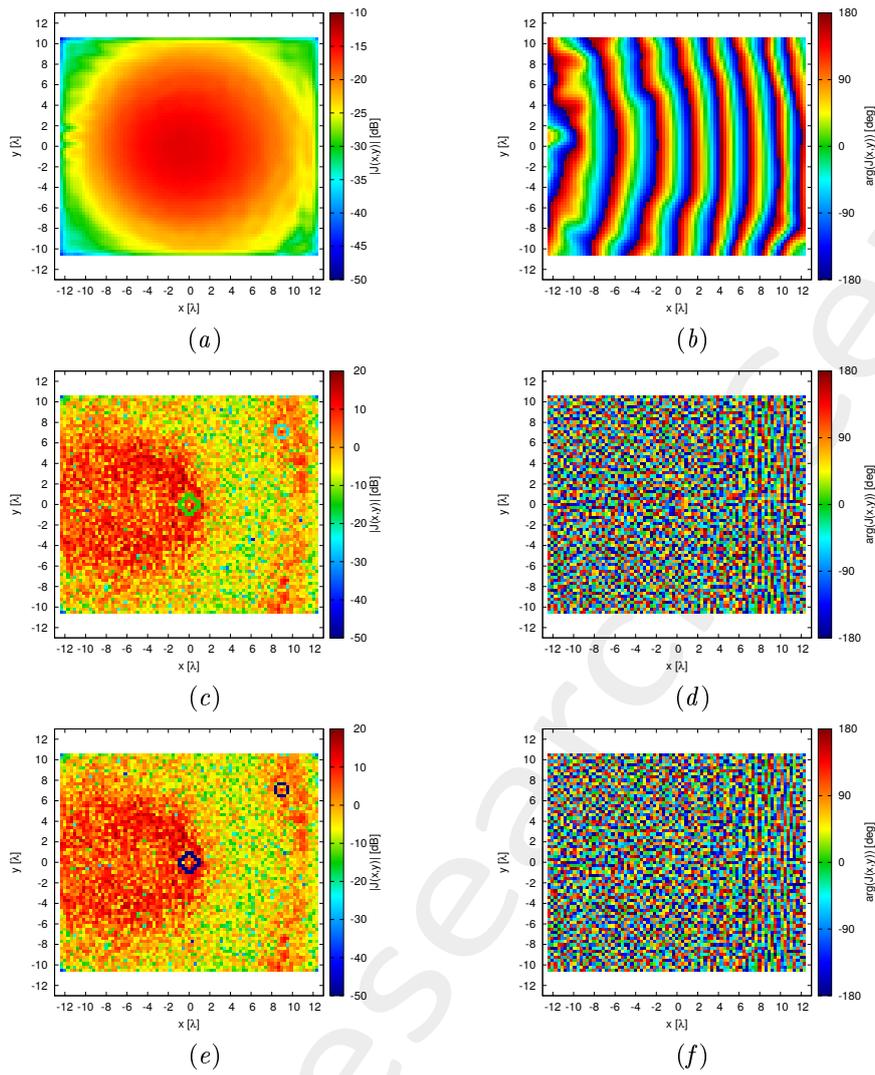


Figure 18: (a)(c)(e) Magnitude and (b)(d)(f) phase (a)(b) of  $J^{MN}(x, y)$ , (c)(d)  $J^{NR}(x, y; \underline{\alpha})$ , and (e)(f)  $J^{TOT}(x, y; \underline{\alpha})$ .

## Radiated Field

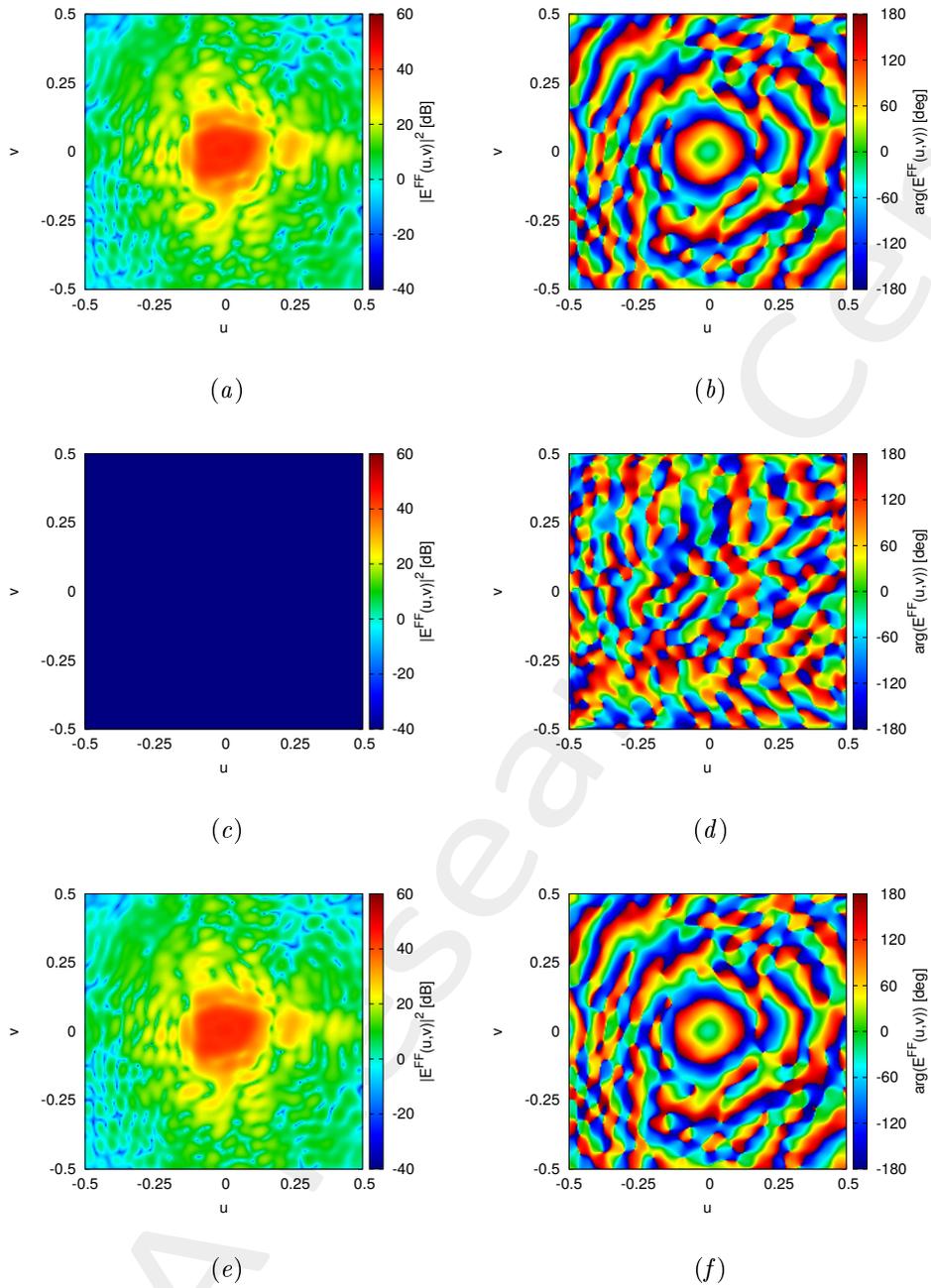


Figure 19: (a)(c)(e) Magnitude and (b)(d)(f) phase of the radiated field by (a)(b),  $J^{MN}(x, y)$ , (c)(d)  $J^{NR}(x, y; \underline{\alpha})$ , and (e)(f)  $J^{TOT}(x, y; \underline{\alpha})$ .

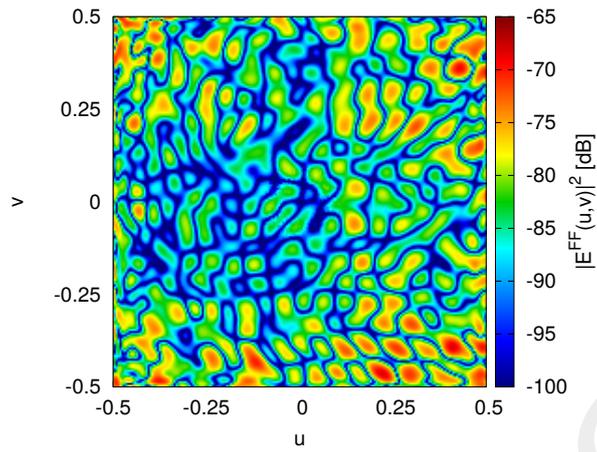


Figure 20: Magnitude of the difference between the radiated fields by  $J^{MN}(x, y)$  and  $J^{TOT}(x, y; \underline{\alpha})$ .

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## 1.5 Shape “Circle @ Center”

### Parameters

- Number of reflectarray elements:  $M = 81, N = 69$ ;
- Operative frequency:  $f = 3.6$  [GHz];
- Polarization: L-CO;
- Number of elements in the forbidden region:  $Q = 37$ ;

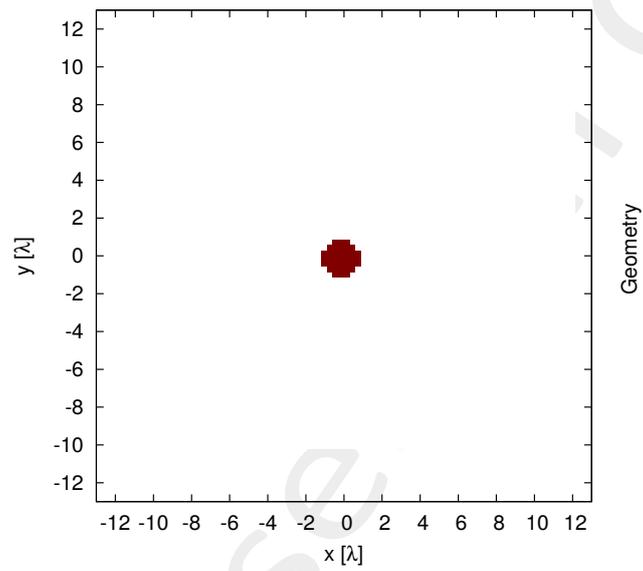


Figure 21: Geometry of forbidden region  $\Omega$ .

## Results

Magnitude and phase of the  $NR$  coefficients.

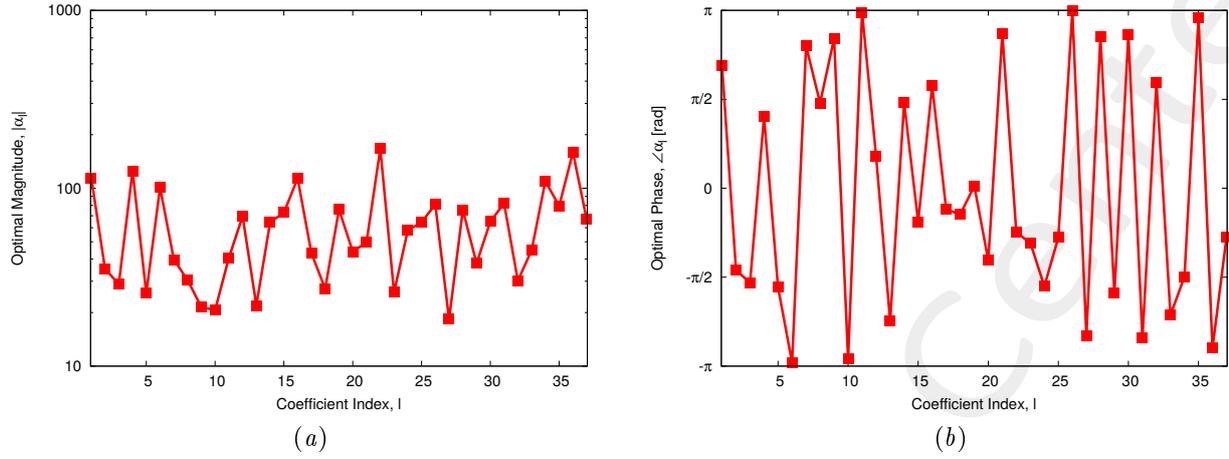


Figure 22: Magnitude (a) and phase (b) of the solution.

Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$	Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$	Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$
1	$-6.39 \times 10^1$	$9.49 \times 10^1$	14	4.04	$6.42 \times 10^1$	26	$-8.11 \times 10^1$	1.05
2	4.48	$-3.49 \times 10^1$	15	$6.06 \times 10^1$	$-4.07 \times 10^1$	27	$-1.57 \times 10^1$	-9.43
3	-2.94	$-2.87 \times 10^1$	16	$-2.67 \times 10^1$	$1.10 \times 10^2$	28	$-6.76 \times 10^1$	$3.36 \times 10^1$
4	$3.73 \times 10^1$	$1.20 \times 10^2$	17	$4.02 \times 10^1$	$-1.57 \times 10^1$	29	$-1.06 \times 10^1$	$-3.63 \times 10^1$
5	-4.60	$-2.53 \times 10^1$	18	$2.44 \times 10^1$	$-1.22 \times 10^1$	30	$-5.91 \times 10^1$	$2.67 \times 10^1$
6	$-1.01 \times 10^2$	-6.07	19	$7.58 \times 10^1$	3.10	31	$-7.24 \times 10^1$	$-3.89 \times 10^1$
7	$-3.21 \times 10^1$	$2.33 \times 10^1$	20	$1.29 \times 10^1$	$-4.21 \times 10^1$	32	-8.77	$2.89 \times 10^1$
8	2.04	$3.04 \times 10^1$	21	$-4.56 \times 10^1$	$1.96 \times 10^1$	33	$-2.78 \times 10^1$	$-3.51 \times 10^1$
9	$-1.89 \times 10^1$	$1.02 \times 10^1$	22	$1.18 \times 10^2$	$-1.18 \times 10^2$	34	$6.91 \times 10^{-1}$	$-1.10 \times 10^2$
10	$-2.05 \times 10^1$	-2.58	23	$1.48 \times 10^1$	$-2.13 \times 10^1$	35	$-7.88 \times 10^1$	$1.01 \times 10^1$
11	$-4.06 \times 10^1$	1.52	24	-9.27	$-5.72 \times 10^1$	36	$-1.52 \times 10^2$	$-4.98 \times 10^1$
12	$5.89 \times 10^1$	$3.70 \times 10^1$	25	$4.16 \times 10^1$	$-4.92 \times 10^1$	37	$4.31 \times 10^1$	$-5.11 \times 10^1$
13	$-1.53 \times 10^1$	$-1.57 \times 10^1$						

Table V: Solution of the linear system.

## Currents Distribution

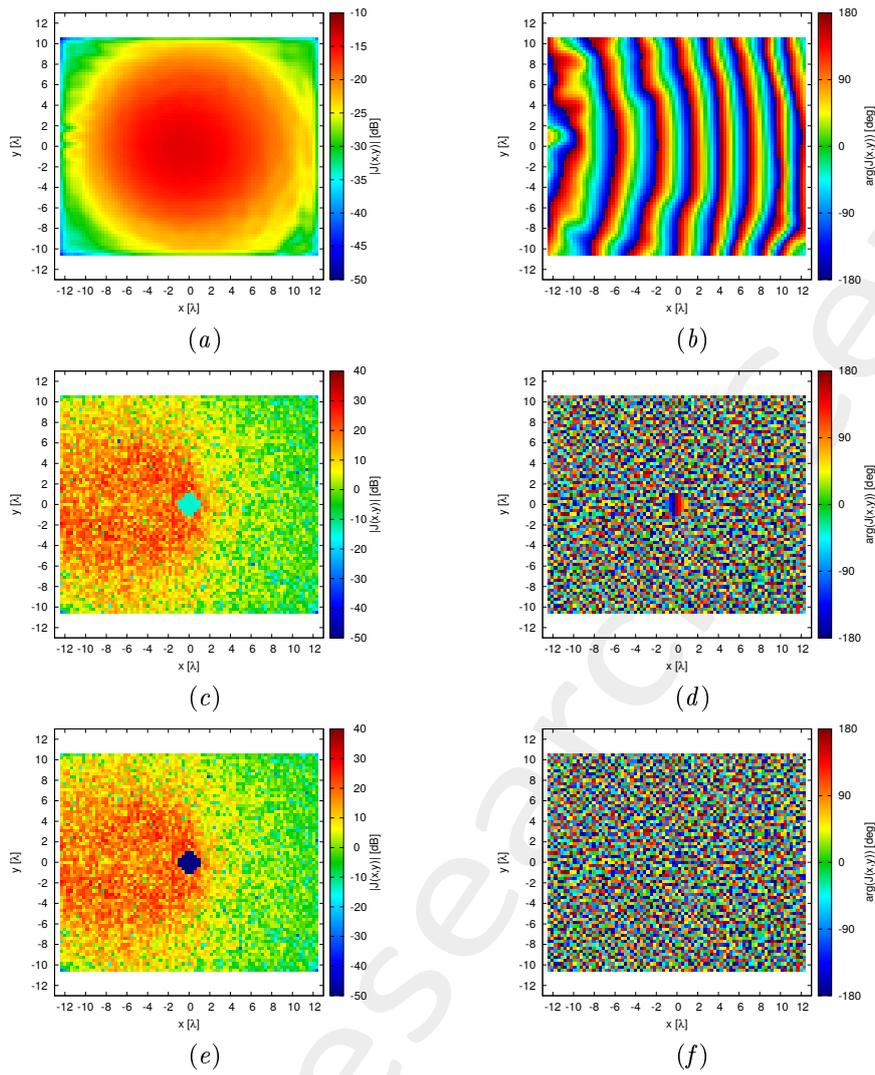


Figure 23: (a)(c)(e) Magnitude and (b)(d)(f) phase (a)(b) of  $J^{MN}(x, y)$ , (c)(d)  $J^{NR}(x, y; \underline{\alpha})$ , and (e)(f)  $J^{TOT}(x, y; \underline{\alpha})$ .

## Radiated Field

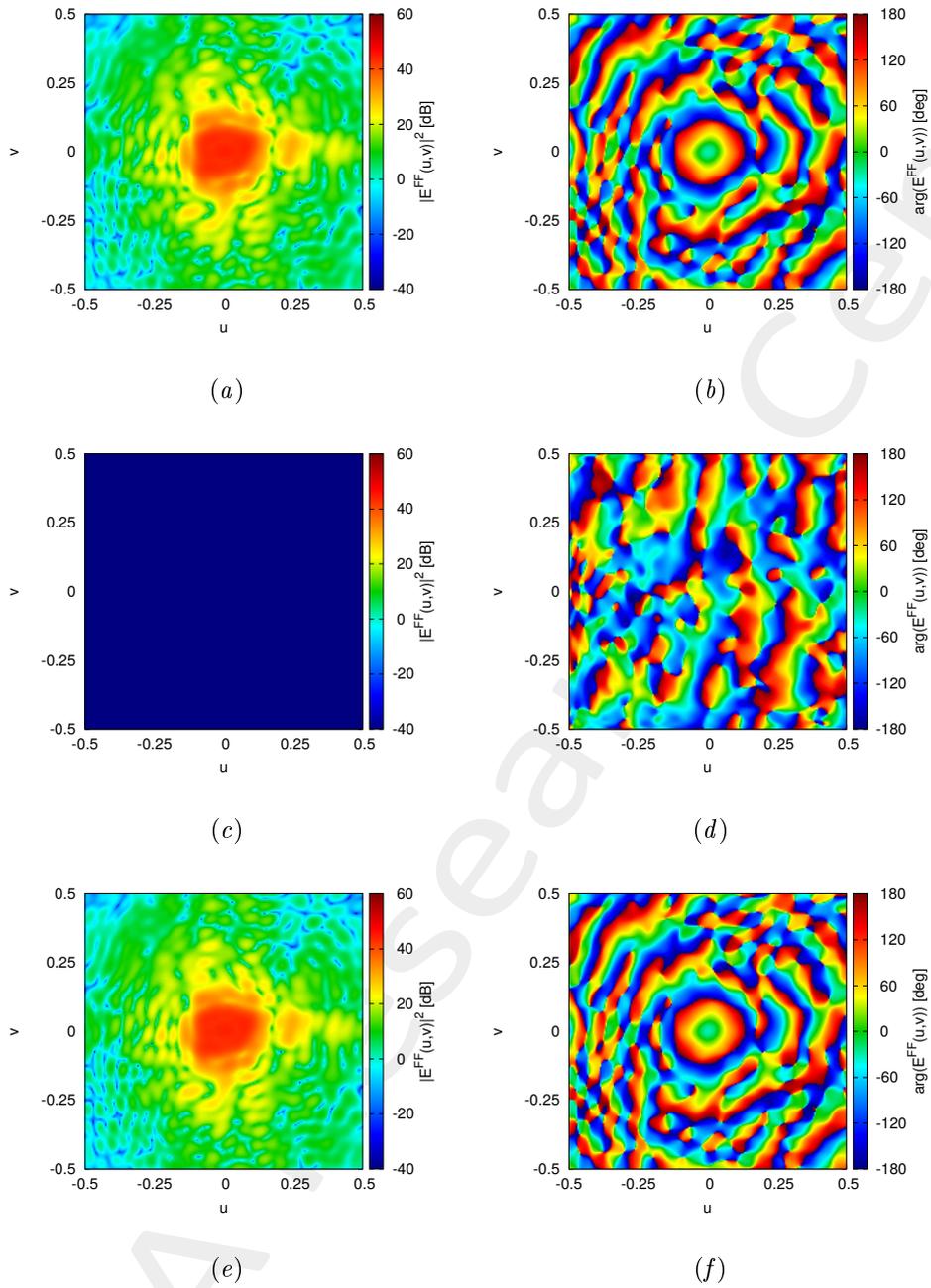


Figure 24: (a)(c)(e) Magnitude and (b)(d)(f) phase of the radiated field by (a)(b),  $J^{MN}(x, y)$ , (c)(d)  $J^{NR}(x, y; \underline{\alpha})$ , and (e)(f)  $J^{TOT}(x, y; \underline{\alpha})$ .

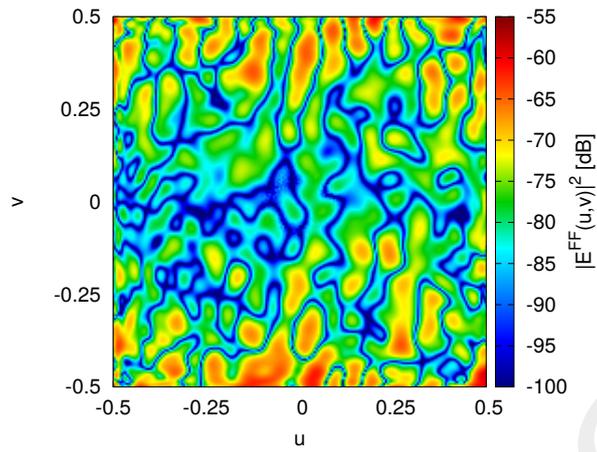


Figure 25: Magnitude of the difference between the radiated fields by  $J^{MN}(x, y)$  and  $J^{TOT}(x, y; \underline{\alpha})$ .

## 1.6 Shape “2 Circle @ Center and up right corner”

### Parameters

- Number of reflectarray elements:  $M = 81, N = 69$ ;
- Operative frequency:  $f = 3.6$  [GHz];
- Polarization: L-CO;
- Number of elements in the forbidden region:  $Q = 58$ ;

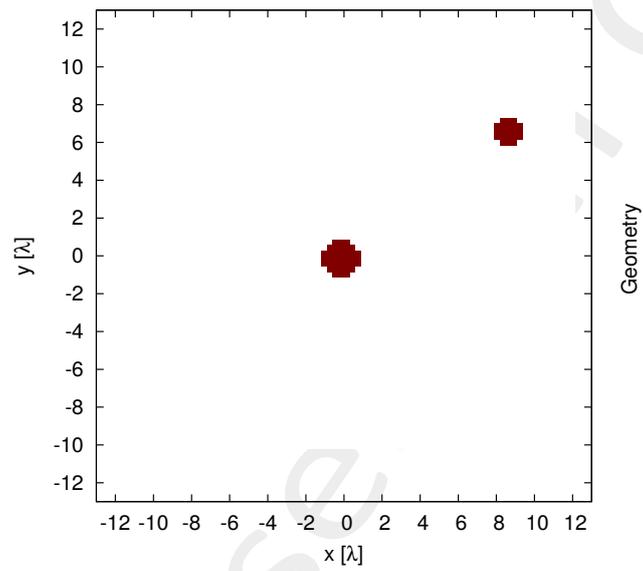


Figure 26: Geometry of forbidden region  $\Omega$ .

## Results

Magnitude and phase of the  $NR$  coefficients.

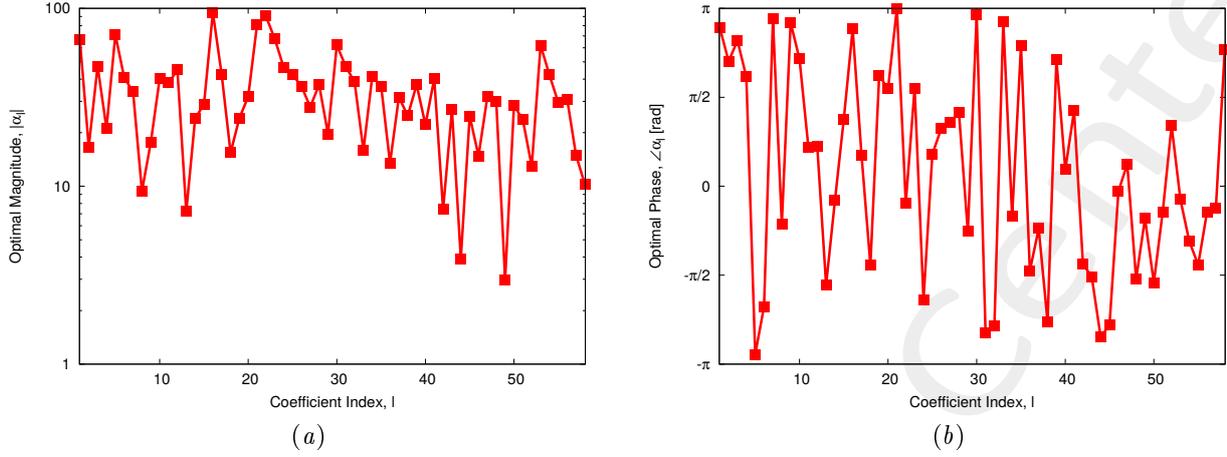


Figure 27: Magnitude (a) and phase (b) of the solution.

Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$	Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$	Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$
1	$-6.30 \times 10^1$	$2.22 \times 10^1$	21	$-8.09 \times 10^1$	$1.72 \times 10^{-1}$	40	$2.12 \times 10^1$	6.45
2	-9.91	$1.34 \times 10^1$	22	$8.64 \times 10^1$	$-2.69 \times 10^1$	41	9.53	$3.92 \times 10^1$
3	$-3.99 \times 10^1$	$2.56 \times 10^1$	23	$-1.08 \times 10^1$	$6.64 \times 10^1$	42	1.46	-7.26
4	-7.47	$1.98 \times 10^1$	24	$-1.96 \times 10^1$	$-4.24 \times 10^1$	43	$-8.66 \times 10^{-1}$	$-2.69 \times 10^1$
5	$-7.01 \times 10^1$	$-1.22 \times 10^1$	25	$3.57 \times 10^1$	$2.28 \times 10^1$	44	-3.47	-1.80
6	$-2.15 \times 10^1$	$-3.47 \times 10^1$	26	$1.92 \times 10^1$	$3.11 \times 10^1$	45	$-1.91 \times 10^1$	$-1.59 \times 10^1$
7	$-3.33 \times 10^1$	6.38	27	$1.22 \times 10^1$	$2.51 \times 10^1$	46	$1.47 \times 10^1$	-1.32
8	7.39	-5.79	28	$1.01 \times 10^1$	$3.58 \times 10^1$	47	$2.95 \times 10^1$	$1.22 \times 10^1$
9	$-1.71 \times 10^1$	4.45	29	$1.37 \times 10^1$	$-1.41 \times 10^1$	48	-1.94	$-2.98 \times 10^1$
10	$-2.52 \times 10^1$	$3.14 \times 10^1$	30	$-6.18 \times 10^1$	6.89	49	2.52	-1.62
11	$2.94 \times 10^1$	$2.43 \times 10^1$	31	$-4.02 \times 10^1$	$-2.46 \times 10^1$	50	-3.74	$-2.82 \times 10^1$
12	$3.42 \times 10^1$	$2.93 \times 10^1$	32	$-3.01 \times 10^1$	$-2.42 \times 10^1$	51	$2.13 \times 10^1$	$-1.03 \times 10^1$
13	-1.22	-7.10	33	$-1.55 \times 10^1$	3.56	52	6.19	$1.14 \times 10^1$
14	$2.33 \times 10^1$	-5.96	34	$3.58 \times 10^1$	$-2.11 \times 10^1$	53	$6.03 \times 10^1$	$-1.46 \times 10^1$
15	$1.08 \times 10^1$	$2.68 \times 10^1$	35	$-2.90 \times 10^1$	$2.23 \times 10^1$	54	$2.37 \times 10^1$	$-3.49 \times 10^1$
16	$-8.86 \times 10^1$	$3.38 \times 10^1$	36	1.01	$-1.34 \times 10^1$	55	5.36	$-2.90 \times 10^1$
17	$3.61 \times 10^1$	$2.20 \times 10^1$	37	$2.32 \times 10^1$	$-2.16 \times 10^1$	56	$2.77 \times 10^1$	$-1.35 \times 10^1$
18	2.70	$-1.52 \times 10^1$	38	$-1.83 \times 10^1$	$-1.70 \times 10^1$	57	$1.39 \times 10^1$	-5.57
19	-9.09	$2.23 \times 10^1$	39	$-2.32 \times 10^1$	$2.91 \times 10^1$	58	-7.62	6.86
20	-4.70	$3.15 \times 10^1$						

Table VI: Solution of the linear system.

## Currents Distribution

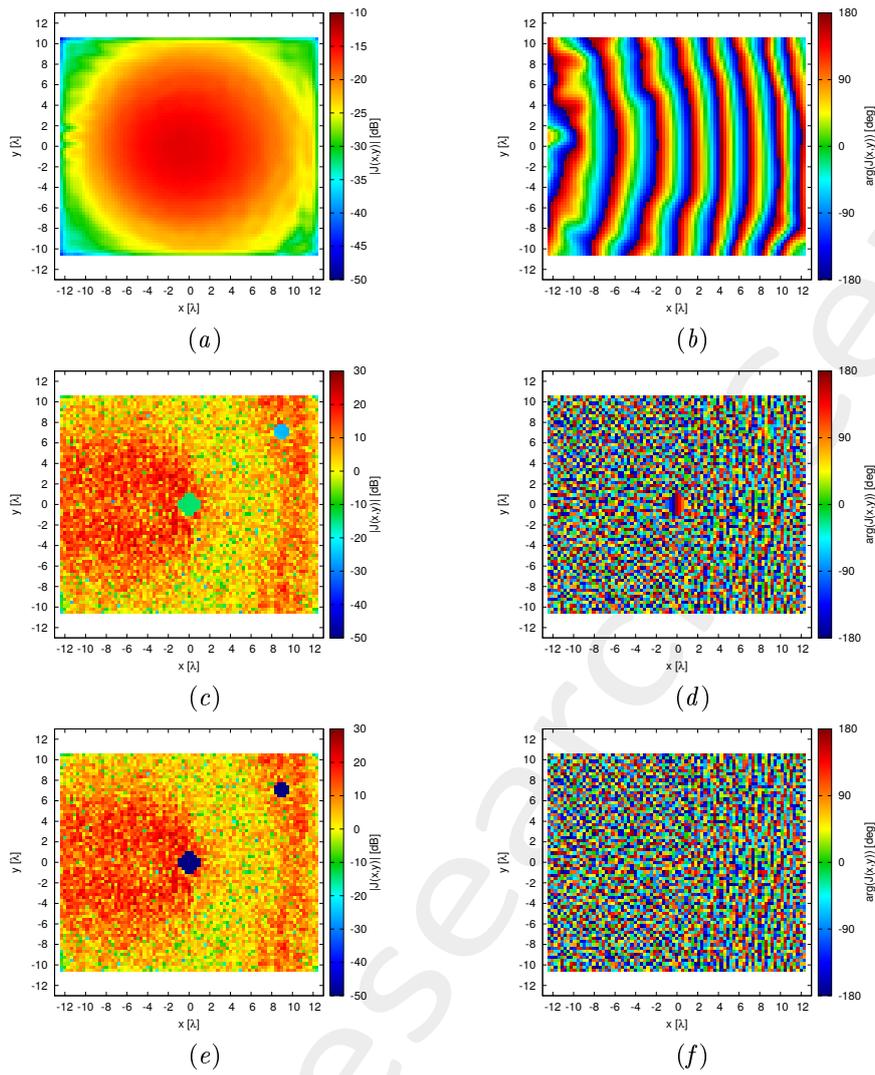


Figure 28: (a)(c)(e) Magnitude and (b)(d)(f) phase (a)(b) of  $J^{MN}(x, y)$ , (c)(d)  $J^{NR}(x, y; \underline{\alpha})$ , and (e)(f)  $J^{TOT}(x, y; \underline{\alpha})$ .

## Radiated Field

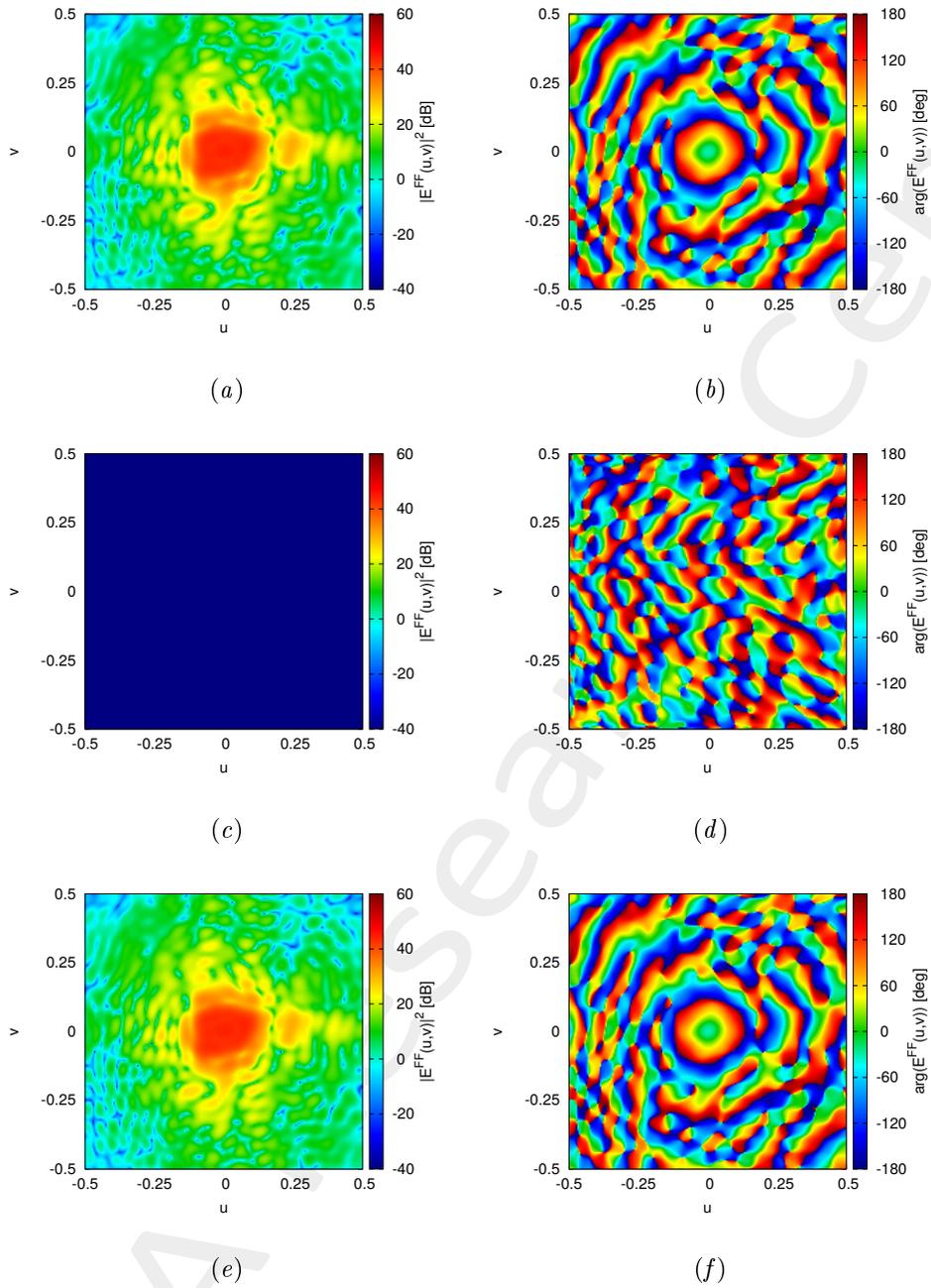


Figure 29: (a)(c)(e) Magnitude and (b)(d)(f) phase of the radiated field by (a)(b),  $J^{MN}(x, y)$ , (c)(d)  $J^{NR}(x, y; \underline{\alpha})$ , and (e)(f)  $J^{TOT}(x, y; \underline{\alpha})$ .

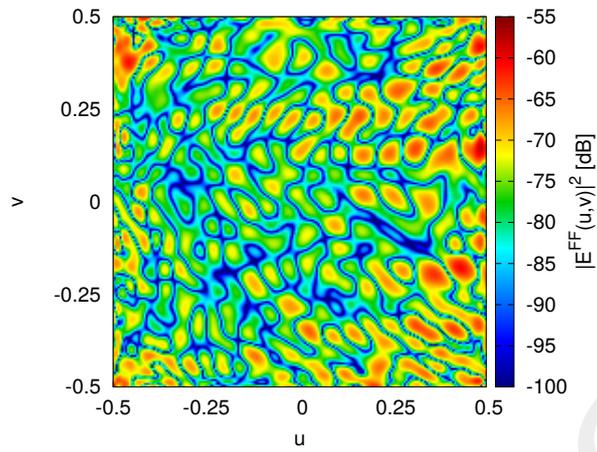


Figure 30: Magnitude of the difference between the radiated fields by  $J^{MN}(x, y)$  and  $J^{TOT}(x, y; \underline{\alpha})$ .

## 1.7 Shape “Plus @ down left corner”

### Parameters

- Number of reflectarray elements:  $M = 81, N = 69$ ;
- Operative frequency:  $f = 3.6$  [GHz];
- Polarization: L-CO;
- Number of elements in the forbidden region:  $Q = 28$ ;

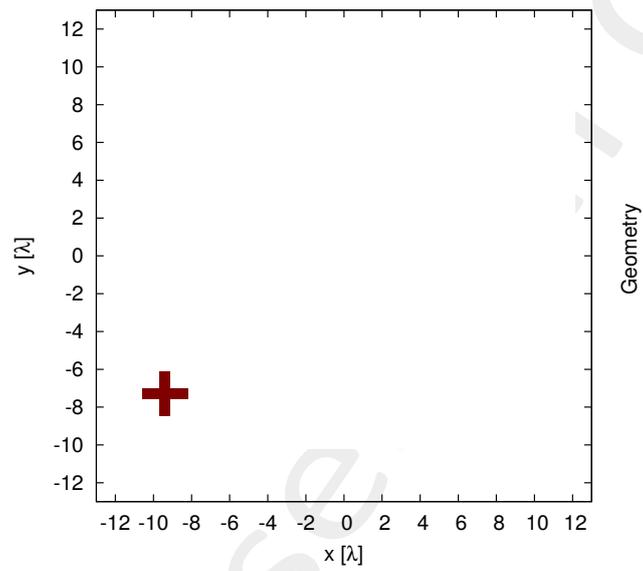


Figure 31: Geometry of forbidden region  $\Omega$ .

## Results

Magnitude and phase of the  $NR$  coefficients.

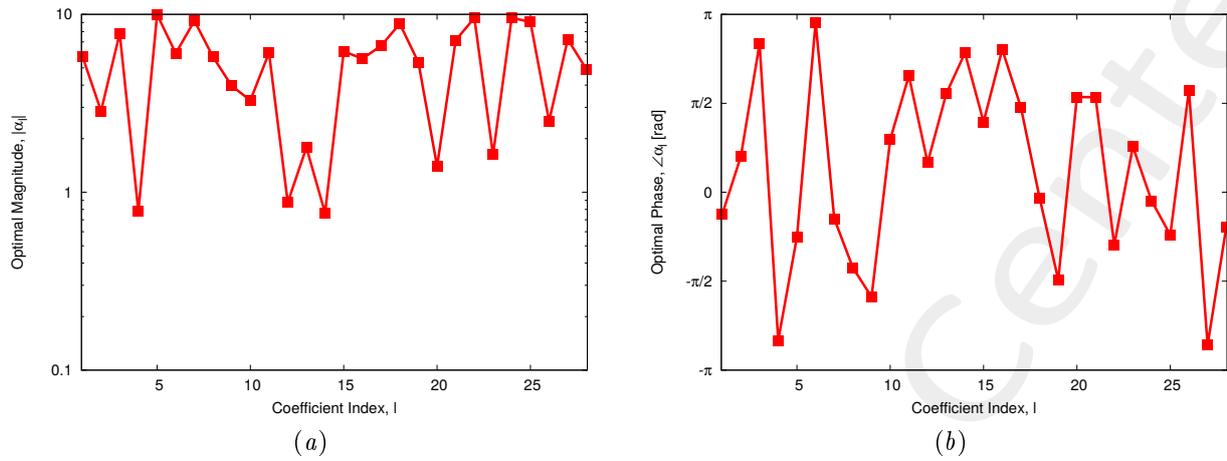


Figure 32: Magnitude (a) and phase (b) of the solution.

Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$	Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$	Index $q$	$\Re\{\alpha_q\}$	$\Im\{\alpha_q\}$
1	5.39	-2.20	11	-2.84	5.38	20	$-1.54 \times 10^{-1}$	1.39
2	2.30	1.70	12	$7.60 \times 10^{-1}$	$4.38 \times 10^{-1}$	21	$-7.65 \times 10^{-1}$	7.12
3	-6.79	3.87	13	$-2.98 \times 10^{-1}$	1.76	22	5.69	-7.66
4	$-6.78 \times 10^{-1}$	$-3.93 \times 10^{-1}$	14	$-5.95 \times 10^{-1}$	$4.82 \times 10^{-1}$	23	1.13	1.18
5	7.03	-7.07	15	2.00	5.87	24	9.47	-1.43
6	-5.98	$8.36 \times 10^{-1}$	16	-4.59	3.27	25	6.60	-6.19
7	8.21	-4.14	17	$4.62 \times 10^{-1}$	6.64	26	$-5.79 \times 10^{-1}$	2.44
8	1.35	-5.59	18	8.81	$-8.83 \times 10^{-1}$	27	-6.54	-3.11
9	-1.08	-3.81	19	$1.37 \times 10^{-1}$	-5.36	28	3.99	-2.86
10	1.96	2.63						

Table VII: Solution of the linear system.

## Currents Distribution

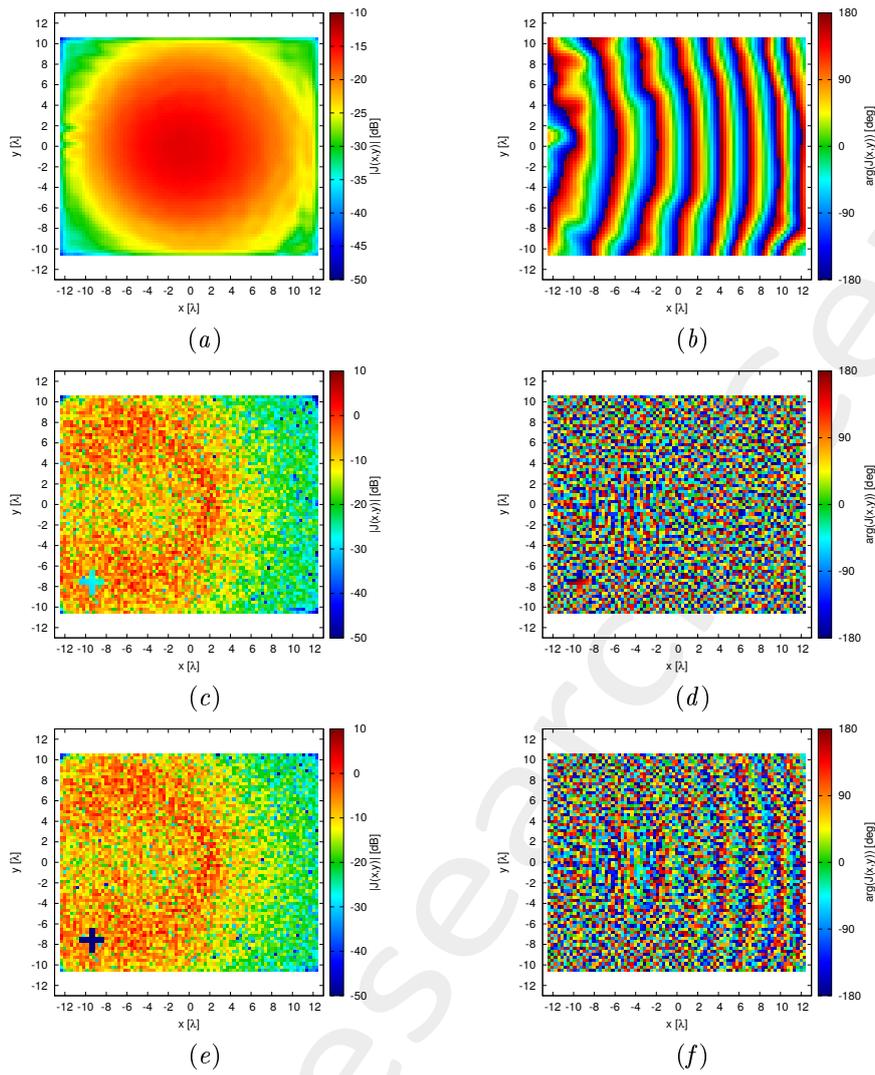


Figure 33: (a)(c)(e) Magnitude and (b)(d)(f) phase (a)(b) of  $J^{MN}(x, y)$ , (c)(d)  $J^{NR}(x, y; \underline{\alpha})$ , and (e)(f)  $J^{TOT}(x, y; \underline{\alpha})$ .

## Radiated Field

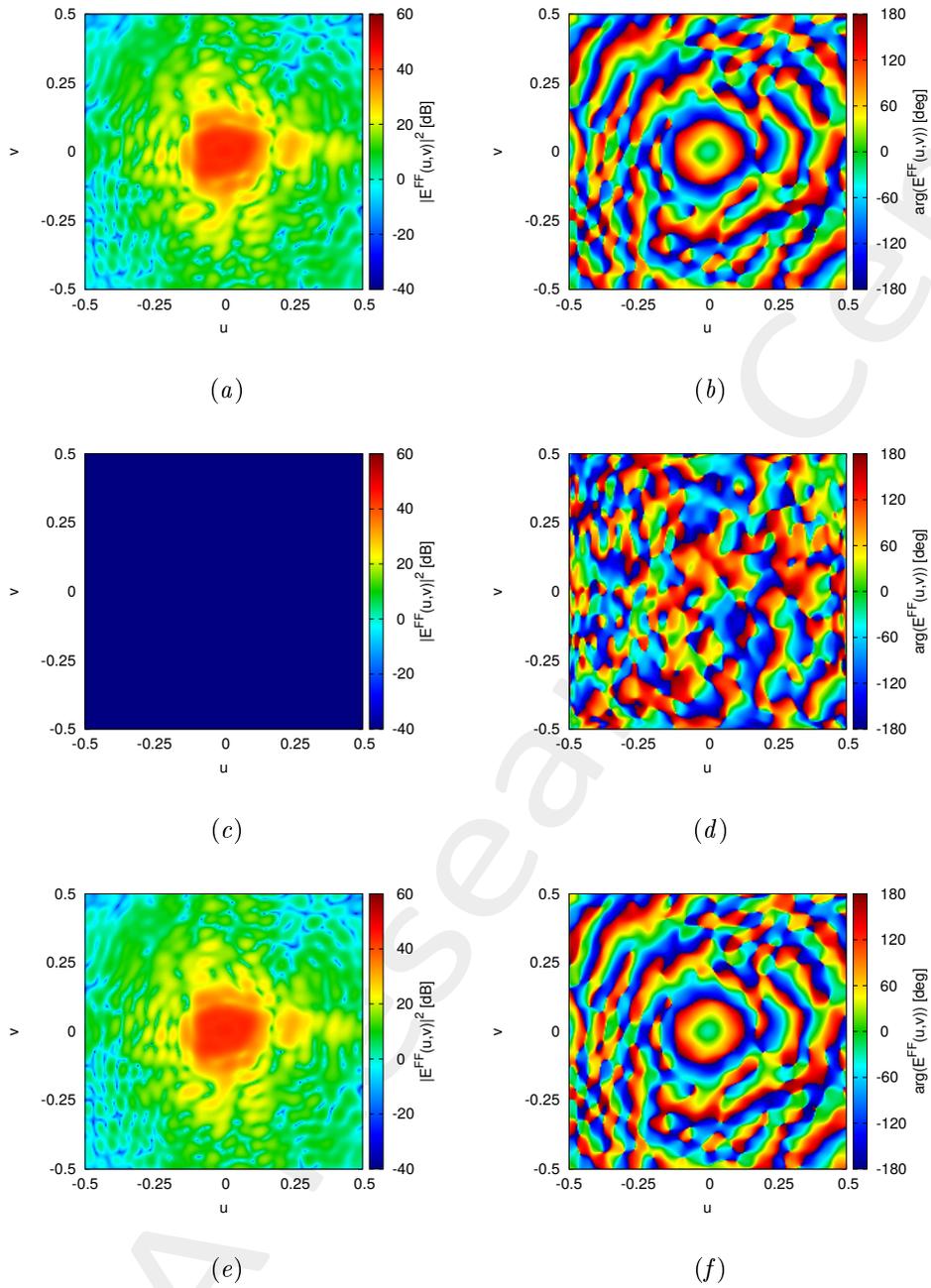


Figure 34: (a)(c)(e) Magnitude and (b)(d)(f) phase of the radiated field by (a)(b),  $J^{MN}(x, y)$ , (c)(d)  $J^{NR}(x, y; \underline{\alpha})$ , and (e)(f)  $J^{TOT}(x, y; \underline{\alpha})$ .

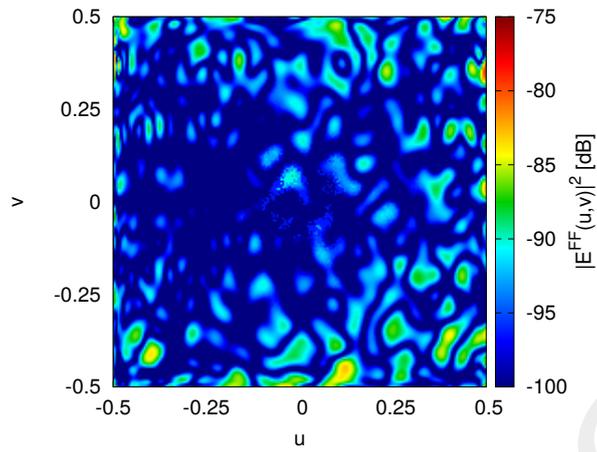


Figure 35: Magnitude of the difference between the radiated fields by  $J^{MN}(x, y)$  and  $J^{TOT}(x, y; \underline{\alpha})$ .

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