

# **A customized genetic algorithm for the synthesis of adaptive thinned array with constrained directivity**

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## **Abstract**

An innovative adaptive nulling strategy based on reconfigurable thinned arrays is studied in this report. A customized version of the genetic algorithms exploiting ad-hoc operators devoted to keep constant the number of elements instantaneously active is applied to optimize the on/off status of the switches to maximize the signal-to-interference-plus-noise ratio at the antenna output. The performances of the technique have been analyzed varying the number of array elements and the number of interferences within a static scenario.

# TEST CASE 5 - 32 Elements - Fixed Scenario, Single Interference -

$$\eta \in [0.00 - 1.00]$$

## Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a single interference.

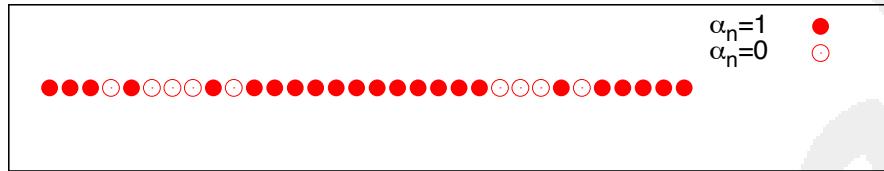
## Test Case Description

- Number of Elements  $N = 32$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 1$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ$

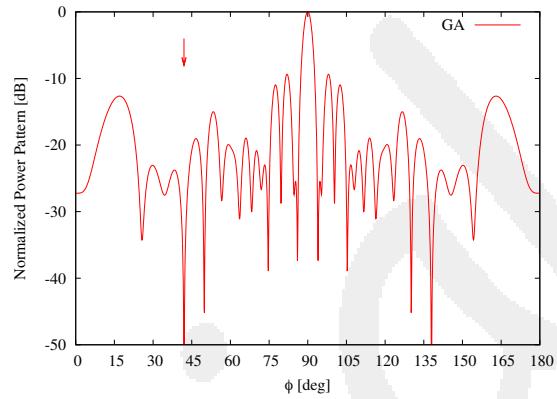
## Optimization Approach: GA

- Number of Variables:  $X = 32$  ( $\alpha_n, n = 1, \dots, N$ )
- Population: 16
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.00$
- Maximum Thinning Coefficient:  $\eta_{max} = 1.00$
- Number of Repetitions for Statistical Analysis: 20

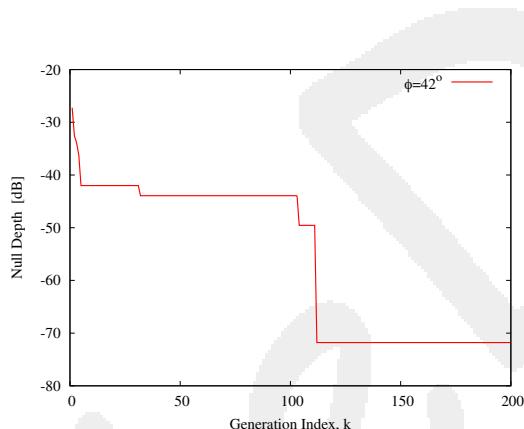
**GA - 32 Elements - Single Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$



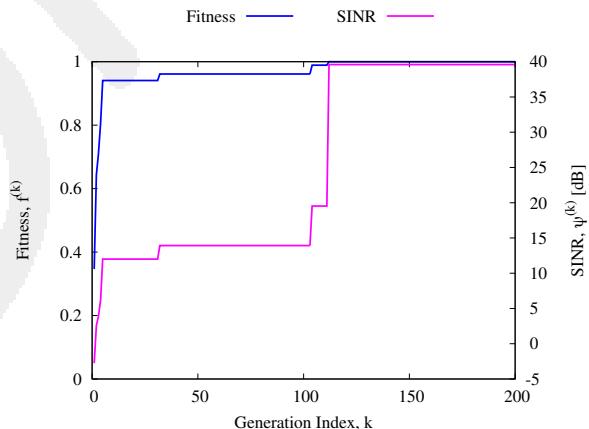
**Fig.16 - Thinning Configuration**



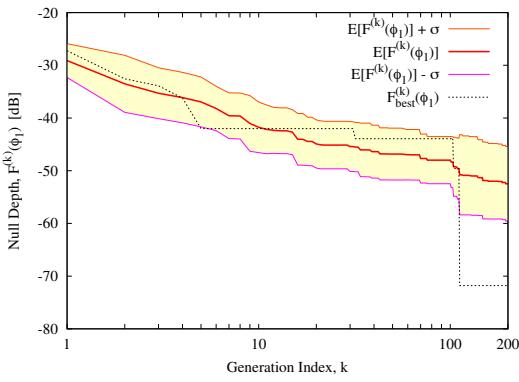
**Fig.17 - Pattern**



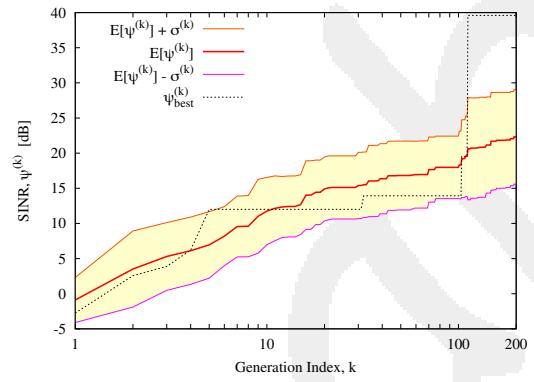
**Fig.18 - Nulls Depth**



**Fig.19 - Fitness - SINR**



**Fig.20 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics**



**Fig.21 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	Nr. Active Elements	SINR [dB]
GA	-71.79	23	39.60

**Tab.6 - GA Simulation Results Analysis**

## TEST CASE 6 - 32 Elements - Fixed Scenario, Single Interference - $\eta \in [0.50 - 0.70]$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a single interference.

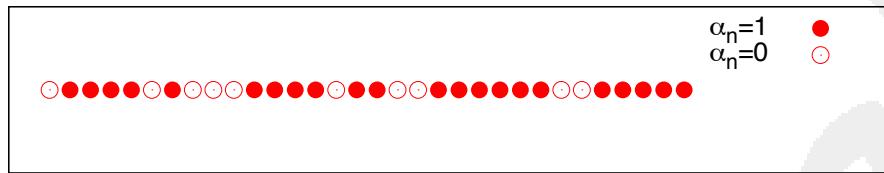
### Test Case Description

- Number of Elements  $N = 32$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 1$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ$

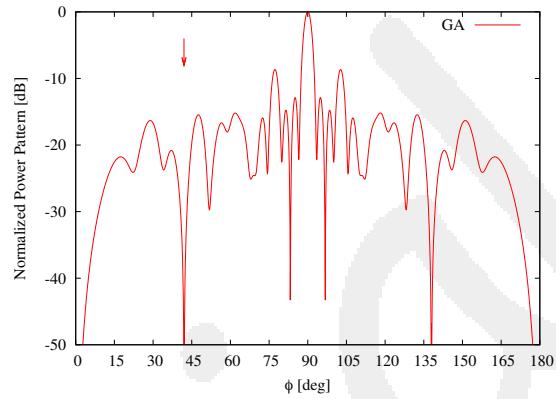
### Optimization Approach: GA

- Number of Variables:  $X = 32$  ( $\alpha_n, n = 1, \dots, N$ )
- Population: 16
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.50$
- Maximum Thinning Coefficient:  $\eta_{max} = 0.70$
- Number of Repetitions for Statistical Analysis: 20

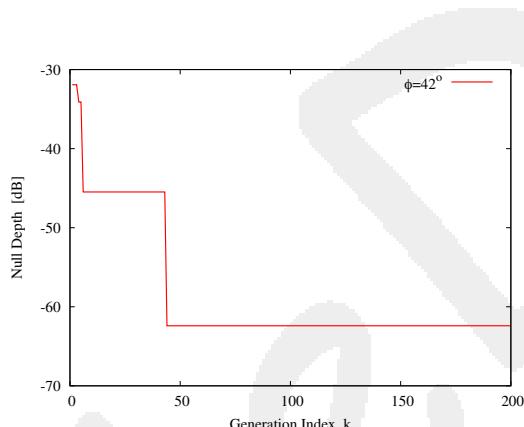
**GA - 32 Elements - Single Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$



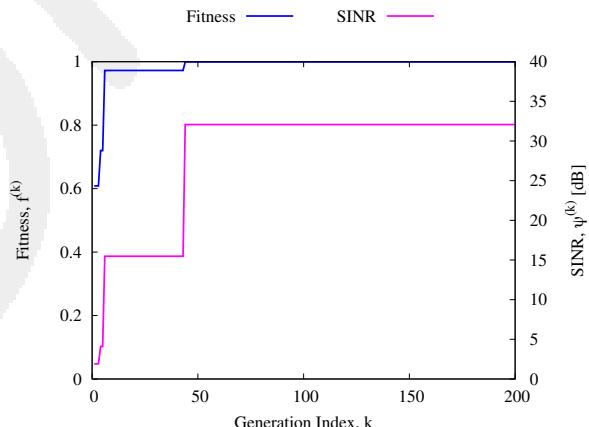
**Fig.22 - Thinning Configuration**



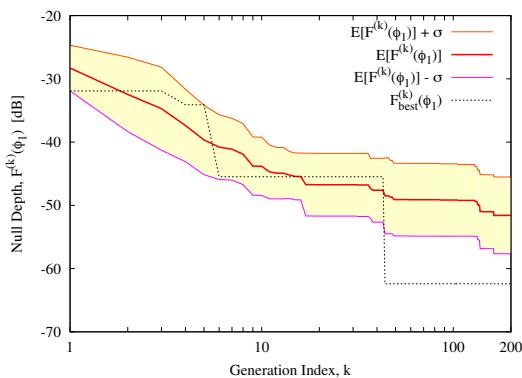
**Fig.23 - Pattern**



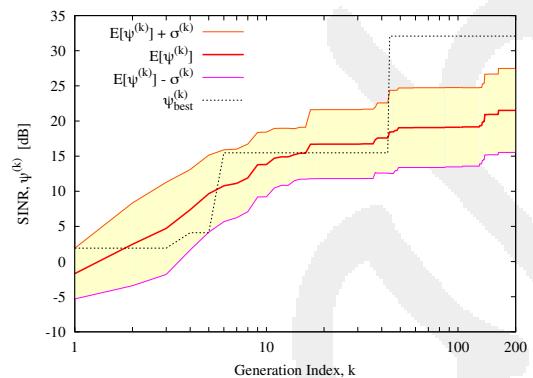
**Fig.24 - Nulls Depth**



**Fig.25 - Fitness - SINR**



**Fig.26 - Null Depth  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ$  Statistics**



**Fig.27 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	Nr. Active Elements	SINR [dB]
GA	-62.41	22	32.08

**Tab.7 - GA Simulation Results Analysis**

## TEST CASE 7 - 32 Elements - Fixed Scenario, Single Interference - $\eta \in [0.60 - 0.60]$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a single interference.

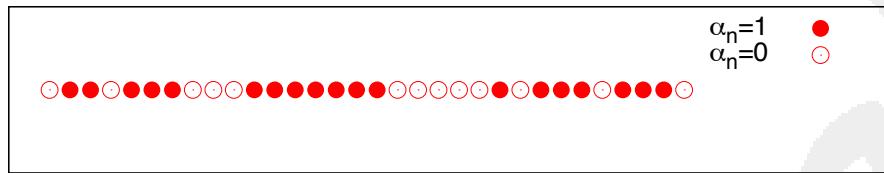
### Test Case Description

- Number of Elements  $N = 32$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 1$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ$

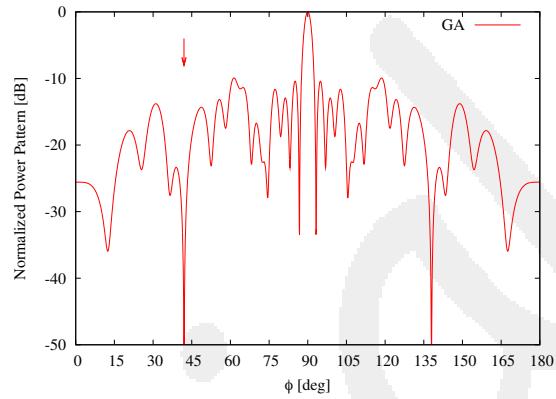
### Optimization Approach: GA

- Number of Variables:  $X = 32 (\alpha_n, n = 1, \dots, N)$
- Population: 16
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.60$
- Maximum Thinning Coefficient:  $\eta_{max} = 0.60$
- Number of Repetitions for Statistical Analysis: 20

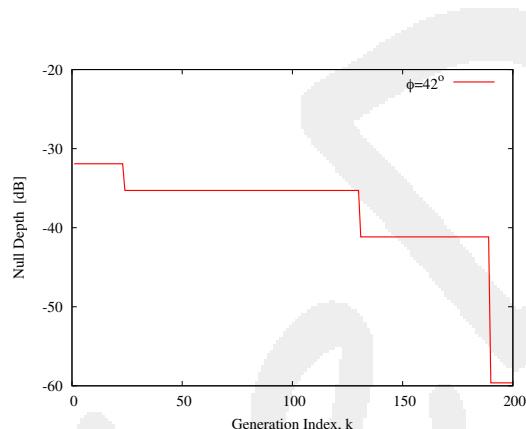
**GA - 32 Elements - Single Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$



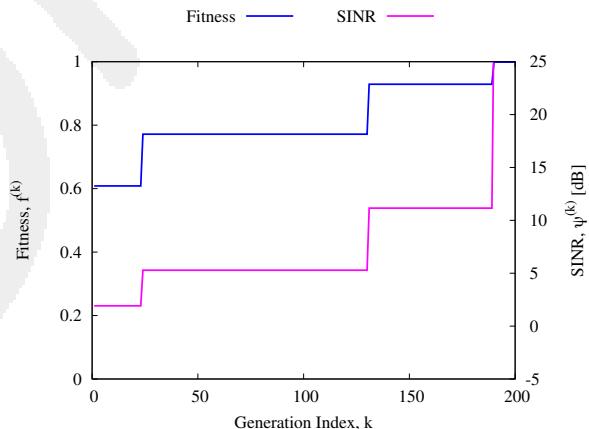
**Fig.28 - Thinning Configuration**



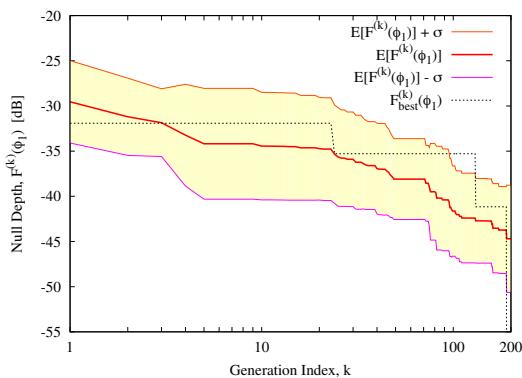
**Fig.29 - Pattern**



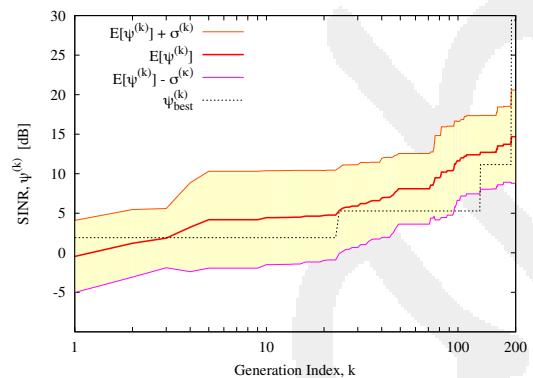
**Fig.30 - Nulls Depth**



**Fig.31 - Fitness - SINR**



**Fig.32 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics**



**Fig.33 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	Nr. Active Elements	SINR [dB]
GA	-53.18	19	23.14

**Tab.8 - GA Simulation Results Analysis**

## TEST CASE 8 - 32 Elements - Fixed Scenario, Double Interference - $\eta \in [0.00 - 1.00]$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a double interference.

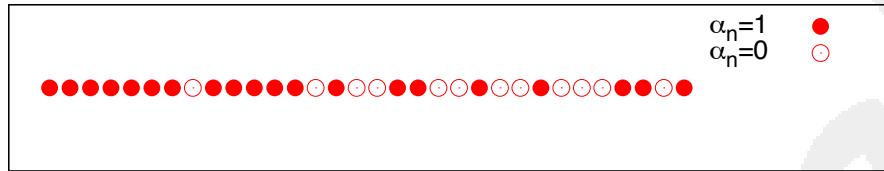
### Test Case Description

- Number of Elements  $N = 32$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 2$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ, \theta_2^i = 90^\circ, \phi_2^i = 113^\circ$

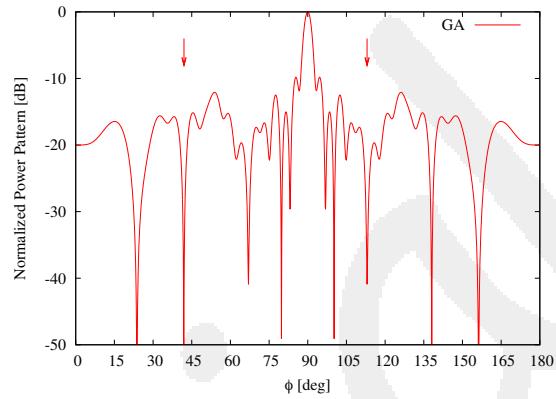
### Optimization Approach: GA

- Number of Variables:  $X = 32 (\alpha_n, n = 1, \dots, N)$
- Population: 16
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.00$
- Maximum Thinning Coefficient:  $\eta_{max} = 1.00$
- Number of Repetitions for Statistical Analysis: 20

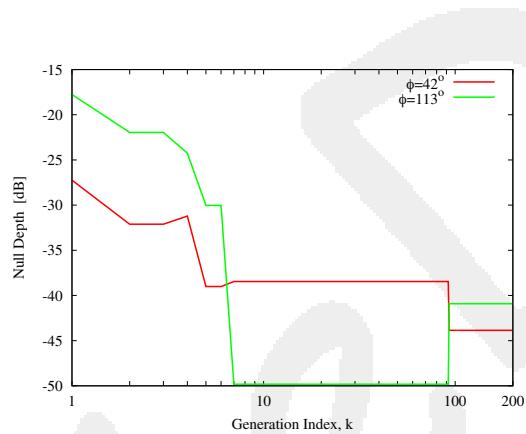
**GA - 32 Elements - Double Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$ ,  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$



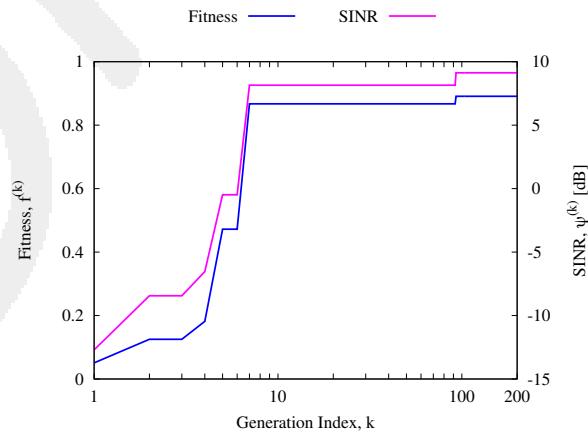
**Fig.34 - Thinning Configuration**



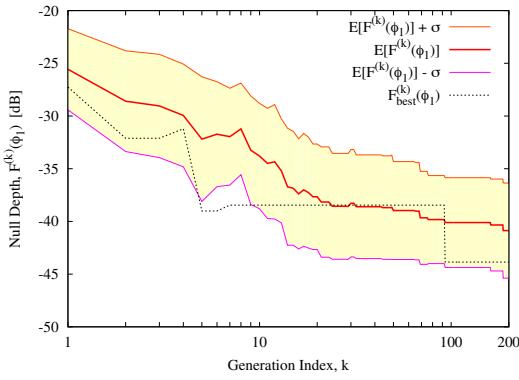
**Fig.35 - Pattern**



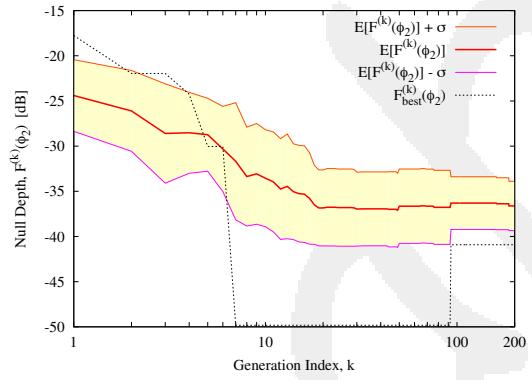
**Fig.36 - Nulls Depth**



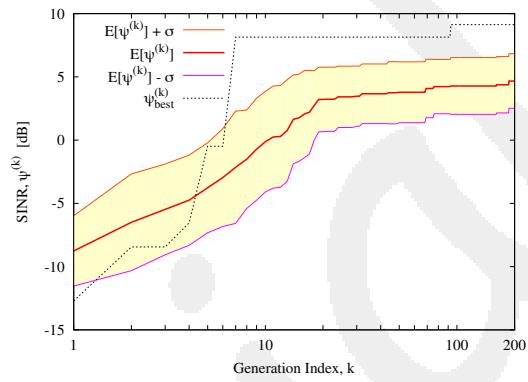
**Fig.37 - Fitness - SINR**



**Fig.38 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics**



**Fig.39 - Null Depth  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$  Statistics**



**Fig.40 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	$AF(\theta_2^i, \phi_2^i)$	Nr. Active Elements	$SINR [dB]$
GA	-43.85	-40.92	20	9.13

**Tab.9 - GA Simulation Results Analysis**

## TEST CASE 9 - 32 Elements - Fixed Scenario, Double Interference - $\eta \in [0.50 - 0.70]$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a double interference.

### Test Case Description

- Number of Elements  $N = 32$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 2$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ, \theta_2^i = 90^\circ, \phi_2^i = 113^\circ$

### Optimization Approach: GA

- Number of Variables:  $X = 32 (\alpha_n, n = 1, \dots, N)$
- Population: 16
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.50$
- Maximum Thinning Coefficient:  $\eta_{max} = 0.70$
- Number of Repetitions for Statistical Analysis: 20

**GA - 32 Elements - Double Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$ ,  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$

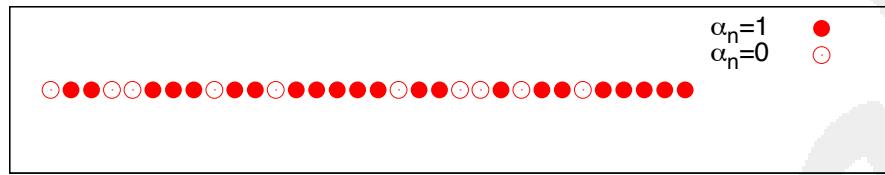


Fig.41 - Thinning Configuration

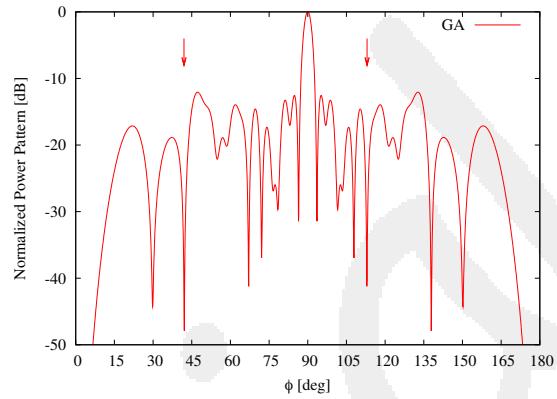


Fig.42 - Pattern

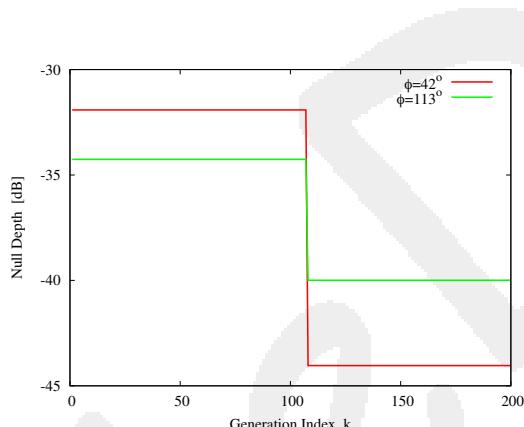


Fig.43 - Nulls Depth

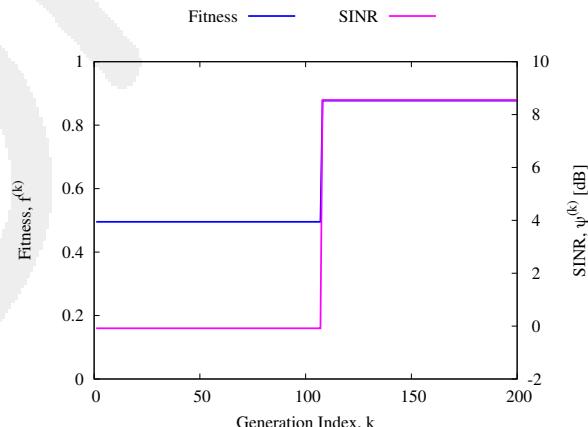
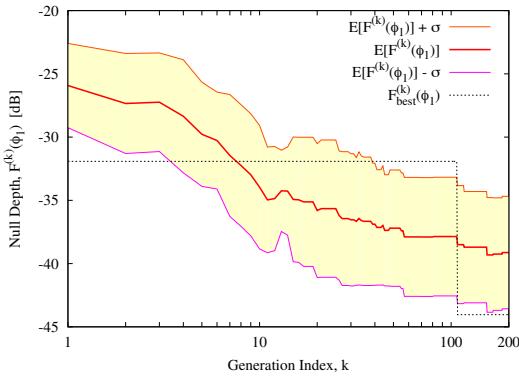
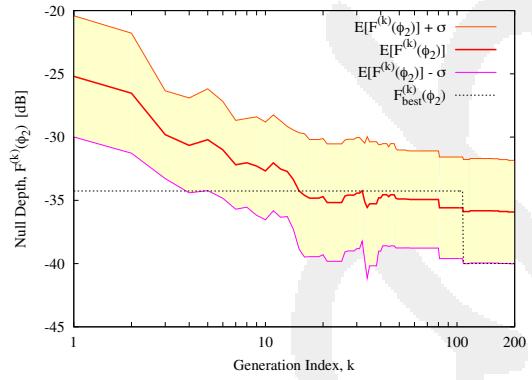


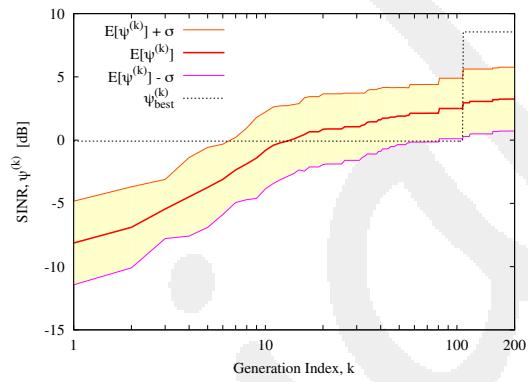
Fig.44 - Fitness - SINR



**Fig.45 - Null Depth  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ$  Statistics**



**Fig.46 - Null Depth  $\theta_2^i = 90^\circ, \phi_2^i = 113^\circ$  Statistics**



**Fig.47 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	$AF(\theta_2^i, \phi_2^i)$	Nr. Active Elements	$SINR [dB]$
GA	-44.04	-39.99	22	8.55

**Tab.10 - GA Simulation Results Analysis**

## TEST CASE 10 - 32 Elements - Fixed Scenario, Double Interference -

$$\eta \in [0.60 - 0.60]$$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a double interference.

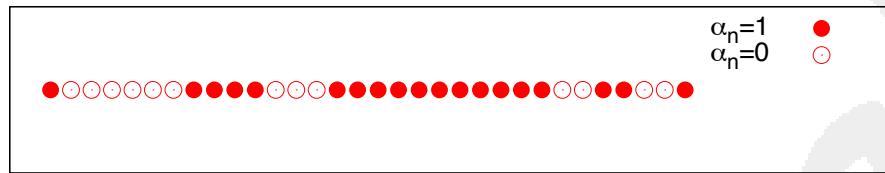
### Test Case Description

- Number of Elements  $N = 32$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 2$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ, \theta_2^i = 90^\circ, \phi_2^i = 113^\circ$

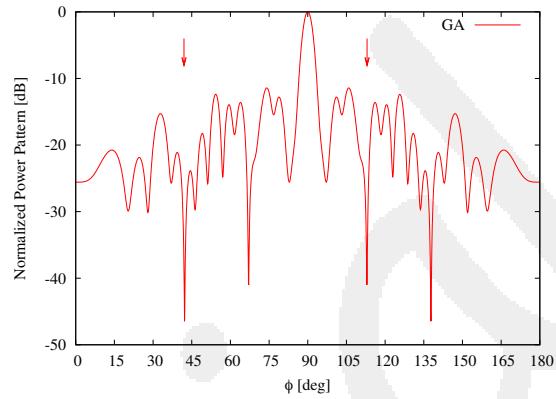
### Optimization Approach: GA

- Number of Variables:  $X = 32 (\alpha_n, n = 1, \dots, N)$
- Population: 16
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.60$
- Maximum Thinning Coefficient:  $\eta_{max} = 0.60$
- Number of Repetitions for Statistical Analysis: 20

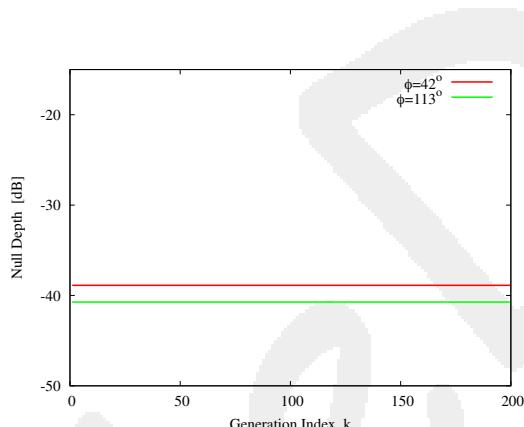
**GA - 32 Elements - Double Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$ ,  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$



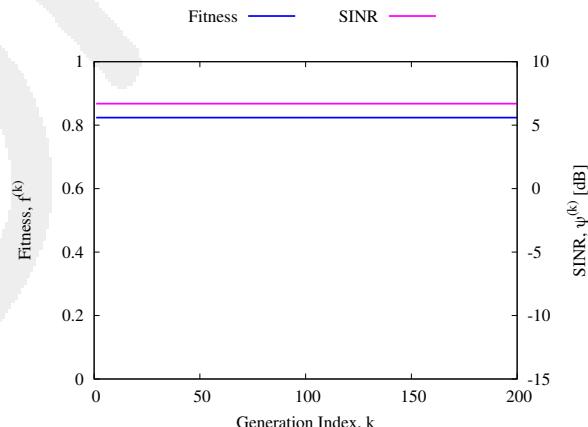
**Fig.48 - Thinning Configuration**



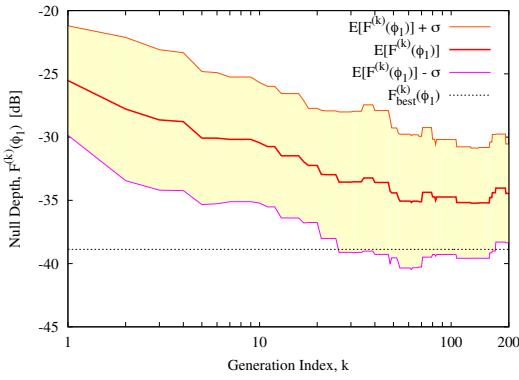
**Fig.49 - Pattern**



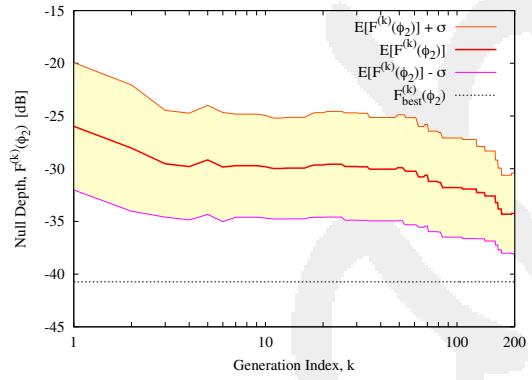
**Fig.50 - Nulls Depth**



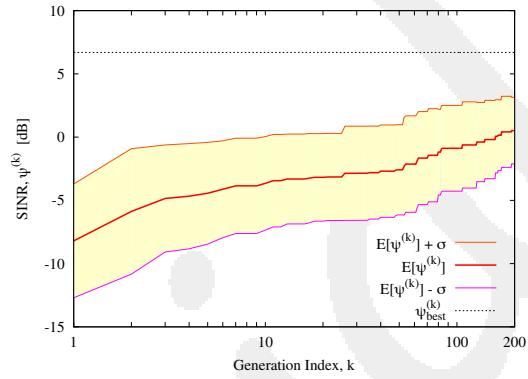
**Fig.51 - Fitness - SINR**



**Fig.52 - Null Depth  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ$  Statistics**



**Fig.53 - Null Depth  $\theta_2^i = 90^\circ, \phi_2^i = 113^\circ$  Statistics**



**Fig.54 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	$AF(\theta_2^i, \phi_2^i)$	Nr. Active Elements	$SINR [dB]$
GA	-38.87	-40.73	19	6.69

**Tab.11 - GA Simulation Results Analysis**

# TEST CASE 11 - 32 Elements - Fixed Scenario, Triple Interference - $\eta \in [0.00 - 1.00]$

## Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a triple interference.

## Test Case Description

- Number of Elements  $N = 32$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 3$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ, \theta_2^i = 90^\circ, \phi_2^i = 113^\circ, \theta_3^i = 90^\circ, \phi_3^i = 164^\circ$

## Optimization Approach: GA

- Number of Variables:  $X = 32 (\alpha_n, n = 1, \dots, N)$
- Population: 16
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.00$
- Maximum Thinning Coefficient:  $\eta_{max} = 1.00$
- Number of Repetitions for Statistical Analysis: 20

**GA - 32 Elements - Triple Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$ ,  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$ ,  $\theta_3^i = 90^\circ$ ,  $\phi_3^i = 164^\circ$

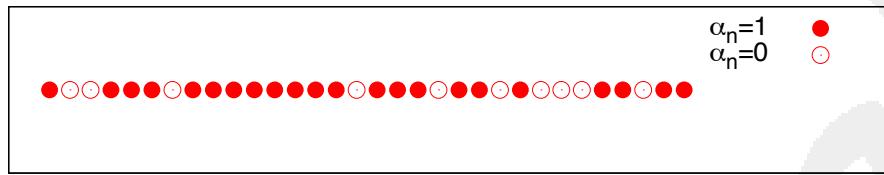


Fig.55 - Thinning Configuration

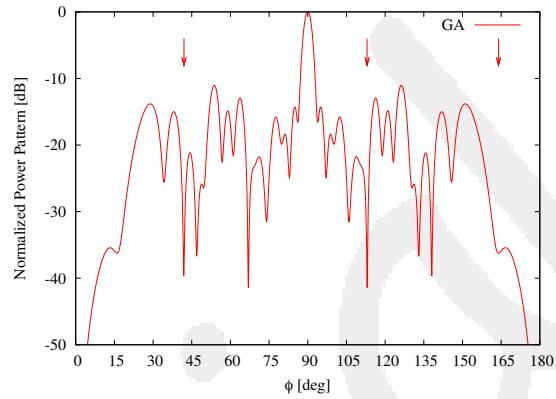


Fig.56 - Pattern

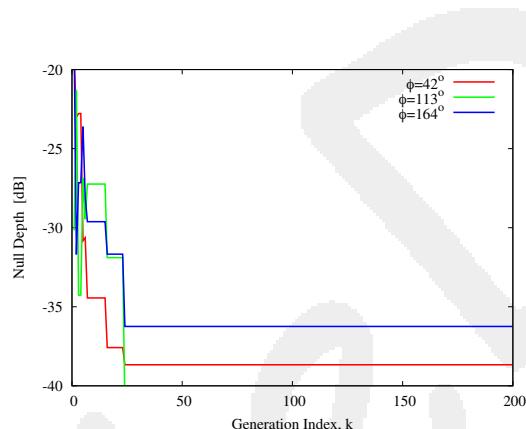


Fig.57 - Nulls Depth

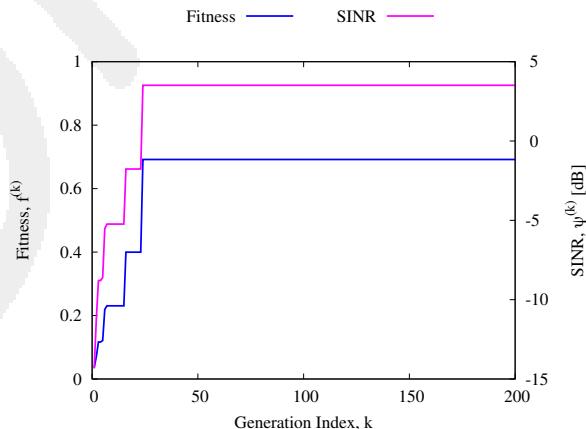


Fig.58 - Fitness - SINR

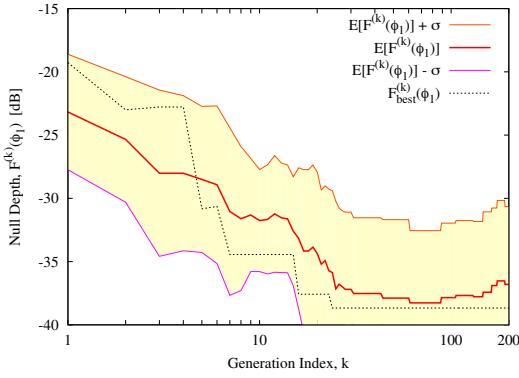


Fig.59 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics

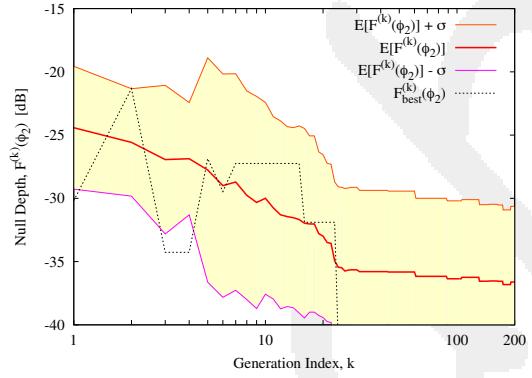


Fig.60 - Null Depth  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$  Statistics

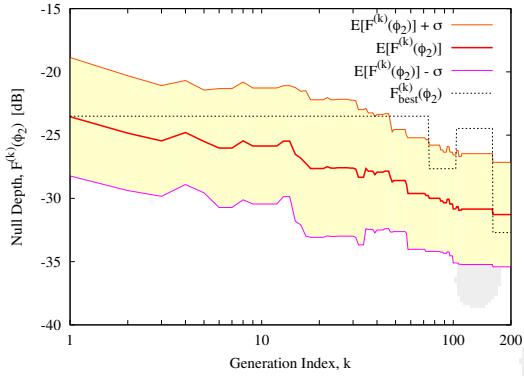


Fig.61 - Null Depth  $\theta_3^i = 90^\circ$ ,  $\phi_3^i = 164^\circ$  Statistics

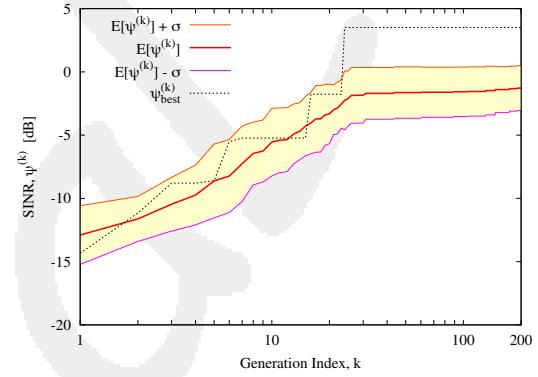


Fig.62 - SINR Statistics

	$AF(\theta_1^i, \phi_1^i)$	$AF(\theta_2^i, \phi_2^i)$	$AF(\theta_3^i, \phi_3^i)$	Nr. Active Elements	$SINR [dB]$
GA	-38.67	-41.41	-36.25	22	3.51

Tab.12 - GA Simulation Results Analysis

## TEST CASE 12 - 32 Elements - Fixed Scenario, Triple Interference - $\eta \in [0.50 - 0.70]$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a triple interference.

### Test Case Description

- Number of Elements  $N = 32$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 3$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ, \theta_2^i = 90^\circ, \phi_2^i = 113^\circ, \theta_3^i = 90^\circ, \phi_3^i = 164^\circ$

### Optimization Approach: GA

- Number of Variables:  $X = 32 (\alpha_n, n = 1, \dots, N)$
- Population: 16
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.50$
- Maximum Thinning Coefficient:  $\eta_{max} = 0.70$
- Number of Repetitions for Statistical Analysis: 20

**GA - 32 Elements - Triple Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$ ,  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$ ,  $\theta_3^i = 90^\circ$ ,  $\phi_3^i = 164^\circ$

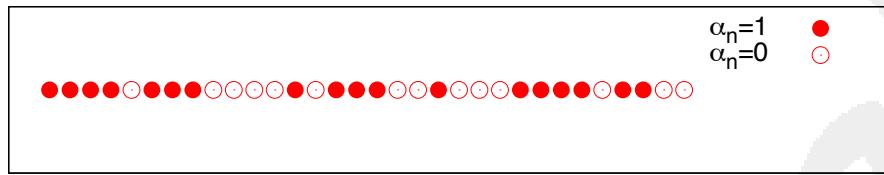


Fig.63 - Thinning Configuration

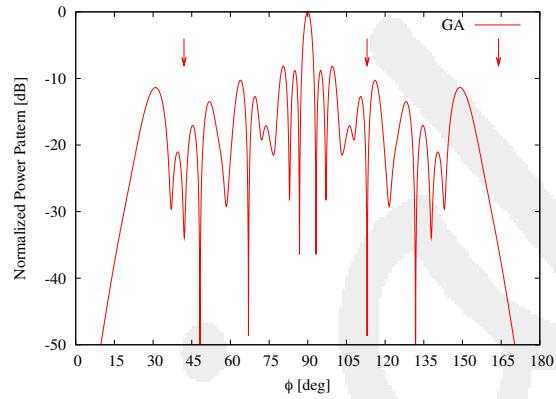


Fig.64 - Pattern

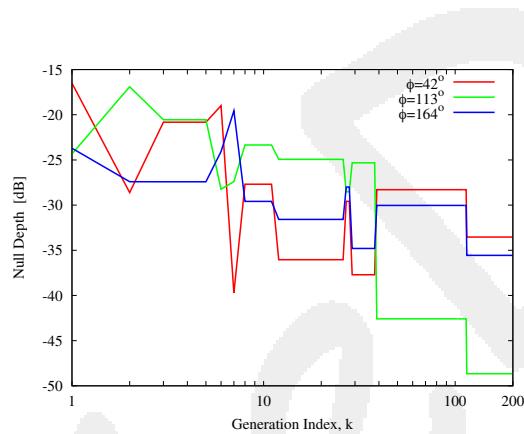


Fig.65 - Nulls Depth

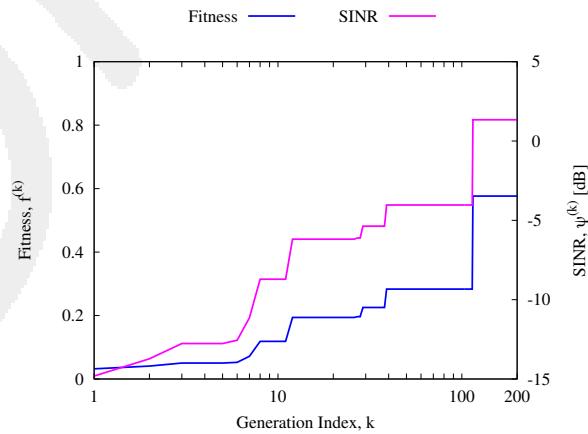


Fig.66 - Fitness - SINR

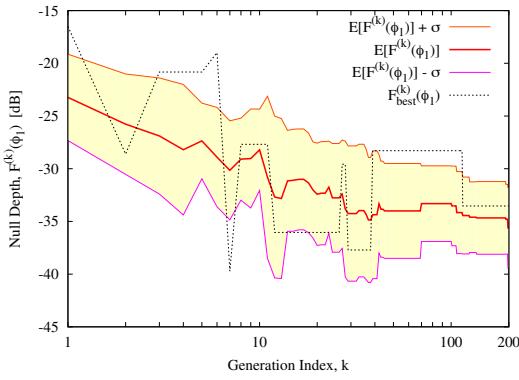


Fig.67 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics

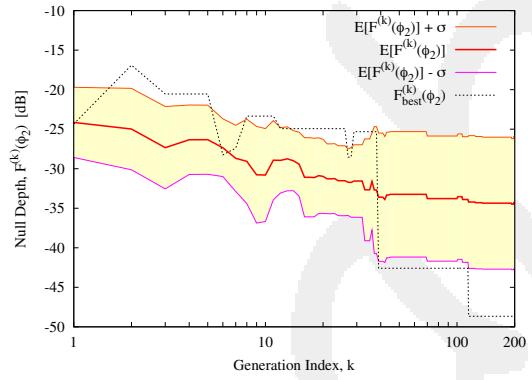


Fig.68 - Null Depth  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$  Statistics

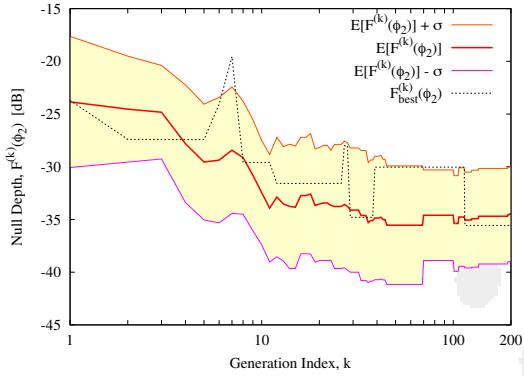


Fig.69 - Null Depth  $\theta_3^i = 90^\circ$ ,  $\phi_3^i = 164^\circ$  Statistics

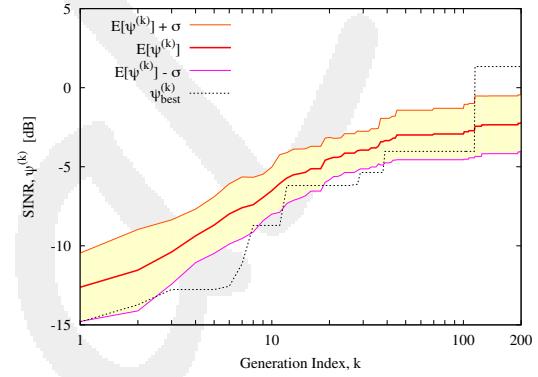


Fig.70 - SINR Statistics

	$AF(\theta_1^i, \phi_1^i)$	$AF(\theta_2^i, \phi_2^i)$	$AF(\theta_3^i, \phi_3^i)$	Nr. Active Elements	SINR [dB]
GA	-33.53	-48.66	-35.56	18	1.34

Tab.13 - GA Simulation Results Analysis

## TEST CASE 13 - 32 Elements - Fixed Scenario, Triple Interference - $\eta \in [0.60 - 0.60]$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a triple interference.

### Test Case Description

- Number of Elements  $N = 32$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 3$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ, \theta_2^i = 90^\circ, \phi_2^i = 113^\circ, \theta_3^i = 90^\circ, \phi_3^i = 164^\circ$

### Optimization Approach: GA

- Number of Variables:  $X = 32 (\alpha_n, n = 1, \dots, N)$
- Population: 16
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.60$
- Maximum Thinning Coefficient:  $\eta_{max} = 0.60$
- Number of Repetitions for Statistical Analysis: 20

**GA - 32 Elements - Triple Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$ ,  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$ ,  $\theta_3^i = 90^\circ$ ,  $\phi_3^i = 164^\circ$

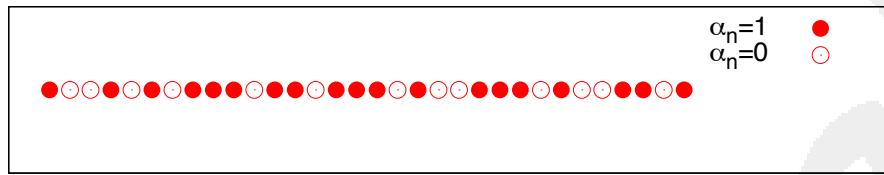


Fig.71 - Thinning Configuration

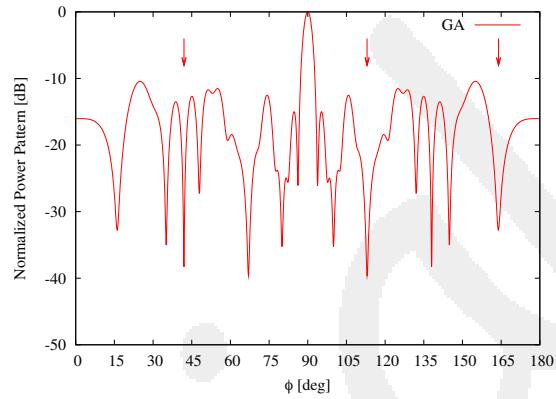


Fig.72 - Pattern

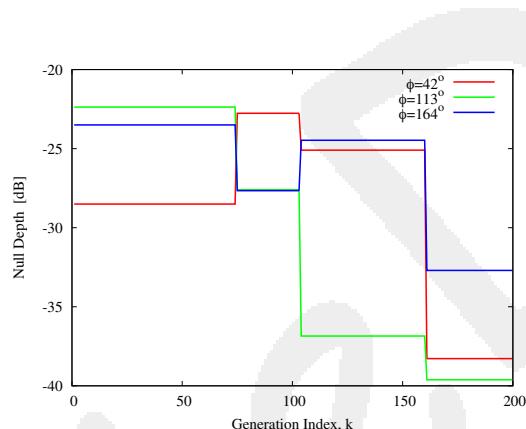


Fig.73 - Nulls Depth

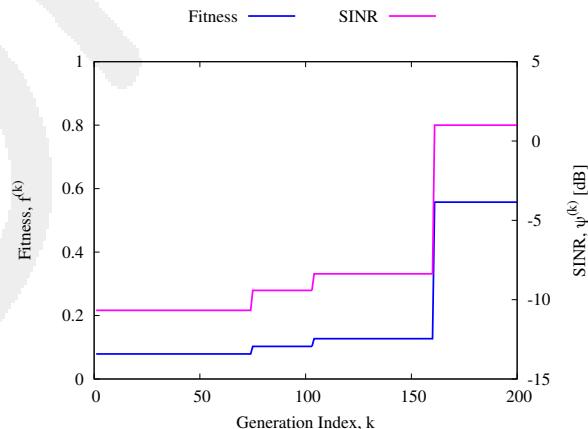


Fig.74 - Fitness - SINR

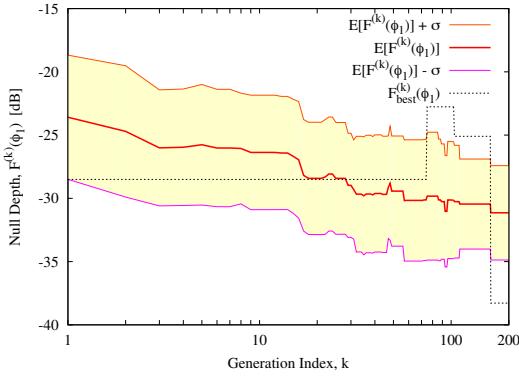


Fig.75 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics

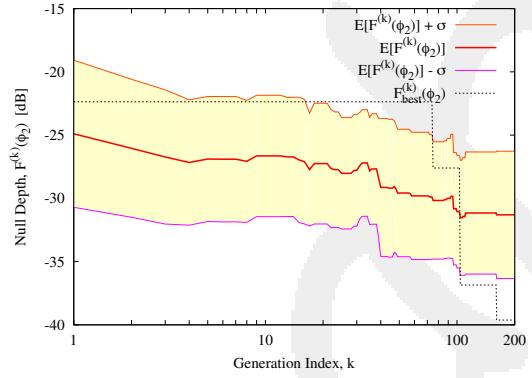


Fig.76 - Null Depth  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$  Statistics

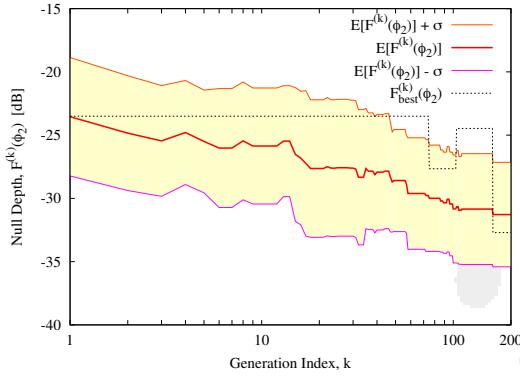


Fig.77 - Null Depth  $\theta_3^i = 90^\circ$ ,  $\phi_3^i = 164^\circ$  Statistics

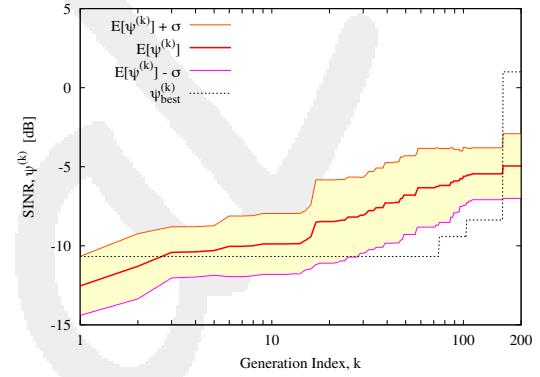


Fig.78 - SINR Statistics

	$AF(\theta_1^i, \phi_1^i)$	$AF(\theta_2^i, \phi_2^i)$	$AF(\theta_3^i, \phi_3^i)$	Nr. Active Elements	SINR [dB]
GA	-38.28	-39.62	-32.70	19	1.00

Tab.14 - GA Simulation Results Analysis

## TEST CASE 14 - 64 Elements - Fixed Scenario, Single Interference - $\eta \in [0.00 - 1.00]$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a single interference.

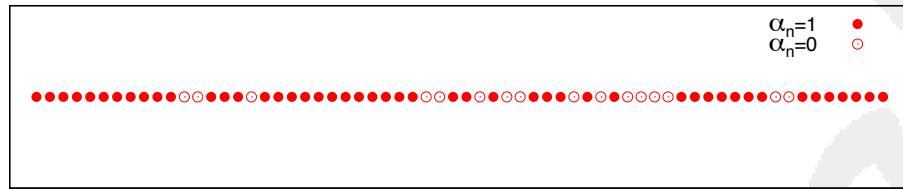
### Test Case Description

- Number of Elements  $N = 64$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 1$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ$

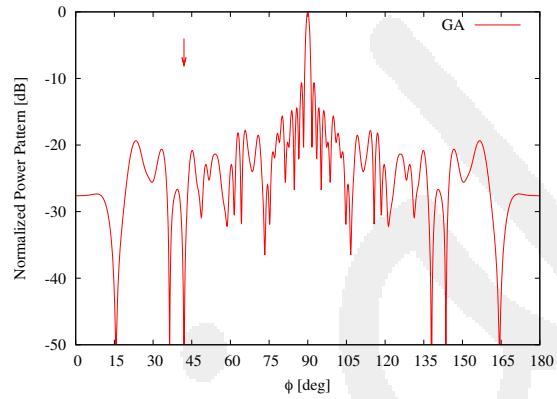
### Optimization Approach: GA

- Number of Variables:  $X = 64 (\alpha_n, n = 1, \dots, N)$
- Population: 32
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.00$
- Maximum Thinning Coefficient:  $\eta_{max} = 1.00$
- Number of Repetitions for Statistical Analysis: 20

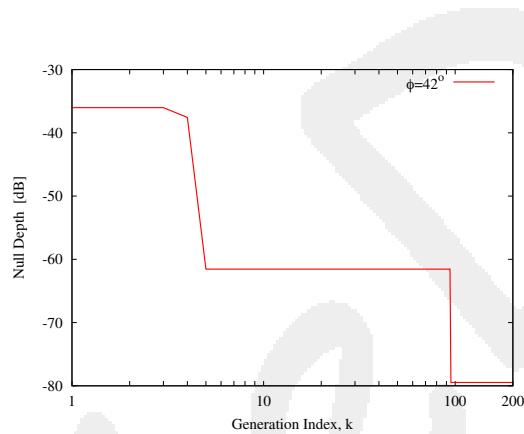
**GA - 64 Elements - Single Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$



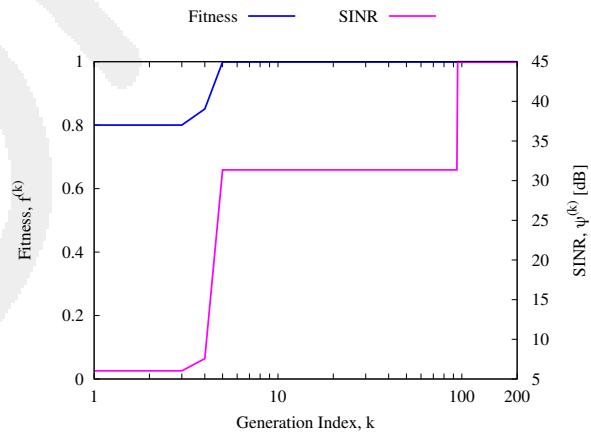
**Fig.79 - Thinning Configuration**



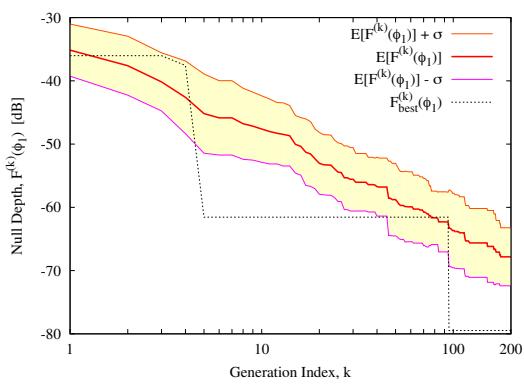
**Fig.80 - Pattern**



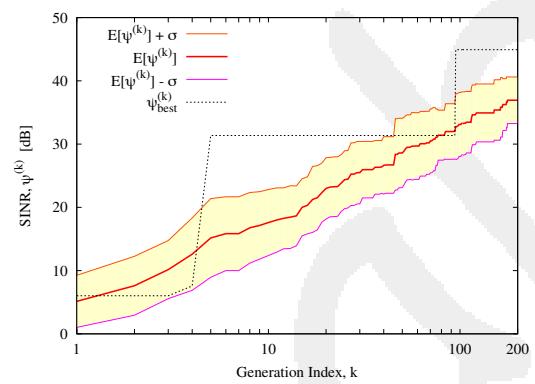
**Fig.81 - Nulls Depth**



**Fig.82 - Fitness - SINR**



**Fig.83 - Null Depth  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ$  Statistics**



**Fig.84 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	Nr. Active Elements	SINR [dB]
GA	-79.47	48	44.93

**Tab.15 - GA Simulation Results Analysis**

# TEST CASE 15 - 64 Elements - Fixed Scenario, Single Interference -

$$\eta \in [0.50 - 0.70]$$

## Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a single interference.

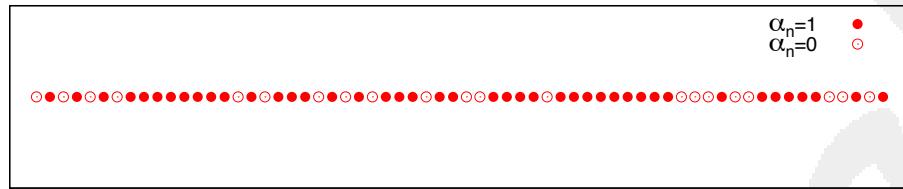
## Test Case Description

- Number of Elements  $N = 64$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 1$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ$

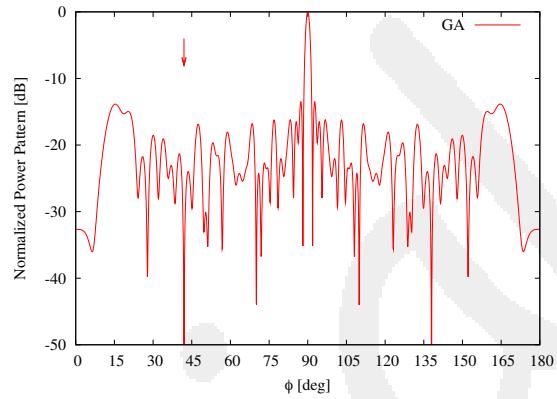
## Optimization Approach: GA

- Number of Variables:  $X = 64 (\alpha_n, n = 1, \dots, N)$
- Population: 32
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.50$
- Maximum Thinning Coefficient:  $\eta_{max} = 0.70$
- Number of Repetitions for Statistical Analysis: 20

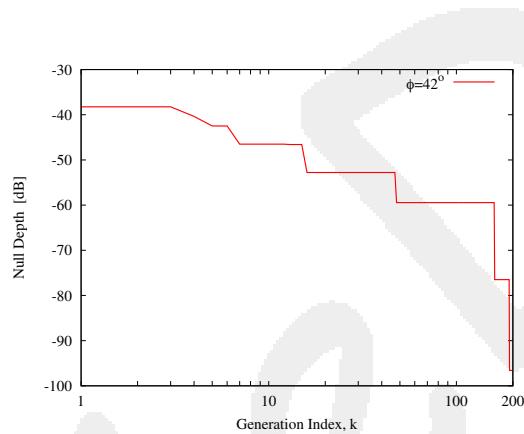
**GA - 64 Elements - Single Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$



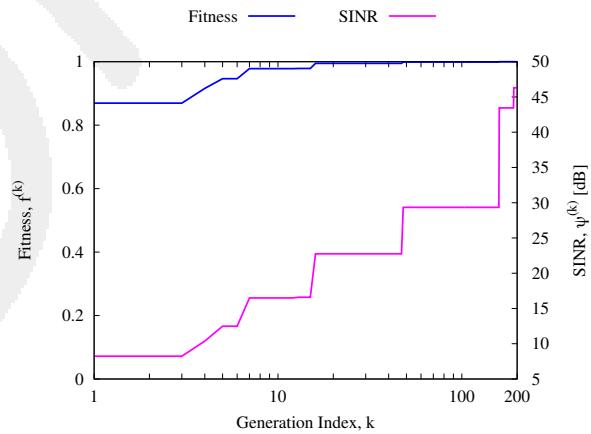
**Fig.85 - Thinning Configuration**



**Fig.86 - Pattern**



**Fig.87 - Nulls Depth**



**Fig.88 - Fitness - SINR**

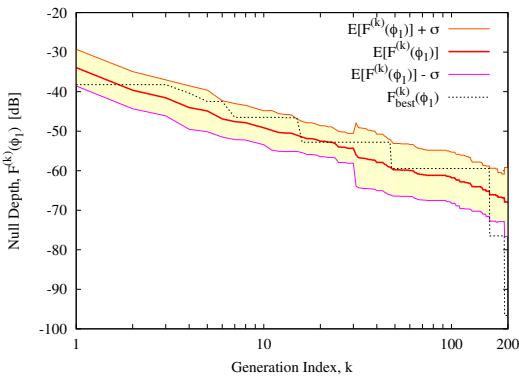


Fig.89 - NullsDepth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics

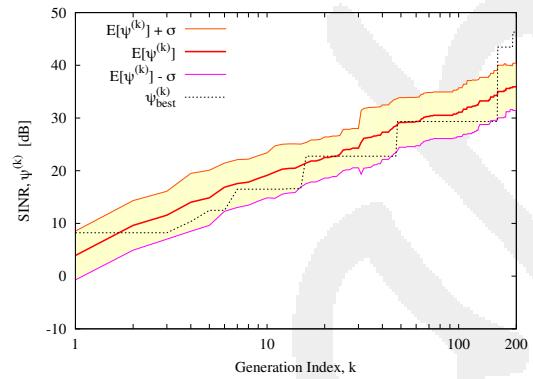


Fig.90 - SINR Statistics

	$AF(\theta_1^i, \phi_1^i)$	Nr. Active Elements	SINR [dB]
GA	-96.59	43	46.29

Tab.16 - GA Simulation Results Analysis

## TEST CASE 16 - 64 Elements - Fixed Scenario, Single Interference - $\eta \in [0.60 - 0.60]$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a single interference.

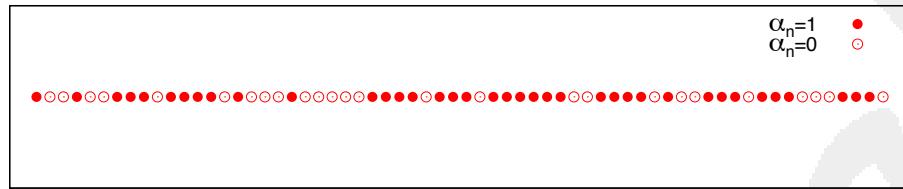
### Test Case Description

- Number of Elements  $N = 64$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 1$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ$

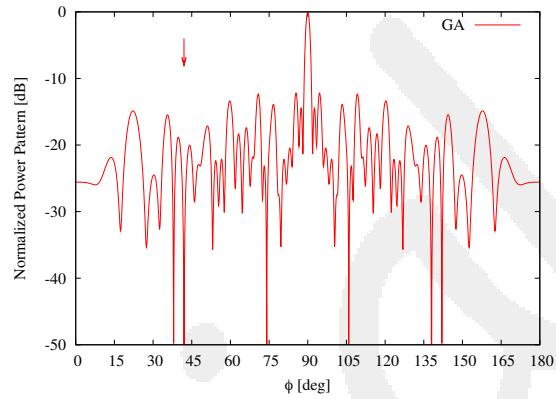
### Optimization Approach: GA

- Number of Variables:  $X = 64 (\alpha_n, n = 1, \dots, N)$
- Population: 32
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.60$
- Maximum Thinning Coefficient:  $\eta_{max} = 0.60$
- Number of Repetitions for Statistical Analysis: 20

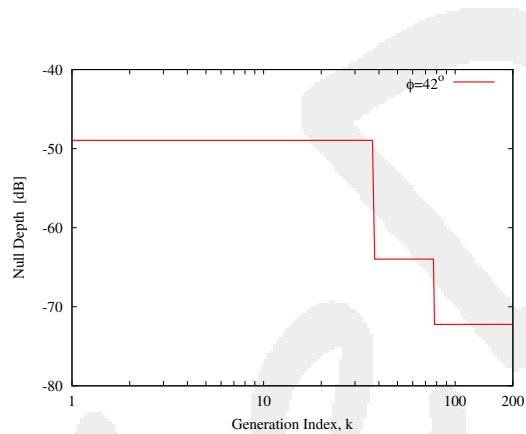
**GA - 64 Elements - Single Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$



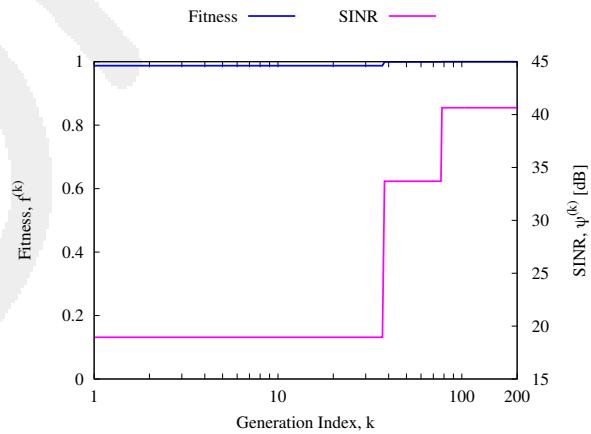
**Fig.91 - Thinning Configuration**



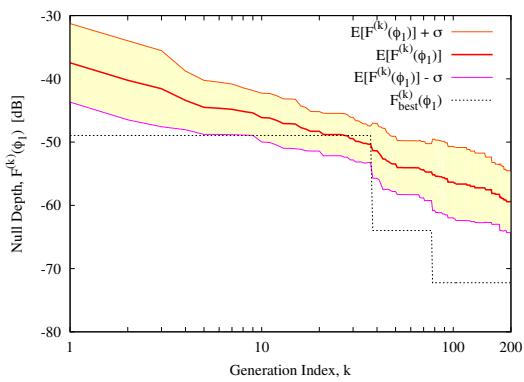
**Fig.92 - Pattern**



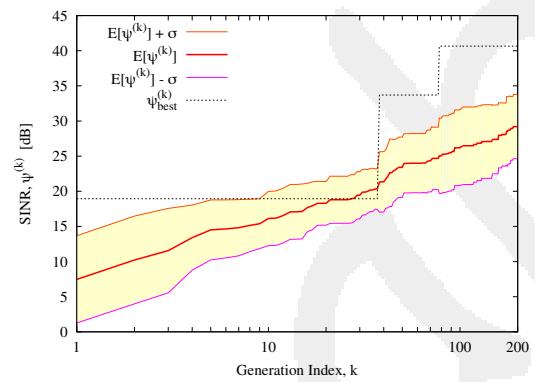
**Fig.93 - Nulls Depth**



**Fig.94 - Fitness - SINR**



**Fig.95 - Null Depth  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ$  Statistics**



**Fig.96 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	Nr. Active Elements	SINR [dB]
GA	-72.23	38	40.65

**Tab.17 - GA Simulation Results Analysis**

## TEST CASE 17 - 64 Elements - Fixed Scenario, Double Interference -

$$\eta \in [0.00 - 1.00]$$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a double interference.

### Test Case Description

- Number of Elements  $N = 64$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 2$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ, \theta_2^i = 90^\circ, \phi_2^i = 113^\circ$

### Optimization Approach: GA

- Number of Variables:  $X = 64 (\alpha_n, n = 1, \dots, N)$
- Population: 32
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.00$
- Maximum Thinning Coefficient:  $\eta_{max} = 1.00$
- Number of Repetitions for Statistical Analysis: 20

**GA - 64 Elements - Double Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$ ,  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$

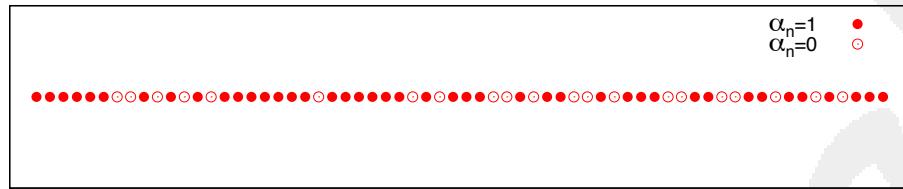


Fig.97 - Thinning Configuration

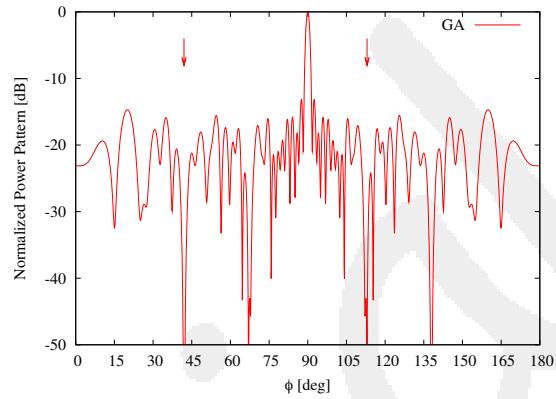


Fig.98 - Pattern

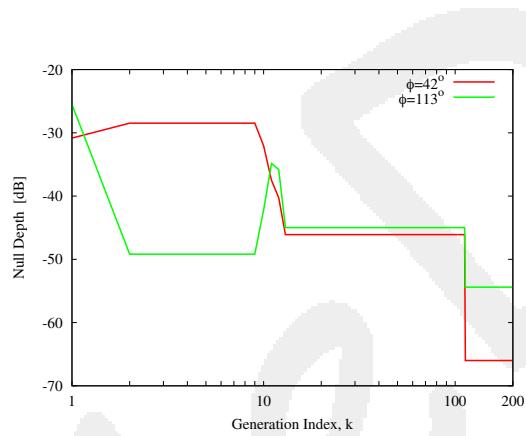


Fig.99 - Nulls Depth

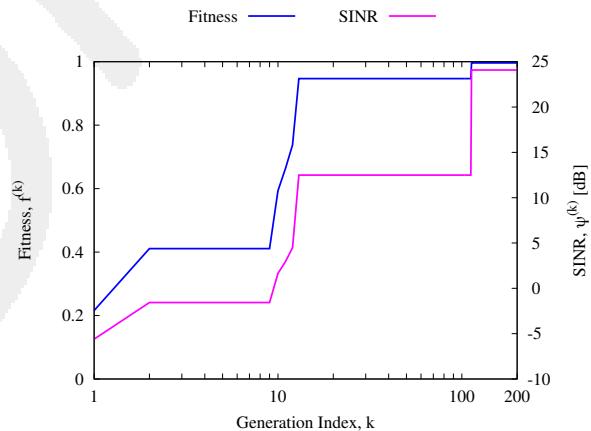
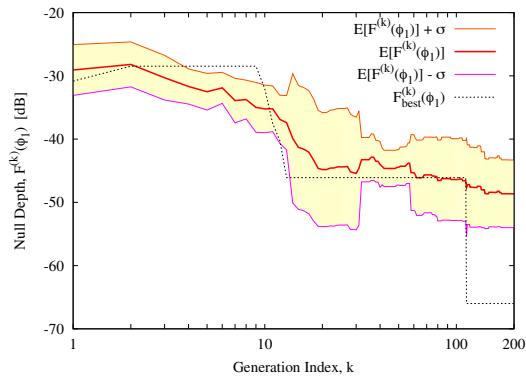
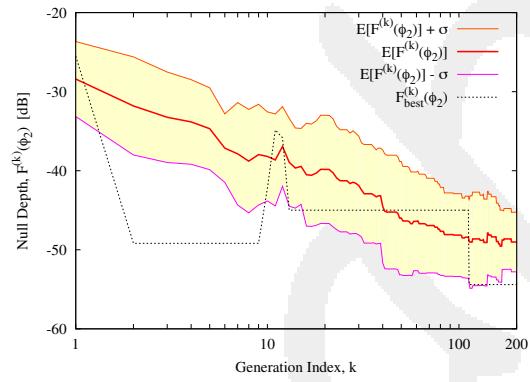


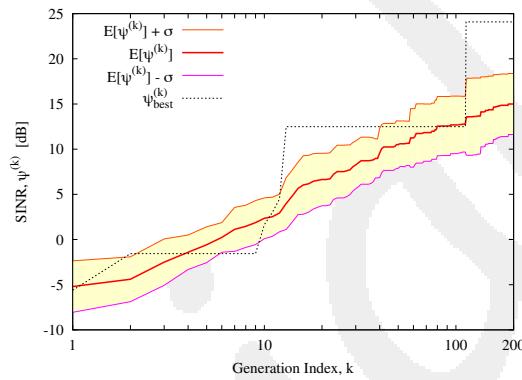
Fig.100 - Fitness - SINR



**Fig.101 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics**



**Fig.102 - Null Depth  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$  Statistics**



**Fig.103 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	$AF(\theta_2^i, \phi_2^i)$	Nr. Active Elements	$SINR [dB]$
GA	-65.99	-54.40	43	24.08

**Tab.18 - GA Simulation Results Analysis**

## TEST CASE 18 - 64 Elements - Fixed Scenario, Double Interference -

$$\eta \in [0.50 - 0.70]$$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a double interference.

### Test Case Description

- Number of Elements  $N = 64$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 2$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ, \theta_2^i = 90^\circ, \phi_2^i = 113^\circ$

### Optimization Approach: GA

- Number of Variables:  $X = 64 (\alpha_n, n = 1, \dots, N)$
- Population: 32
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.50$
- Maximum Thinning Coefficient:  $\eta_{max} = 0.70$
- Number of Repetitions for Statistical Analysis: 20

**GA - 64 Elements - Double Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$ ,  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$

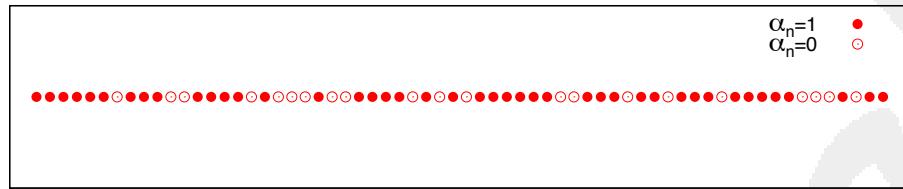


Fig.104 - Thinning Configuration

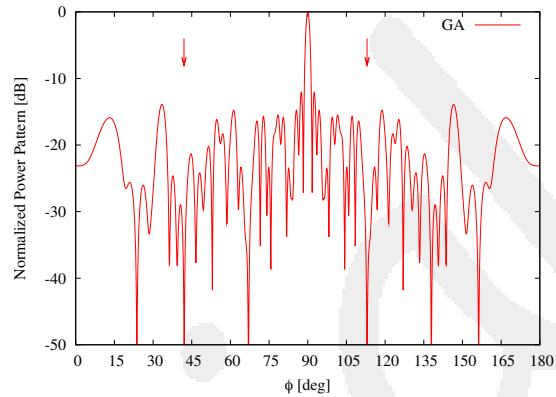


Fig.105 - Pattern

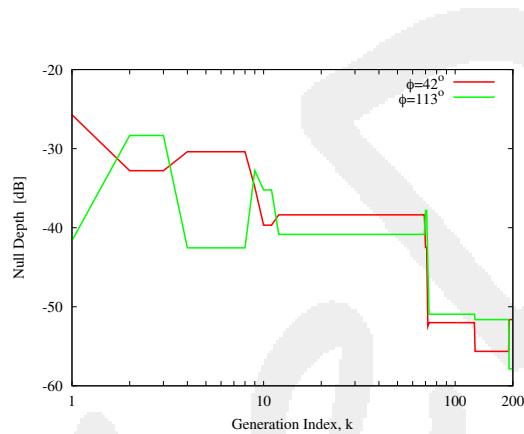


Fig.106 - Nulls Depth

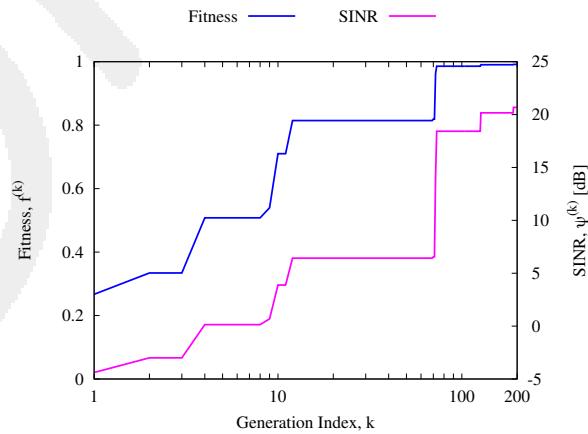
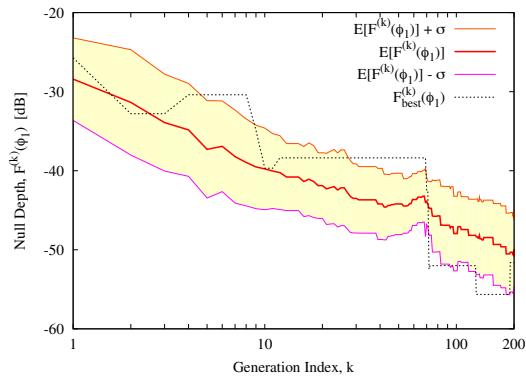
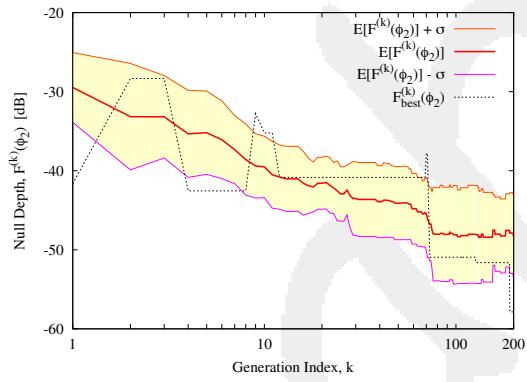


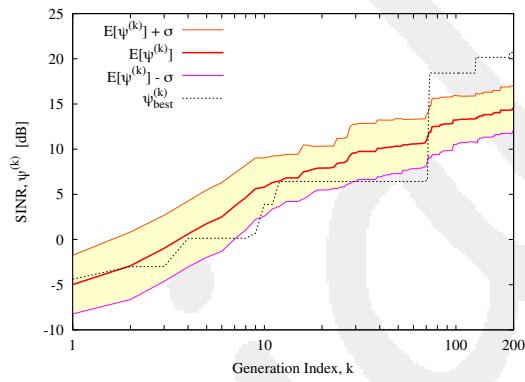
Fig.107 - Fitness - SINR



**Fig.108 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics**



**Fig.109 - Null Depth  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$  Statistics**



**Fig.110 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	$AF(\theta_2^i, \phi_2^i)$	Nr. Active Elements	$SINR [dB]$
GA	-51.62	-57.86	43	20.68

**Tab.19 - GA Simulation Results Analysis**

## TEST CASE 19 - 64 Elements - Fixed Scenario, Double Interference -

$$\eta \in [0.60 - 0.60]$$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a double interference.

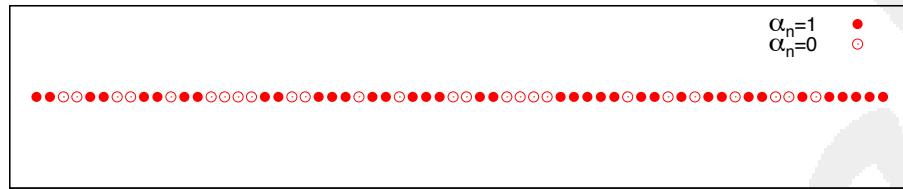
### Test Case Description

- Number of Elements  $N = 64$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 2$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ, \theta_2^i = 90^\circ, \phi_2^i = 113^\circ$

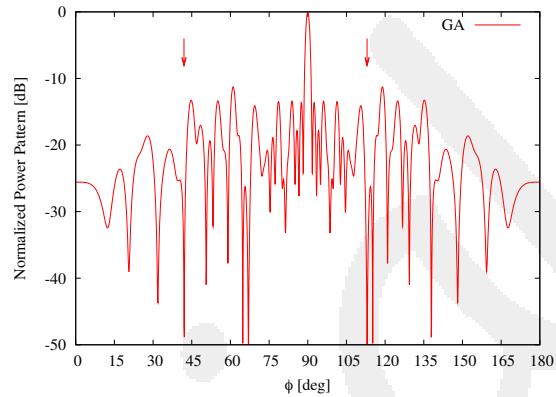
### Optimization Approach: GA

- Number of Variables:  $X = 64 (\alpha_n, n = 1, \dots, N)$
- Population: 32
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.60$
- Maximum Thinning Coefficient:  $\eta_{max} = 0.60$
- Number of Repetitions for Statistical Analysis: 20

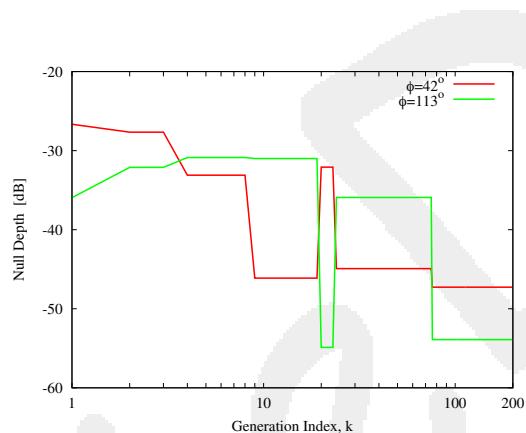
**GA - 64 Elements - Double Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$ ,  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$



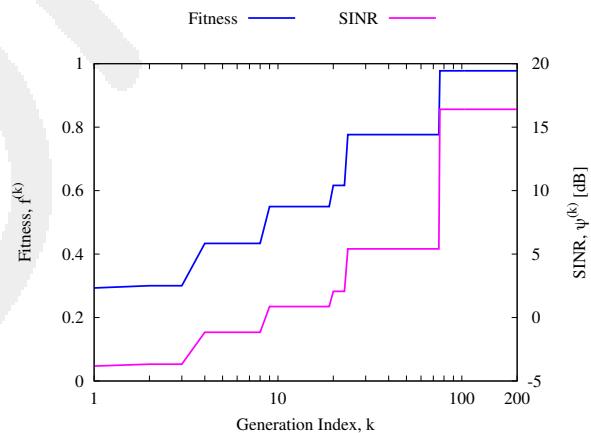
**Fig.111 - Thinning Configuration**



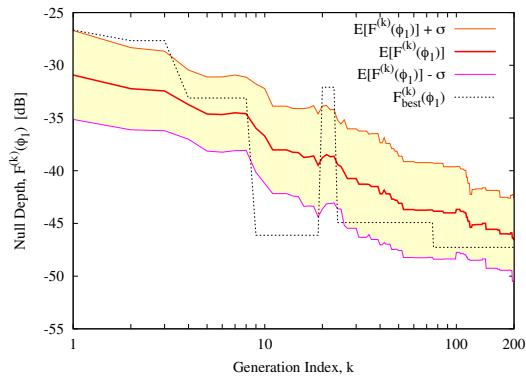
**Fig.112 - Pattern**



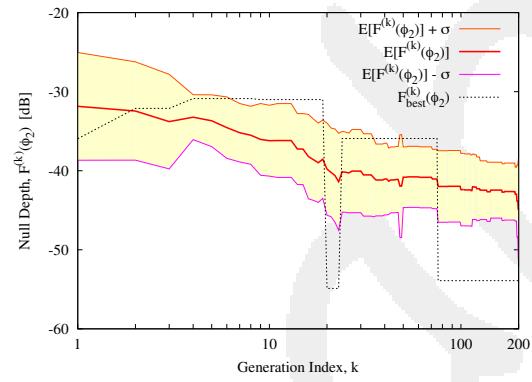
**Fig.113 - Nulls Depth**



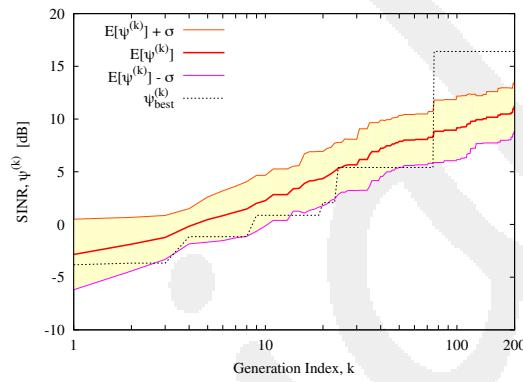
**Fig.114 - Fitness - SINR**



**Fig.115 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics**



**Fig.116 - Null Depth  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$  Statistics**



**Fig.117 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	$AF(\theta_2^i, \phi_2^i)$	Nr. Active Elements	$SINR [dB]$
GA	-47.27	-53.90	38	16.41

**Tab.20 - GA Simulation Results Analysis**

# TEST CASE 20 - 64 Elements - Fixed Scenario, Triple Interference - $\eta \in [0.00 - 1.00]$

## Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a double interference.

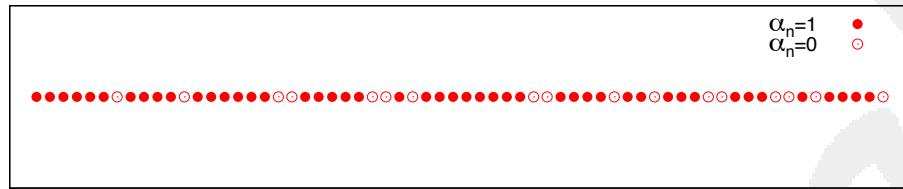
## Test Case Description

- Number of Elements  $N = 64$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 3$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ, \theta_2^i = 90^\circ, \phi_2^i = 113^\circ, \theta_3^i = 90^\circ, \phi_3^i = 164^\circ$

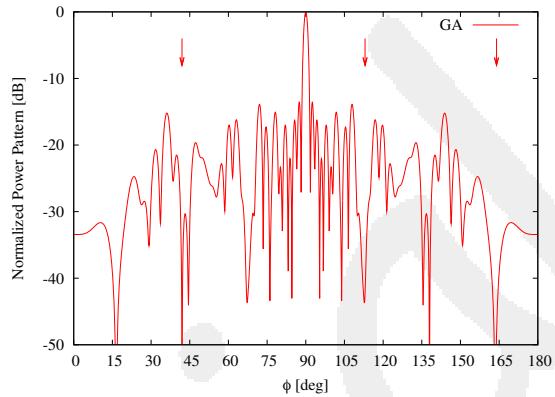
## Optimization Approach: GA

- Number of Variables:  $X = 64 (\alpha_n, n = 1, \dots, N)$
- Population: 32
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.00$
- Maximum Thinning Coefficient:  $\eta_{max} = 1.00$
- Number of Repetitions for Statistical Analysis: 20

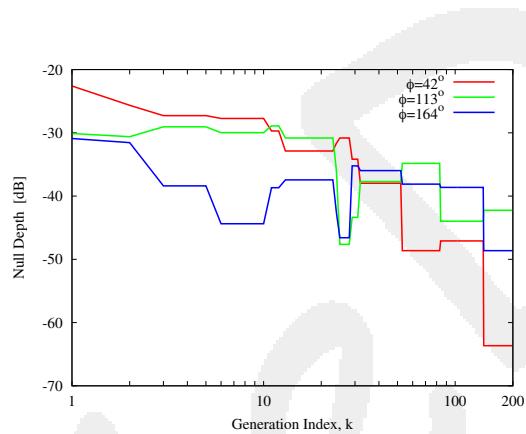
**GA - 64 Elements - Triple Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$ ,  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$ ,  $\theta_3^i = 90^\circ$ ,  $\phi_3^i = 164^\circ$



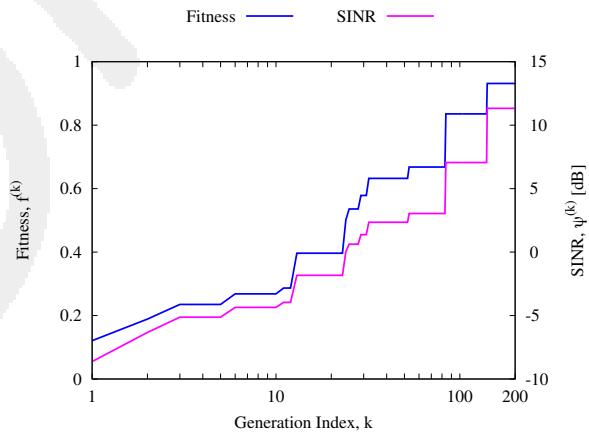
**Fig.118 - Thinning Configuration**



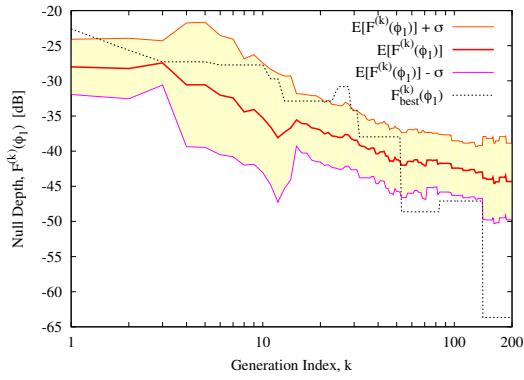
**Fig.119 - Pattern**



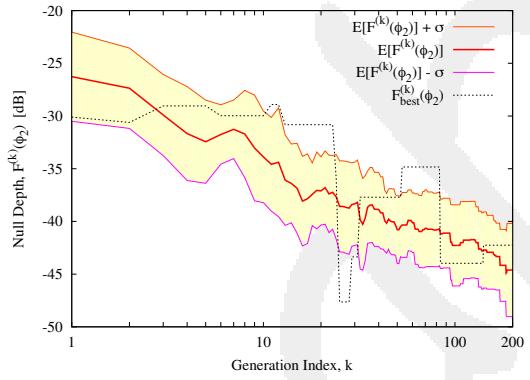
**Fig.120 - Nulls Depth**



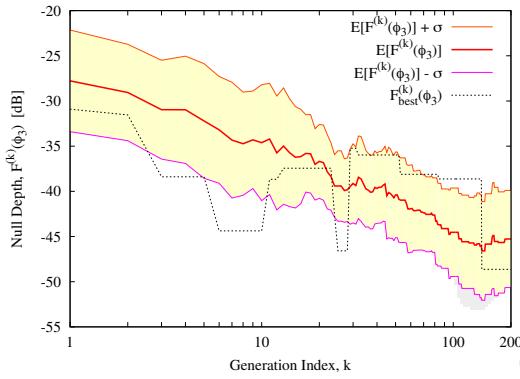
**Fig.121 - Fitness - SINR**



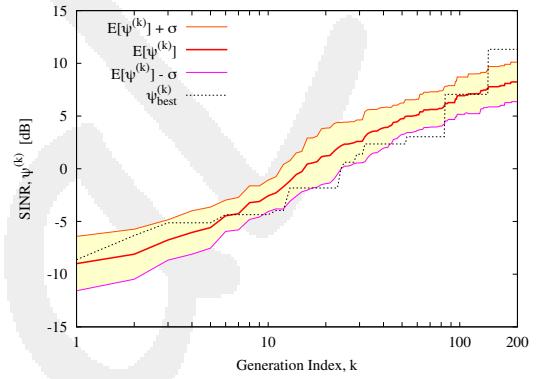
**Fig.122 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics**



**Fig.123 - Null Depth  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$  Statistics**



**Fig.124 - Null Depth  $\theta_3^i = 90^\circ$ ,  $\phi_3^i = 164^\circ$  Statistics**



**Fig.125 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	$AF(\theta_2^i, \phi_2^i)$	$AF(\theta_3^i, \phi_3^i)$	Nr. Active Elements	SINR [dB]
GA	-63.65	-42.25	-48.63	47	11.33

**Tab.21 - GA Simulation Results Analysis**

# TEST CASE 21 - 64 Elements - Fixed Scenario, Triple Interference - $\eta \in [0.50 - 0.70]$

## Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a double interference.

## Test Case Description

- Number of Elements  $N = 64$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 3$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ, \theta_2^i = 90^\circ, \phi_2^i = 113^\circ, \theta_3^i = 90^\circ, \phi_3^i = 164^\circ$

## Optimization Approach: GA

- Number of Variables:  $X = 64 (\alpha_n, n = 1, \dots, N)$
- Population: 32
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.50$
- Maximum Thinning Coefficient:  $\eta_{max} = 0.70$
- Number of Repetitions for Statistical Analysis: 20

**GA - 64 Elements - Triple Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$ ,  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$ ,  $\theta_3^i = 90^\circ$ ,  $\phi_3^i = 164^\circ$

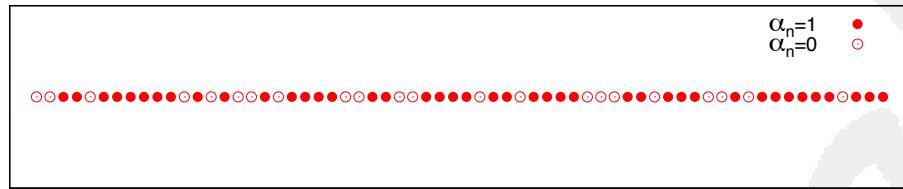


Fig.126 - Thinning Configuration

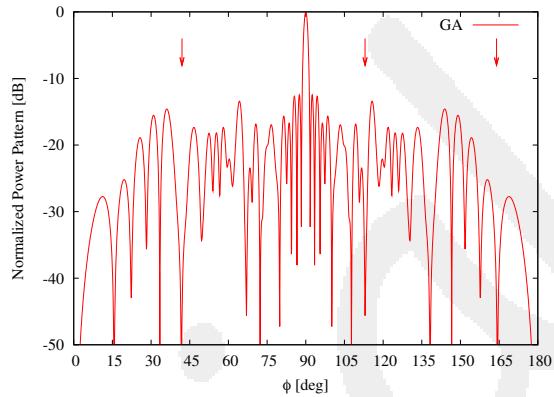


Fig.127 - Pattern

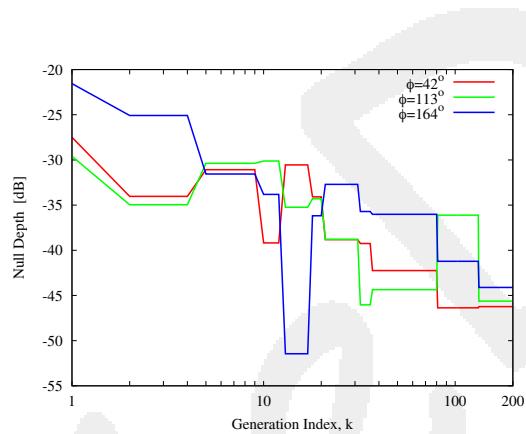


Fig.128 - Nulls Depth

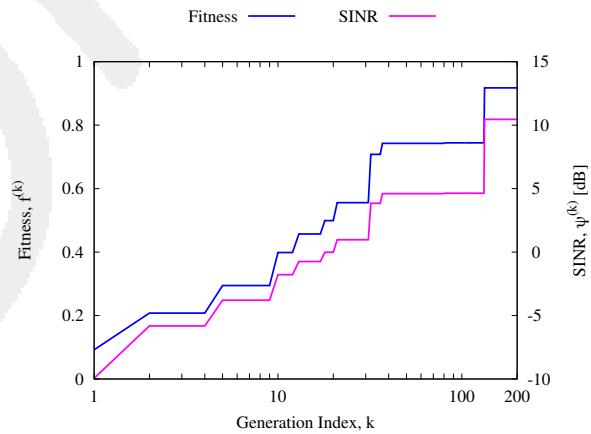
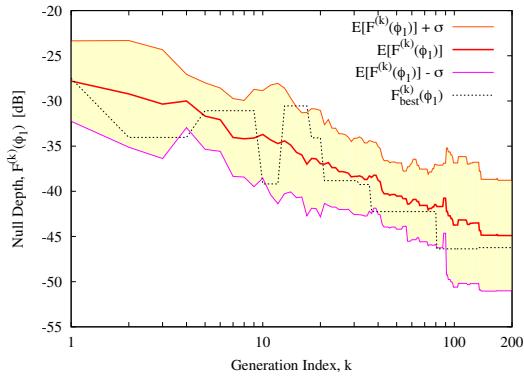
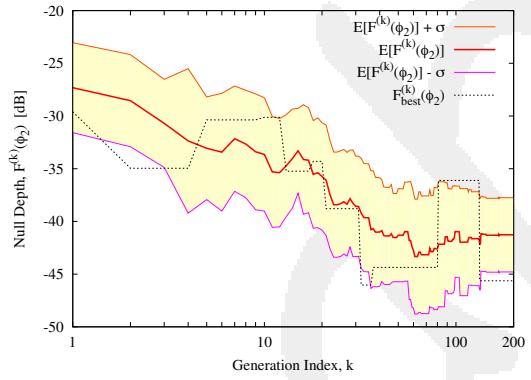


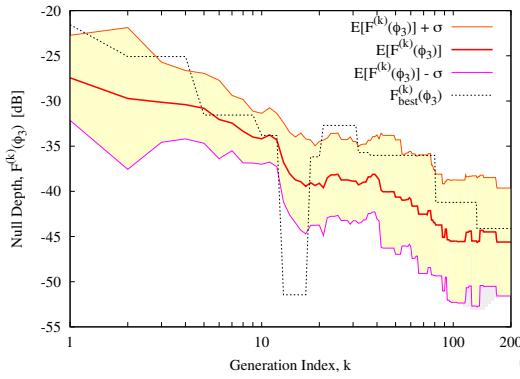
Fig.129 - Fitness - SINR



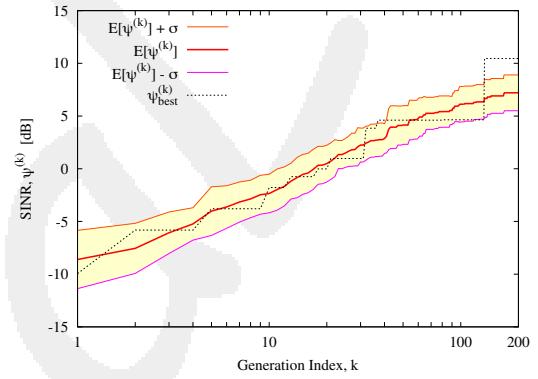
**Fig.130 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics**



**Fig.131 - Null Depth  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$  Statistics**



**Fig.132 - Null Depth  $\theta_3^i = 90^\circ$ ,  $\phi_3^i = 164^\circ$  Statistics**



**Fig.133 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	$AF(\theta_2^i, \phi_2^i)$	$AF(\theta_3^i, \phi_3^i)$	Nr. Active Elements	SINR [dB]
GA	-46.23	-45.63	-44.12	42	10.46

**Tab.22 - GA Simulation Results Analysis**

## TEST CASE 22 - 64 Elements - Fixed Scenario, Triple Interference - $\eta \in [0.60 - 0.60]$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a triple interference.

### Test Case Description

- Number of Elements  $N = 64$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 3$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ, \theta_2^i = 90^\circ, \phi_2^i = 113^\circ, \theta_3^i = 90^\circ, \phi_3^i = 164^\circ$

### Optimization Approach: GA

- Number of Variables:  $X = 64 (\alpha_n, n = 1, \dots, N)$
- Population: 32
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.60$
- Maximum Thinning Coefficient:  $\eta_{max} = 0.60$
- Number of Repetitions for Statistical Analysis: 20

**GA - 64 Elements - Triple Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$ ,  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$ ,  $\theta_3^i = 90^\circ$ ,  $\phi_3^i = 164^\circ$

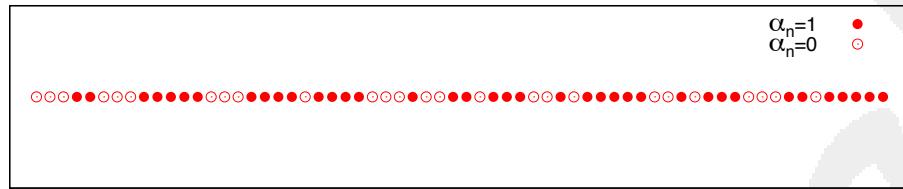


Fig.134 - Thinning Configuration

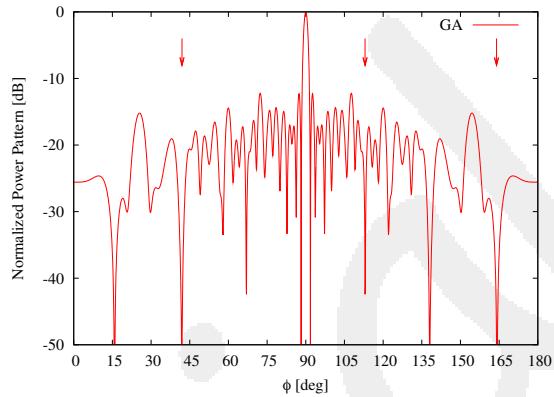


Fig.135 - Pattern

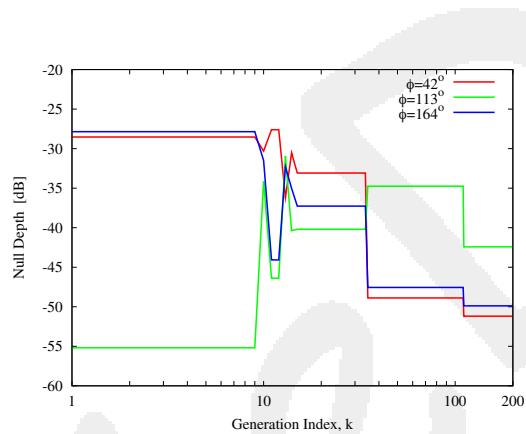


Fig.136 - Nulls Depth

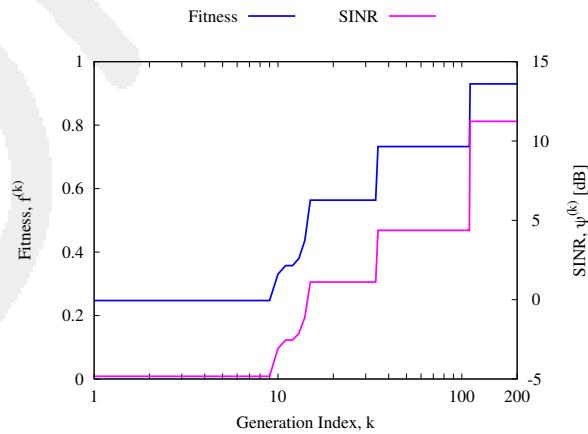
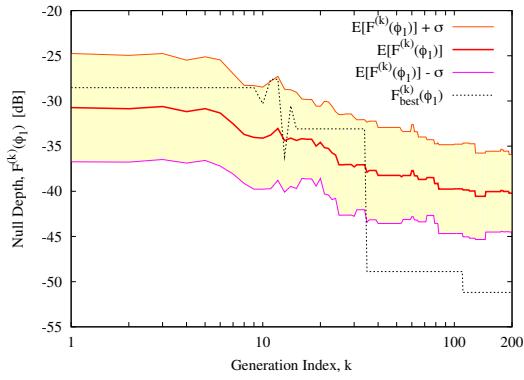
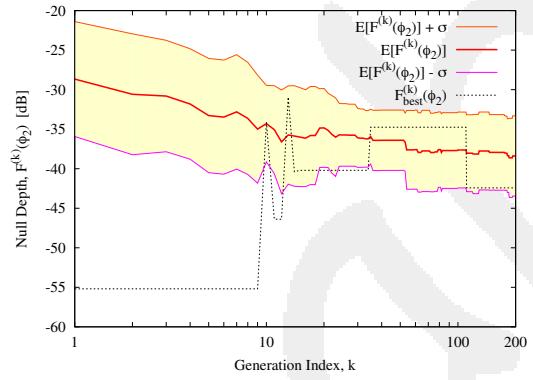


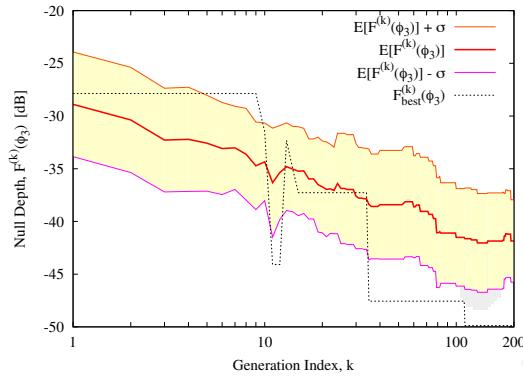
Fig.137 - Fitness - SINR



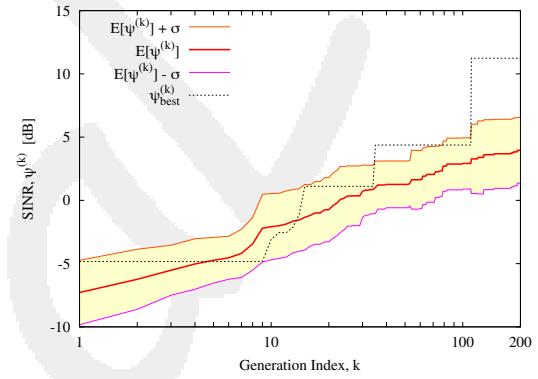
**Fig.138 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics**



**Fig.139 - Null Depth  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$  Statistics**



**Fig.140 - Null Depth  $\theta_3^i = 90^\circ$ ,  $\phi_3^i = 164^\circ$  Statistics**



**Fig.141 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	$AF(\theta_2^i, \phi_2^i)$	$AF(\theta_3^i, \phi_3^i)$	Nr. Active Elements	SINR [dB]
GA	-51.19	-42.42	-49.88	38	11.24

**Tab.23 - GA Simulation Results Analysis**

## TEST CASE 23 - 128 Elements - Fixed Scenario, Single Interference -

$$\eta \in [0.00 - 1.00]$$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a single interference.

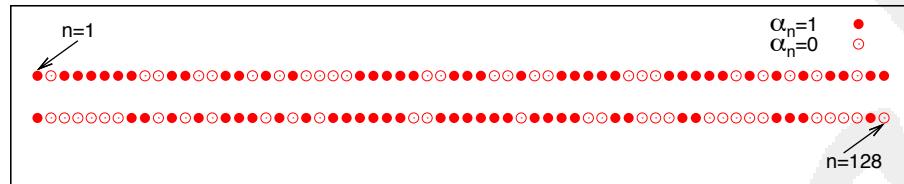
### Test Case Description

- Number of Elements  $N = 128$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 1$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ$

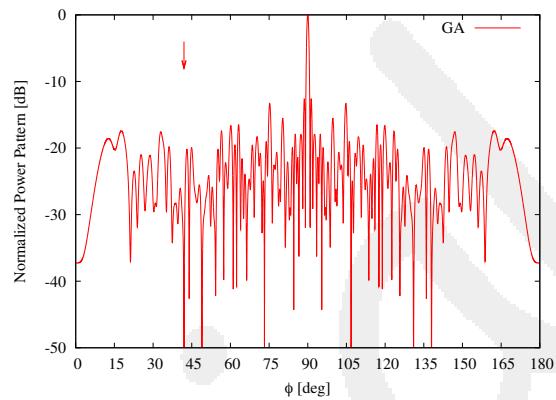
### Optimization Approach: GA

- Number of Variables:  $X = 128$  ( $\alpha_n, n = 1, \dots, N$ )
- Population: 64
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.00$
- Maximum Thinning Coefficient:  $\eta_{max} = 1.00$
- Number of Repetitions for Statistical Analysis: 20

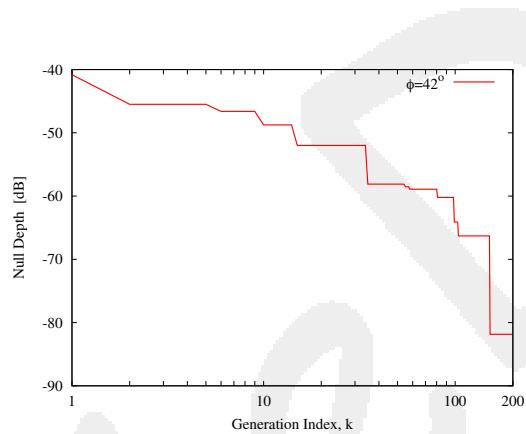
**GA - 128 Elements - Single Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$



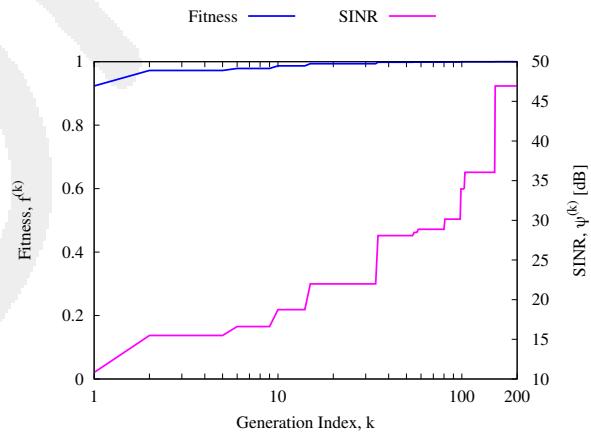
**Fig.142 - Thinning Configuration**



**Fig.143 - Pattern**



**Fig.144 - Nulls Depth**



**Fig.145 - Fitness - SINR**

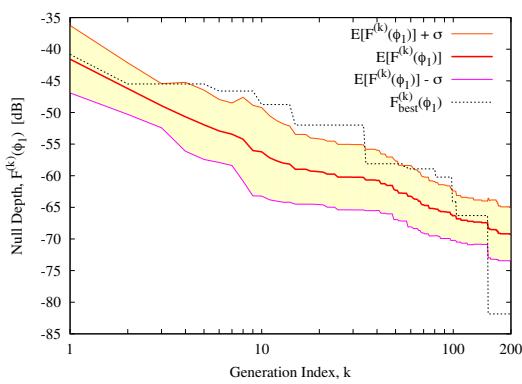


Fig.146 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics

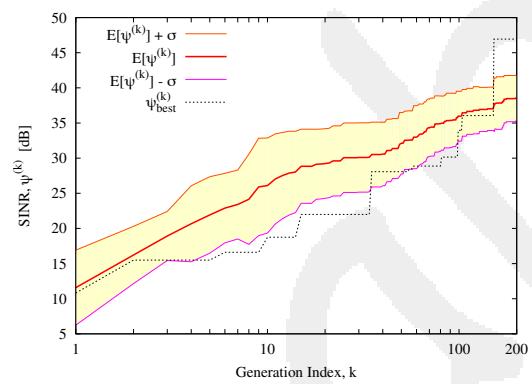


Fig.147 - SINR Statistics

	$AF(\theta_1^i, \phi_1^i)$	Nr. Active Elements	SINR [dB]
GA	-81.85	73	46.94

Tab.24 - GA Simulation Results Analysis

## TEST CASE 23 - 128 Elements - Fixed Scenario, Single Interference - $\eta \in [0.50 - 0.70]$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a single interference.

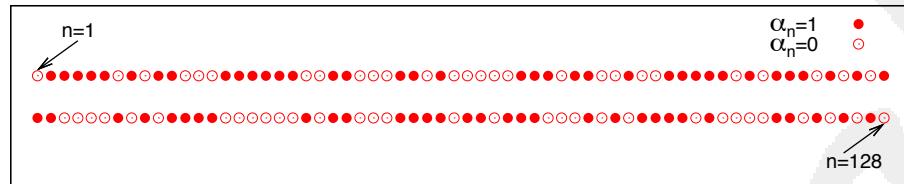
### Test Case Description

- Number of Elements  $N = 128$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 1$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ$

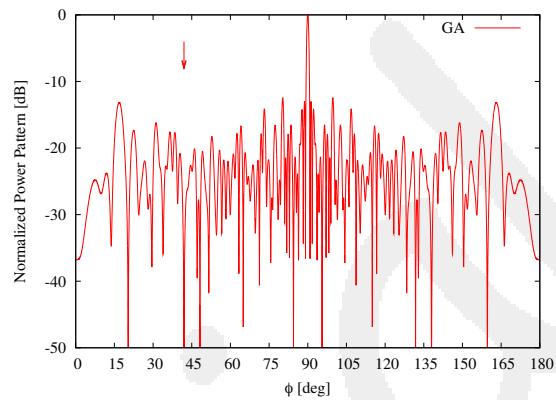
### Optimization Approach: GA

- Number of Variables:  $X = 128$  ( $\alpha_n, n = 1, \dots, N$ )
- Population: 64
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.50$
- Maximum Thinning Coefficient:  $\eta_{max} = 0.70$
- Number of Repetitions for Statistical Analysis: 20

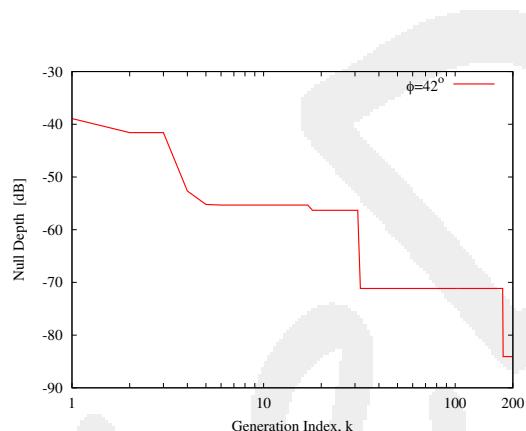
**GA - 128 Elements - Single Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$



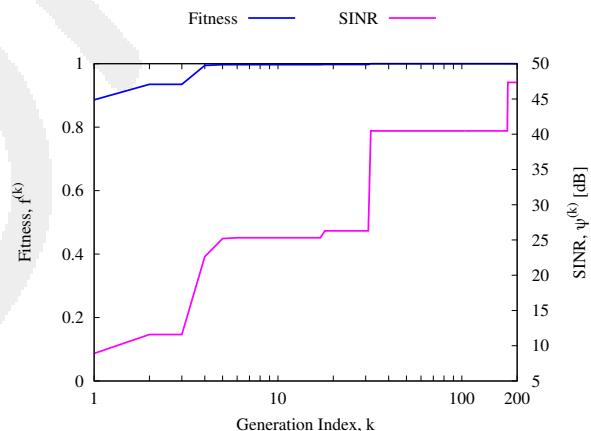
**Fig.148 - Thinning Configuration**



**Fig.149 - Pattern**



**Fig.150 - Nulls Depth**



**Fig.151 - Fitness - SINR**

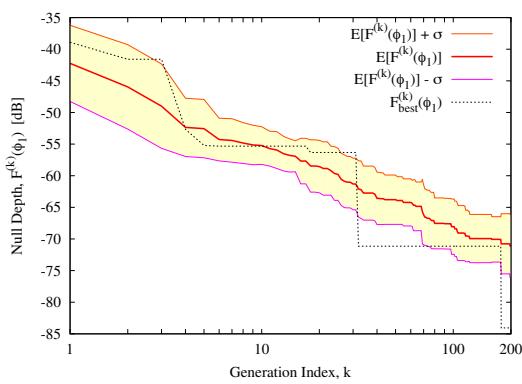


Fig.152 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics

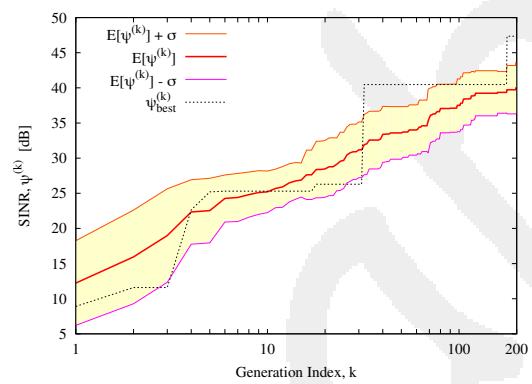


Fig.153 - SINR Statistics

	$AF(\theta_1^i, \phi_1^i)$	Nr. Active Elements	SINR [dB]
GA	-84.07	69	47.35

Tab.25 - GA Simulation Results Analysis

## TEST CASE 10 - 128 Elements - Fixed Scenario, Single Interference -

$$\eta \in [0.60 - 0.60]$$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a single interference.

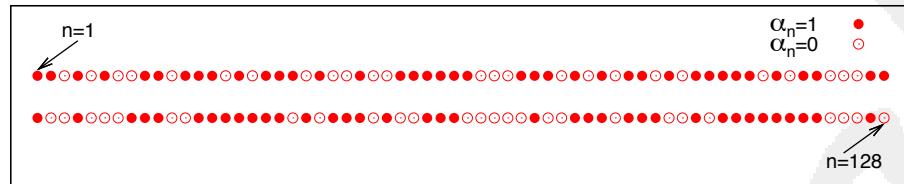
### Test Case Description

- Number of Elements  $N = 128$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 1$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ$

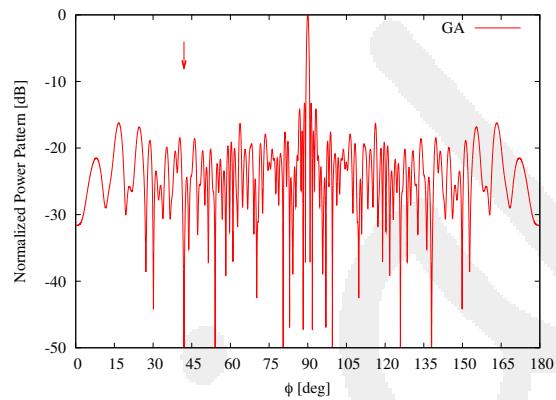
### Optimization Approach: GA

- Number of Variables:  $X = 128$  ( $\alpha_n, n = 1, \dots, N$ )
- Population: 64
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.60$
- Maximum Thinning Coefficient:  $\eta_{max} = 0.60$
- Number of Repetitions for Statistical Analysis: 20

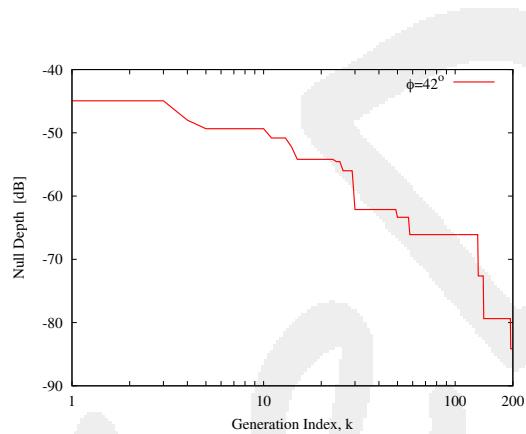
**GA - 128 Elements - Single Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$



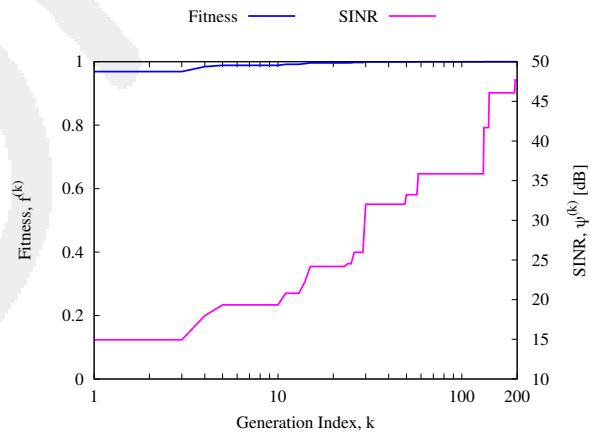
**Fig.154 - Thinning Configuration**



**Fig.155 - Pattern**



**Fig.156 - Nulls Depth**



**Fig.157 - Fitness - SINR**

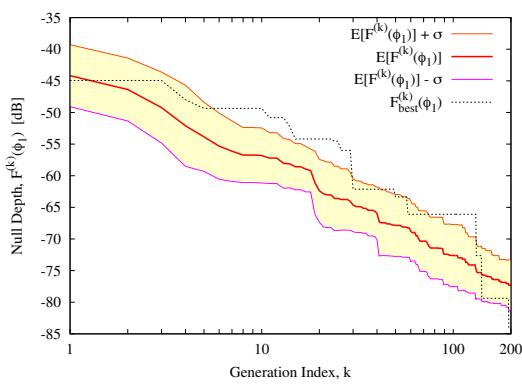


Fig.158 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics

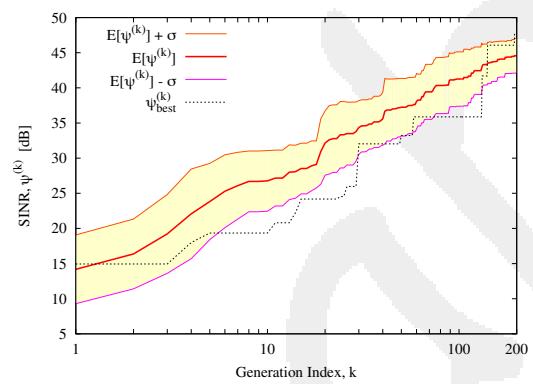


Fig.159 - SINR Statistics

	$AF(\theta_1^i, \phi_1^i)$	Nr. Active Elements	SINR [dB]
GA	-84.14	76	47.69

Tab.26 - GA Simulation Results Analysis

## TEST CASE 23 - 128 Elements - Fixed Scenario, Double Interference

-  $\eta \in [0.00 - 1.00]$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a double interference.

### Test Case Description

- Number of Elements  $N = 128$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 2$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ, \theta_2^i = 90^\circ, \phi_2^i = 113^\circ$

### Optimization Approach: GA

- Number of Variables:  $X = 128 (\alpha_n, n = 1, \dots, N)$
- Population: 64
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.00$
- Maximum Thinning Coefficient:  $\eta_{max} = 1.00$
- Number of Repetitions for Statistical Analysis: 20

**GA - 128 Elements - Double Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$ ,  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$

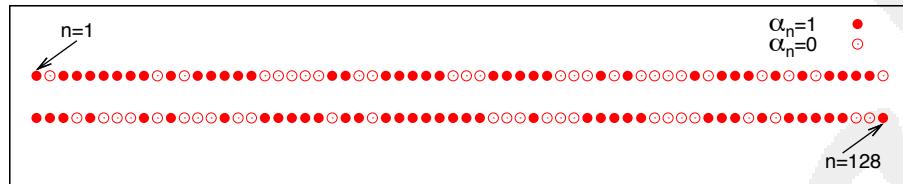


Fig.160 - Thinning Configuration

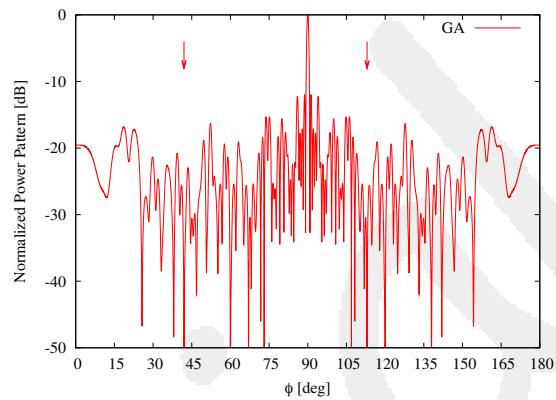


Fig.161 - Pattern

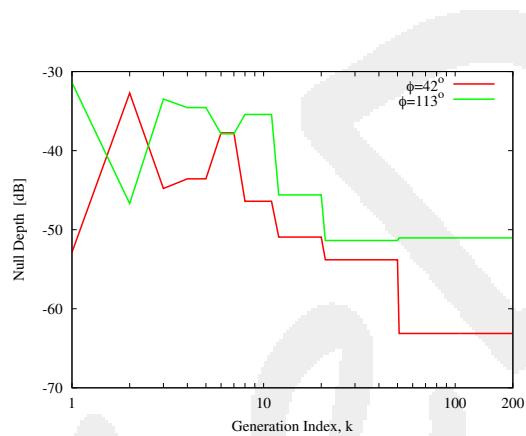


Fig.162 - Nulls Depth

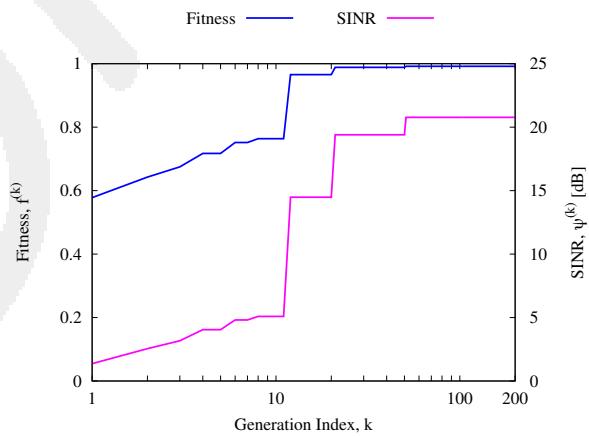
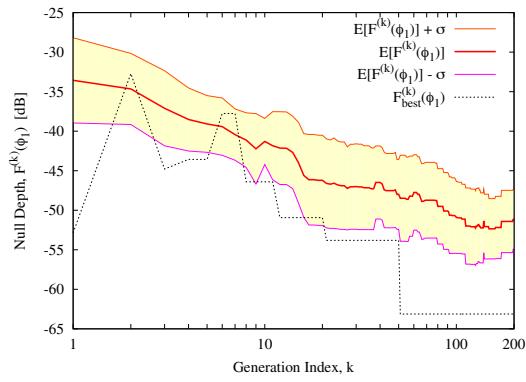
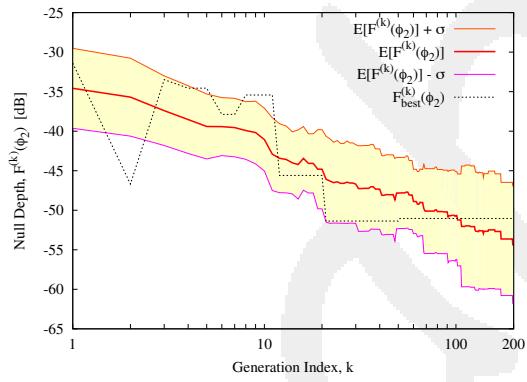


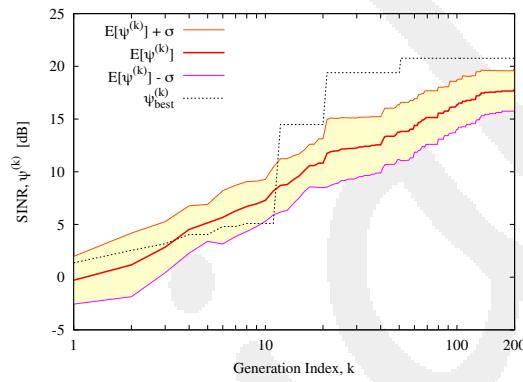
Fig.163 - Fitness - SINR



**Fig.164 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics**



**Fig.165 - Null Depth  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$  Statistics**



**Fig.166 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	$AF(\theta_2^i, \phi_2^i)$	Nr. Active Elements	$SINR [dB]$
GA	-63.12	-51.04	76	20.77

**Tab.27 - GA Simulation Results Analysis**

## TEST CASE 23 - 128 Elements - Fixed Scenario, Double Interference

-  $\eta \in [0.50 - 0.70]$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a double interference.

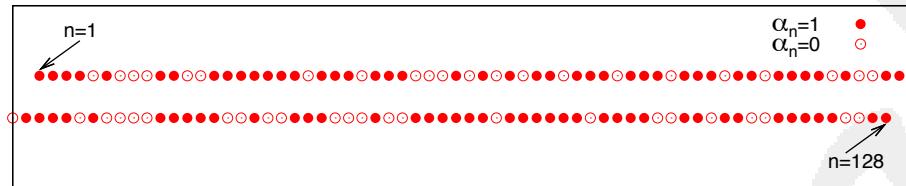
### Test Case Description

- Number of Elements  $N = 128$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 2$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ, \theta_2^i = 90^\circ, \phi_2^i = 113^\circ$

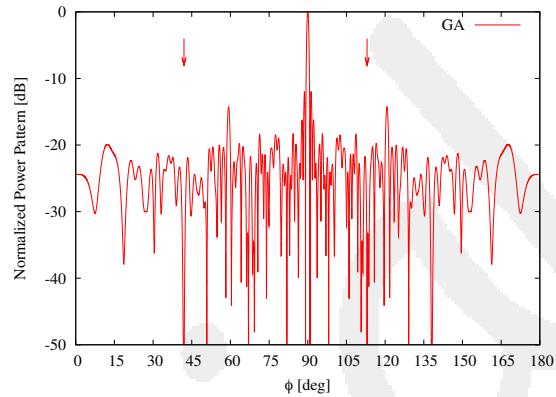
### Optimization Approach: GA

- Number of Variables:  $X = 128 (\alpha_n, n = 1, \dots, N)$
- Population: 64
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.50$
- Maximum Thinning Coefficient:  $\eta_{max} = 0.70$
- Number of Repetitions for Statistical Analysis: 20

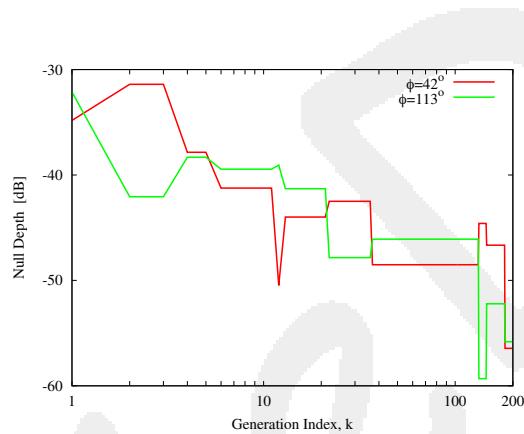
**GA - 128 Elements - Double Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$ ,  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$



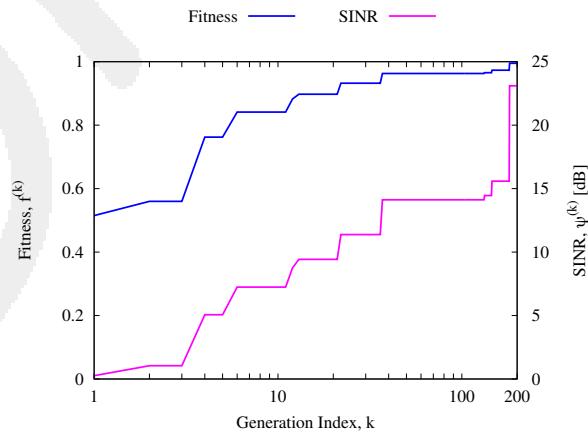
**Fig.167 - Thinning Configuration**



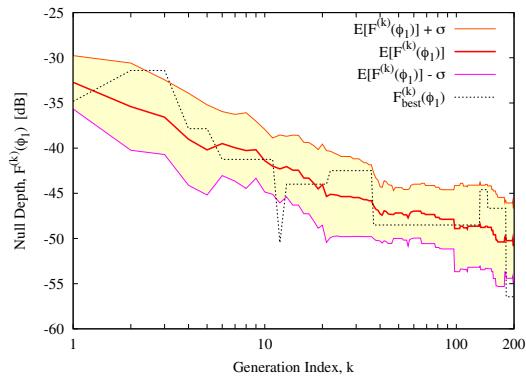
**Fig.168 - Pattern**



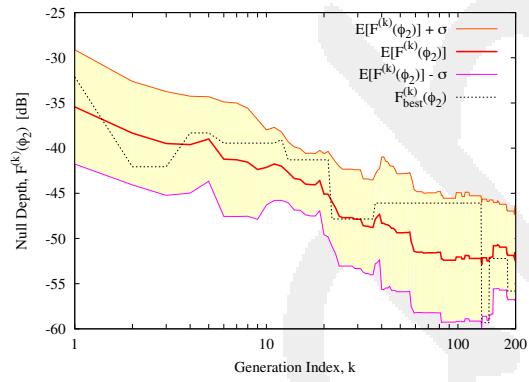
**Fig.169 - Nulls Depth**



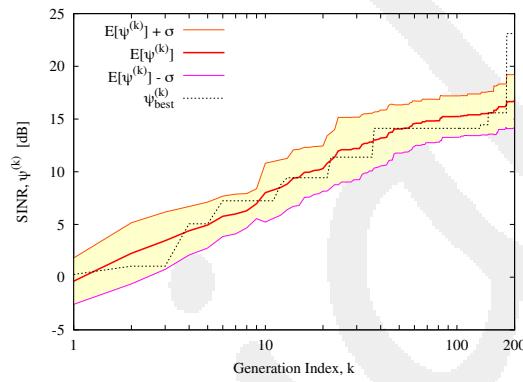
**Fig.170 - Fitness - SINR**



**Fig.171 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics**



**Fig.172 - Null Depth  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$  Statistics**



**Fig.173 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	$AF(\theta_2^i, \phi_2^i)$	Nr. Active Elements	$SINR [dB]$
GA	-56.45	-55.82	83	23.10

**Tab.28 - GA Simulation Results Analysis**

## TEST CASE 10 - 128 Elements - Fixed Scenario, Double Interference

-  $\eta \in [0.60 - 0.60]$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a double interference.

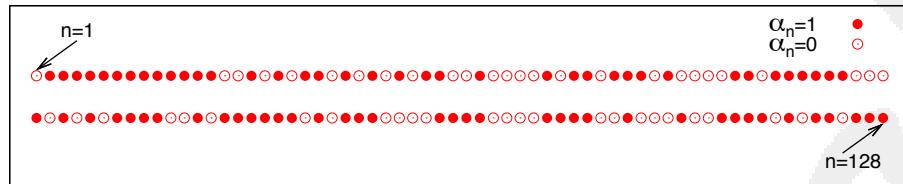
### Test Case Description

- Number of Elements  $N = 128$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 2$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ, \theta_2^i = 90^\circ, \phi_2^i = 113^\circ$

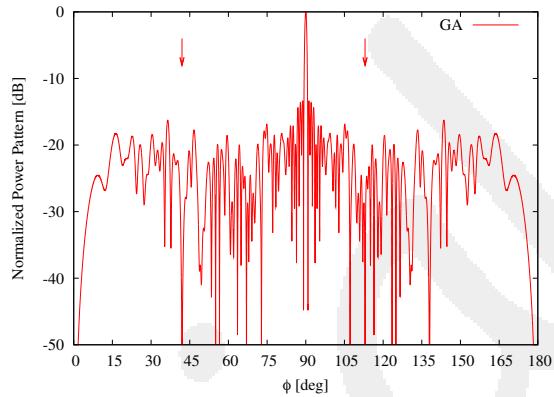
### Optimization Approach: GA

- Number of Variables:  $X = 128 (\alpha_n, n = 1, \dots, N)$
- Population: 64
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.60$
- Maximum Thinning Coefficient:  $\eta_{max} = 0.60$
- Number of Repetitions for Statistical Analysis: 20

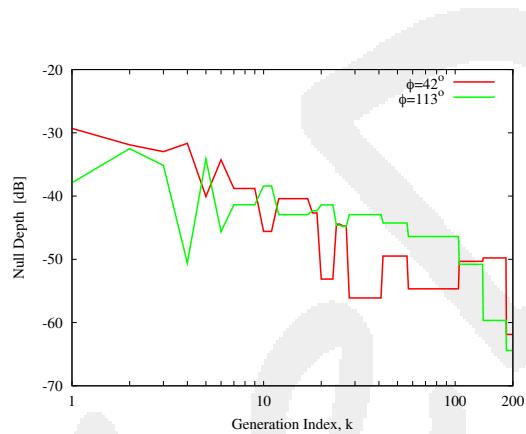
**GA - 128 Elements - Double Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$ ,  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$



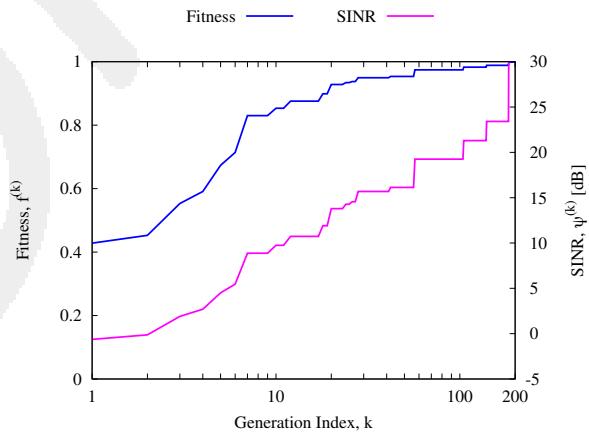
**Fig.174 - Thinning Configuration**



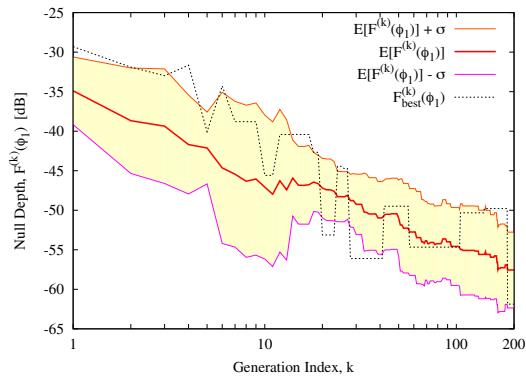
**Fig.175 - Pattern**



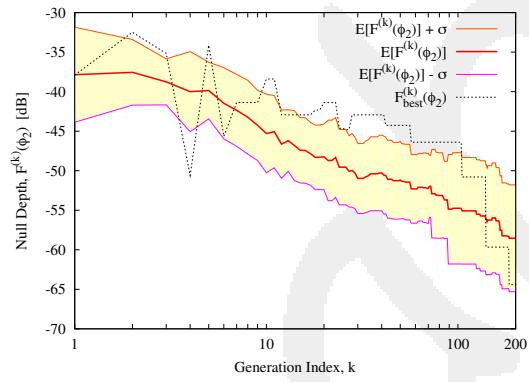
**Fig.176 - Nulls Depth**



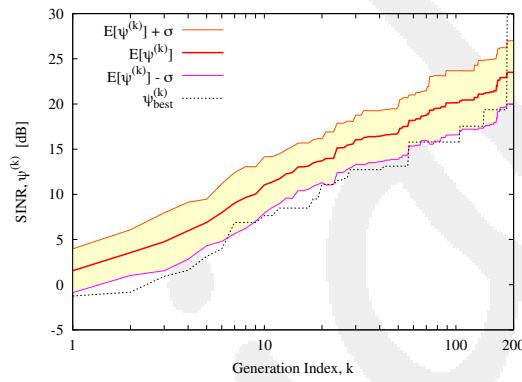
**Fig.177 - Fitness - SINR**



**Fig.178 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics**



**Fig.179 - Null Depth  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$  Statistics**



**Fig.180 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	$AF(\theta_2^i, \phi_2^i)$	Nr. Active Elements	SINR [dB]
GA	-61.87	-64.42	76	29.84

**Tab.29 - GA Simulation Results Analysis**

## TEST CASE 23 - 128 Elements - Fixed Scenario, Triple Interference - $\eta \in [0.00 - 1.00]$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a triple interference.

### Test Case Description

- Number of Elements  $N = 128$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 3$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ, \theta_2^i = 90^\circ, \phi_2^i = 113^\circ, \theta_3^i = 90^\circ, \phi_3^i = 164^\circ$

### Optimization Approach: GA

- Number of Variables:  $X = 128$  ( $\alpha_n, n = 1, \dots, N$ )
- Population: 64
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.00$
- Maximum Thinning Coefficient:  $\eta_{max} = 1.00$
- Number of Repetitions for Statistical Analysis: 20

**GA - 128 Elements - Triple Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$ ,  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$ ,  $\theta_3^i = 90^\circ$ ,  $\phi_3^i = 164^\circ$

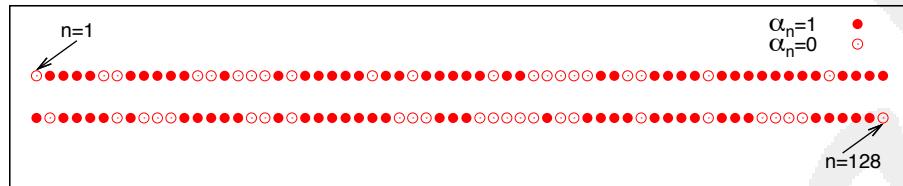


Fig.181 - Thinning Configuration

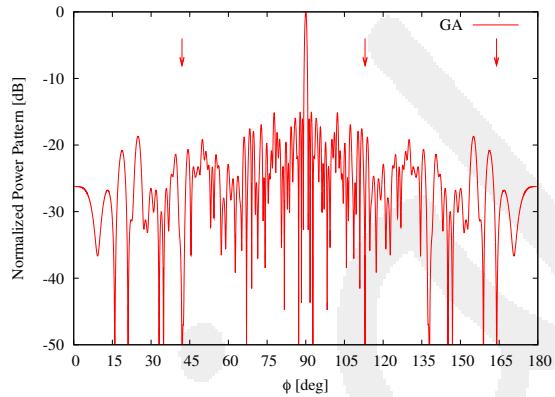


Fig.182 - Pattern

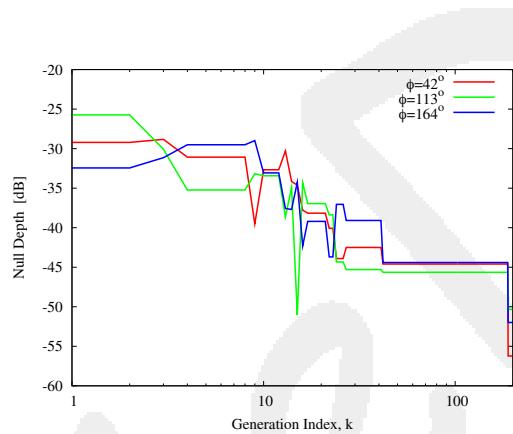


Fig.183 - Nulls Depth

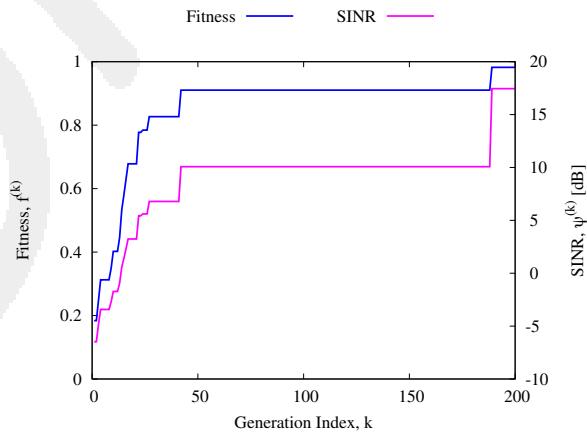
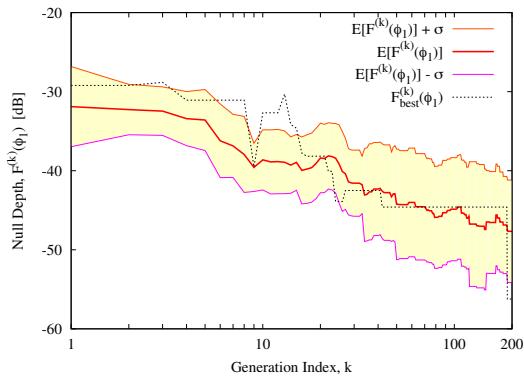
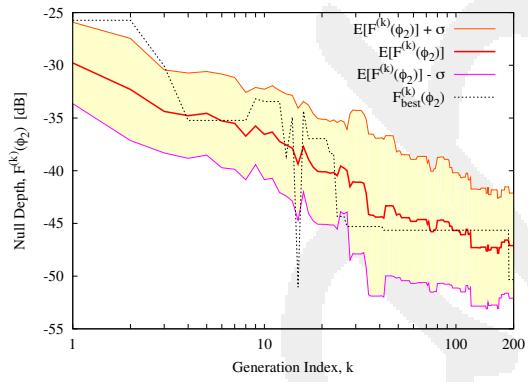


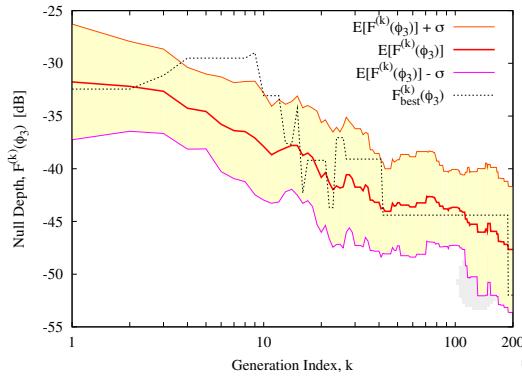
Fig.184 - Fitness - SINR



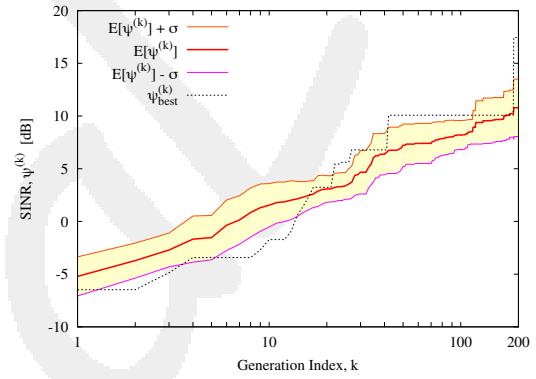
**Fig.185 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics**



**Fig.186 - Null Depth  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$  Statistics**



**Fig.187 - Null Depth  $\theta_3^i = 90^\circ$ ,  $\phi_3^i = 164^\circ$  Statistics**



**Fig.188 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	$AF(\theta_2^i, \phi_2^i)$	$AF(\theta_3^i, \phi_3^i)$	Nr. Active Elements	SINR [dB]
GA	-56.23	-50.33	-51.99	82	17.45

**Tab.30 - GA Simulation Results Analysis**

## TEST CASE 23 - 128 Elements - Fixed Scenario, Triple Interference - $\eta \in [0.50 - 0.70]$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a triple interference.

### Test Case Description

- Number of Elements  $N = 128$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 3$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ, \theta_2^i = 90^\circ, \phi_2^i = 113^\circ, \theta_3^i = 90^\circ, \phi_3^i = 164^\circ$

### Optimization Approach: GA

- Number of Variables:  $X = 128$  ( $\alpha_n, n = 1, \dots, N$ )
- Population: 64
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.50$
- Maximum Thinning Coefficient:  $\eta_{max} = 0.70$
- Number of Repetitions for Statistical Analysis: 20

**GA - 128 Elements - Triple Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$ ,  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$ ,  $\theta_3^i = 90^\circ$ ,  $\phi_3^i = 164^\circ$

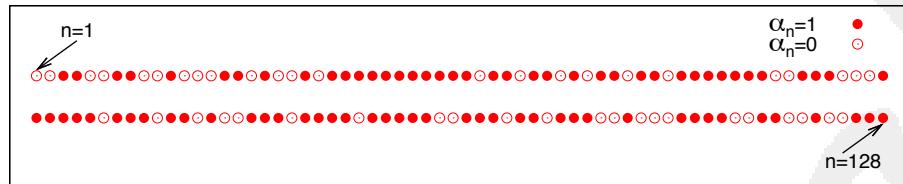


Fig.189 - Thinning Configuration

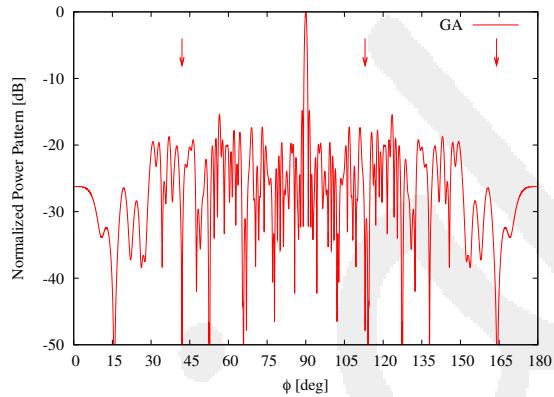


Fig.190 - Pattern

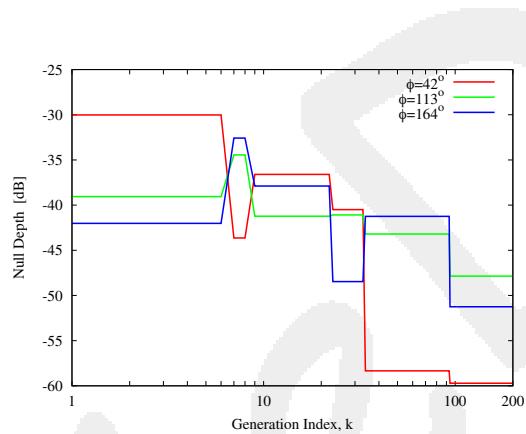


Fig.191 - Nulls Depth

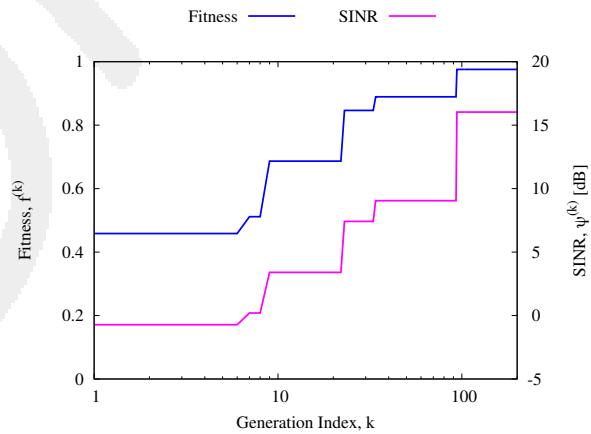
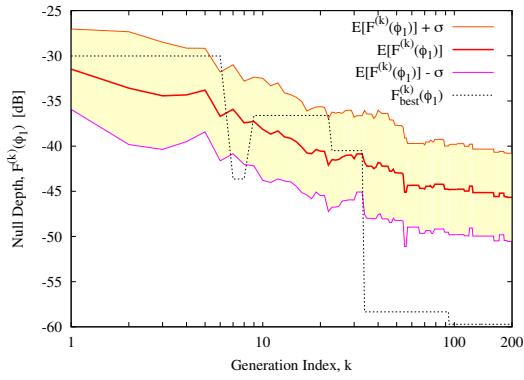
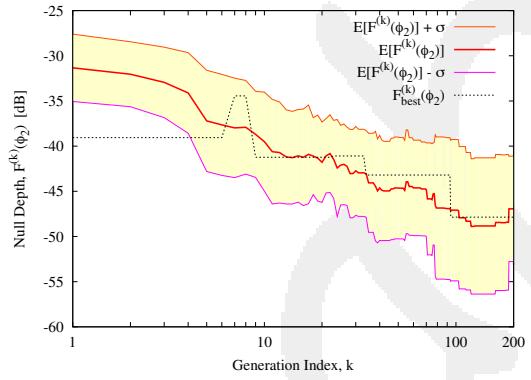


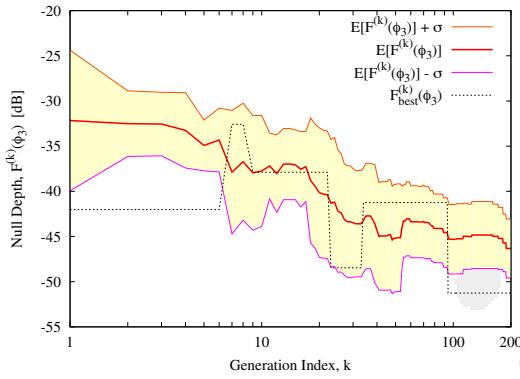
Fig.192 - Fitness - SINR



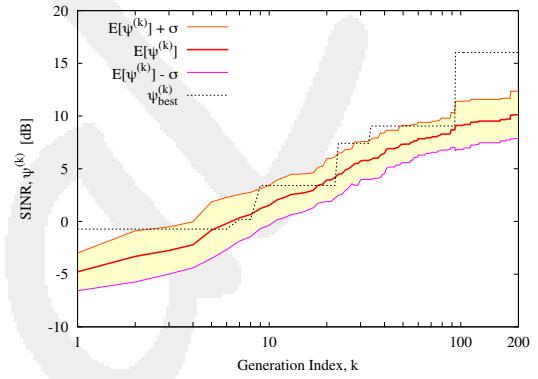
**Fig.193 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics**



**Fig.194 - Null Depth  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$  Statistics**



**Fig.195 - Null Depth  $\theta_3^i = 90^\circ$ ,  $\phi_3^i = 164^\circ$  Statistics**



**Fig.196 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	$AF(\theta_2^i, \phi_2^i)$	$AF(\theta_3^i, \phi_3^i)$	Nr. Active Elements	SINR [dB]
GA	-59.71	-47.86	-51.25	82	16.03

**Tab.31 - GA Simulation Results Analysis**

## TEST CASE 10 - 128 Elements - Fixed Scenario, Triple Interference -

$$\eta \in [0.60 - 0.60]$$

### Goal

Maximization of the SINR using genetic algorithms (GA) to determine the optimal thinned array configuration, considering a static scenario with a triple interference.

### Test Case Description

- Number of Elements  $N = 128$
- Elements Spacing:  $d = 0.5\lambda$
- Max Gain Pattern Direction :  $\theta^d = 90^\circ, \phi^d = 90^\circ$
- Desired Signal Power:  $0 \text{ dB}$
- Interference Power:  $30 \text{ dB}$
- Noise Power:  $-30 \text{ dB}$
- Number of Interferences:  $N^I = 3$
- Interference Direction Of Arrival:  $\theta_1^i = 90^\circ, \phi_1^i = 42^\circ, \theta_2^i = 90^\circ, \phi_2^i = 113^\circ, \theta_3^i = 90^\circ, \phi_3^i = 164^\circ$

### Optimization Approach: GA

- Number of Variables:  $X = 128$  ( $\alpha_n, n = 1, \dots, N$ )
- Population: 64
- Crossover Probability: 0.9
- Mutation Probability: 0.01
- Number of Generations: 200
- Minimum Thinning Coefficient:  $\eta_{min} = 0.60$
- Maximum Thinning Coefficient:  $\eta_{max} = 0.60$
- Number of Repetitions for Statistical Analysis: 20

**GA - 128 Elements - Triple Interference:**  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$ ,  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$ ,  $\theta_3^i = 90^\circ$ ,  $\phi_3^i = 164^\circ$

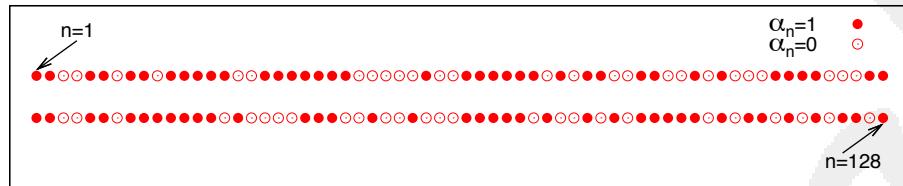


Fig.197 - Thinning Configuration

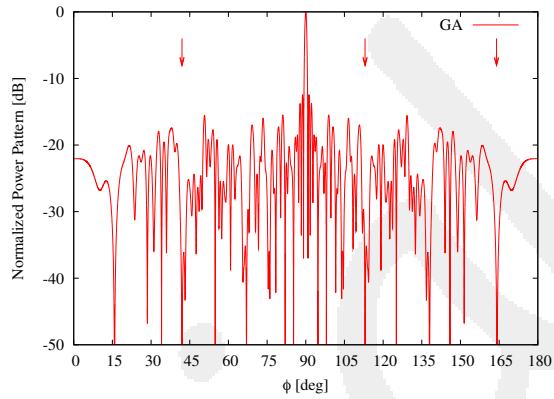


Fig.198 - Pattern

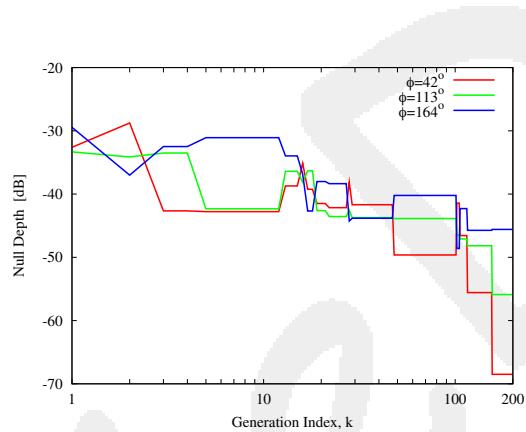


Fig.199 - Nulls Depth

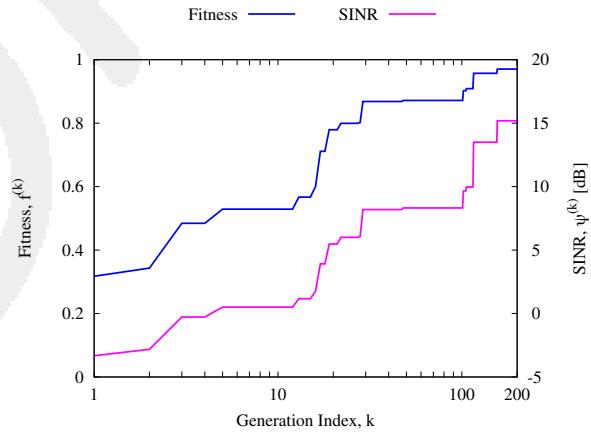
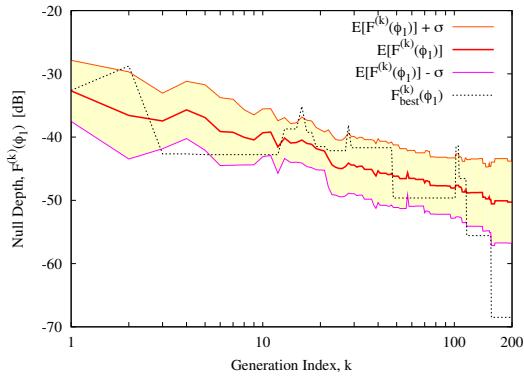
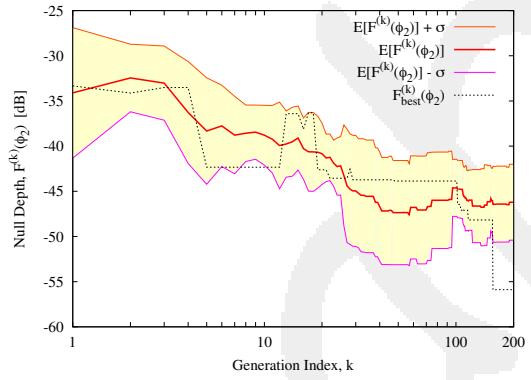


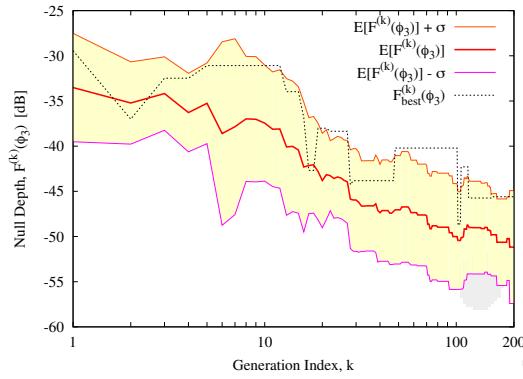
Fig.200 - Fitness - SINR



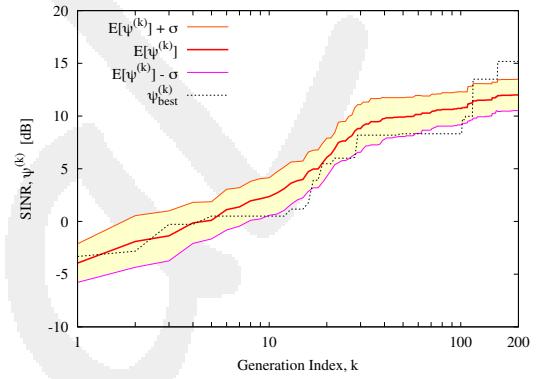
**Fig.201 - Null Depth  $\theta_1^i = 90^\circ$ ,  $\phi_1^i = 42^\circ$  Statistics**



**Fig.202 - Null Depth  $\theta_2^i = 90^\circ$ ,  $\phi_2^i = 113^\circ$  Statistics**



**Fig.203 - Null Depth  $\theta_3^i = 90^\circ$ ,  $\phi_3^i = 164^\circ$  Statistics**



**Fig.204 - SINR Statistics**

	$AF(\theta_1^i, \phi_1^i)$	$AF(\theta_2^i, \phi_2^i)$	$AF(\theta_3^i, \phi_3^i)$	Nr. Active Elements	SINR [dB]
GA	-68.50	-55.89	-45.59	76	15.18

**Tab.32 - GA Simulation Results Analysis**

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