

# **A failure correction strategy in time-modulated linear arrays**

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## **Abstract**

A technique for failure correction in time-modulated linear arrays is analyzed in this report. Starting from the knowledge of the array elements with failures, the on-off behavior of the switches at the other elements is properly reconfigured to radiate a pattern as close as possible to the ideal one in terms of pattern features. The array reconfiguration is carried out by solving an optimization problem through the minimization of a suitable cost function proportional to the mismatch between ideal and reconfigured pattern features.

# Numerical Results

## TEST CASE 1.a - $N = 16$ , Single Failure (External Pulse)

### Goal

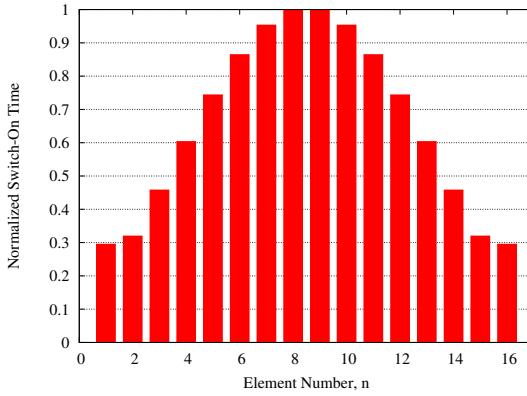
Reconfigure the radiated pattern through a *PSO*-based optimization strategy according to the feature of the pattern before the failure occurred to the *RF* switches.

### Description

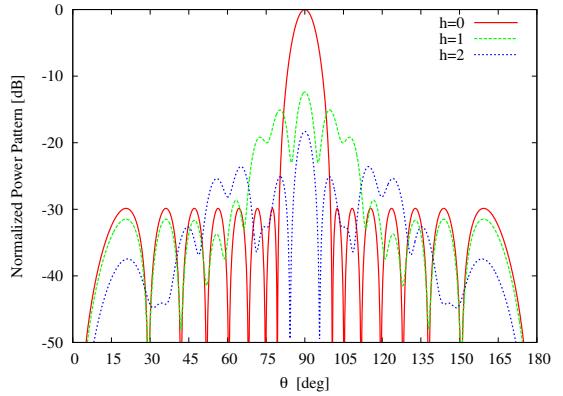
- Number of Elements  $N = 16$
- Elements Spacing:  $d = 0.5\lambda$
- Static Array Excitations: Uniform,  $I_n = 1, n = 1, \dots, N$
- Averaged Time-Modulated Array Excitations: *Dolph-Chebyshev*,  $SLL = -30 \text{ dB}$ ,  $BW = 7.95 \text{ deg}$
- Failure occurred at the element  $n = 2$

### Optimization Approach: PSO [1]

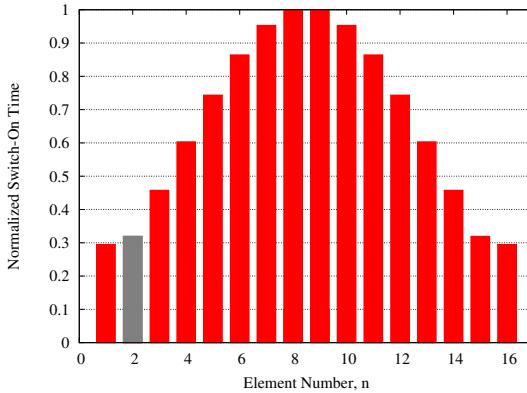
- Number of Variables:  $X = 16 (\tau_n, n = 1, \dots, N)$
- Number of Particles:  $S = N$
- Number of Iterations:  $M = 1000$
- Inertial Weight:  $I_w = 0.4$
- Cost Function:  $SLL$  weight:  $w_{SLL} = 100$ ,  $BW$  weight:  $w_{BW} = 1$ ,  $SR$  weight:  $w_{SR} = 1$



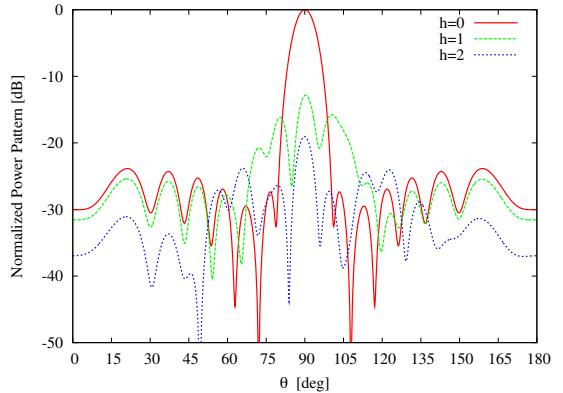
**Fig. 1 - Pulse Sequence - Original**



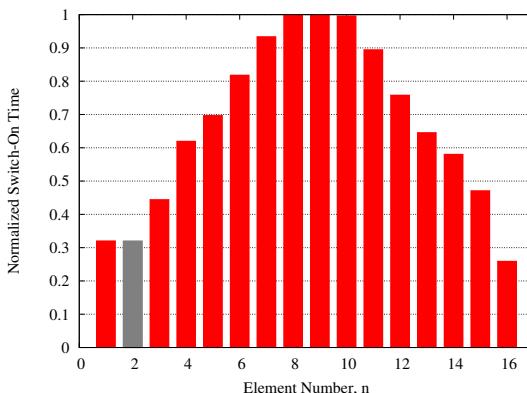
**Fig. 2 - Patterns - Original**



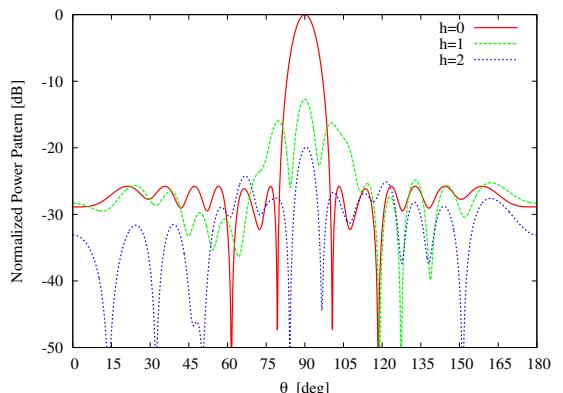
**Fig. 3 - Pulse Sequence - Compromised**



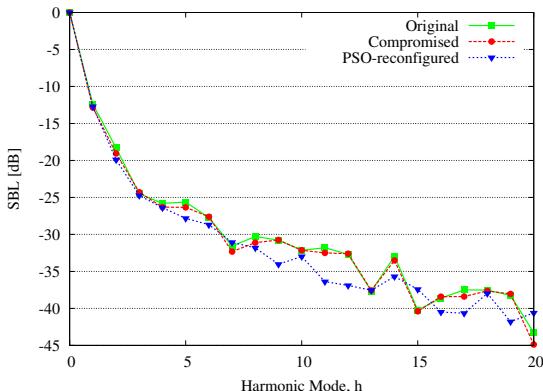
**Fig. 4 - Patterns - Compromised**



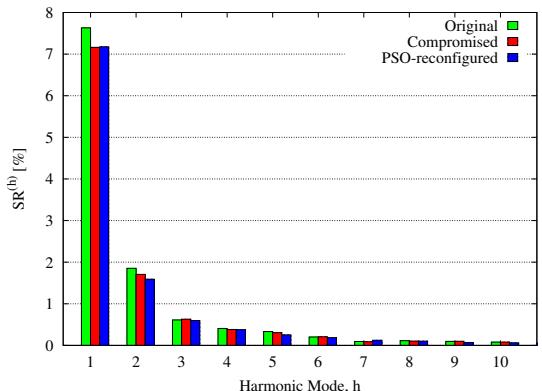
**Fig. 5 - Pulse Sequence - PSO-reconfigured**



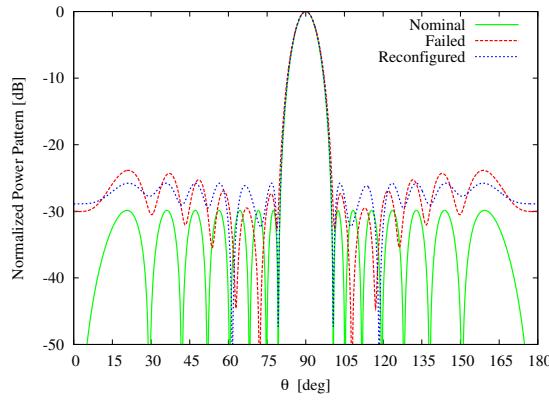
**Fig. 6 - Patterns - PSO-reconfigured**



**Fig. 7 - SBL - Comparison**



**Fig. 8 - SR - Comparison**



**Fig. 9 - SBL - Comparison**

	<i>SLL</i> [dB]	<i>BW</i> [deg]	<i>D</i> [dB]	<i>SBL</i> [dB]	<i>SR</i> [%]
<i>Original</i>	-29.86	7.95	8.36	-12.39	24.17
<i>Compromised</i>	-23.85	8.25	8.37	-12.84	22.79
<i>PSO - reconfigured</i>	-25.78	8.08	8.61	-12.71	22.21

**Tab. I - Patterns features: Sidelobe Level (*SLL*), -3dB Beamwidth (*BW*), Directivity (*D*), Sideband Level (*SBL*) and Sideband Radiation (*SR*)**

## TEST CASE 1.b - $N = 16$ , Single Failure (External Pulse)

### Goal

Reconfigure the radiated pattern through a *PSO*-based optimization strategy according to the feature of the pattern before the failure occurred to the *RF* switches.

### Differences wrt previous test case

- Previous: *BW* weight:  $w_{BW} = 1$
- Current: *BW* weight:  $w_{BW} = 0$  (*SLL*-only required matching)

### Description

- Number of Elements  $N = 16$
- Elements Spacing:  $d = 0.5\lambda$
- Static Array Excitations: Uniform,  $I_n = 1, n = 1, , N$
- Averaged Time-Modulated Array Excitations: *Dolph-Chebyshev*,  $SLL = -30 \text{ dB}$ ,  $BW = 7.95 \text{ deg}$
- Failure occurred at the element  $n = 2$

### Optimization Approach: PSO [1]

- Number of Variables:  $X = 16$  ( $\tau_n, n = 1, \dots, N$ )
- Number of Particles:  $S = N$
- Number of Iterations:  $M = 1000$
- Inertial Weight:  $I_w = 0.4$
- Cost Function: *SLL* weight:  $w_{SLL} = 100$ , *BW* weight:  $w_{BW} = 0$ , *SR* weight:  $w_{SR} = 1$

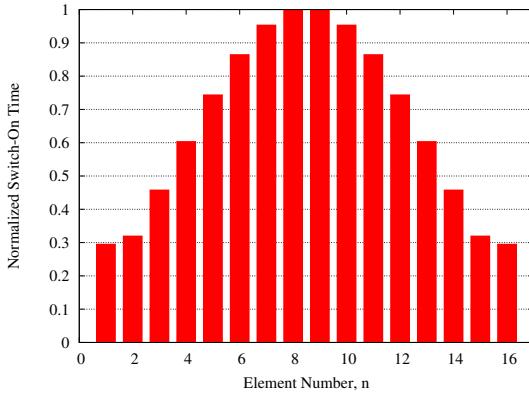


Fig. 10 - Pulse Sequence - Original

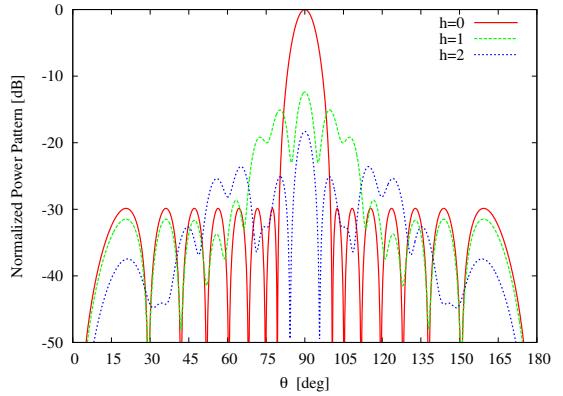


Fig. 11 - Patterns - Original

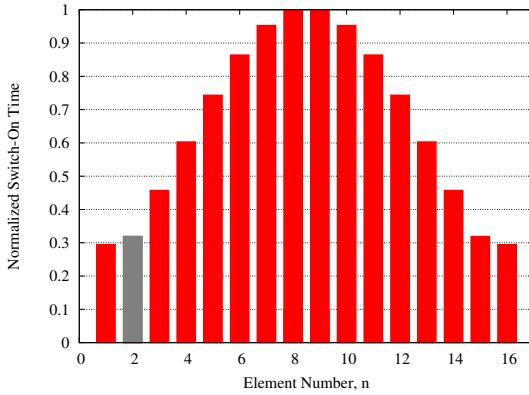


Fig. 12 - Pulse Sequence - Compromised

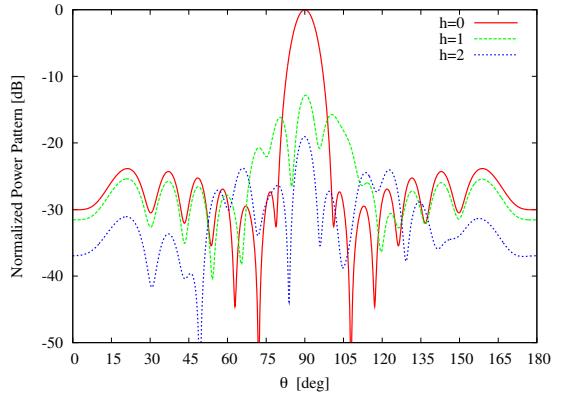


Fig. 13 - Patterns - Compromised

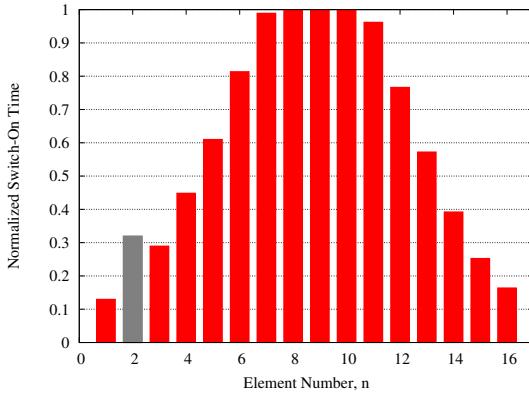


Fig. 14 - Pulse Sequence - PSO-reconfigured

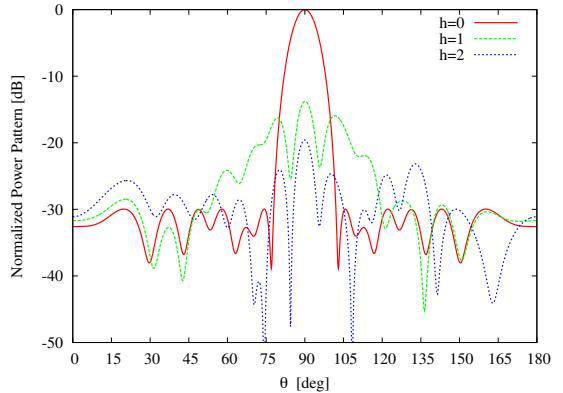


Fig. 15 - Patterns - PSO-reconfigured

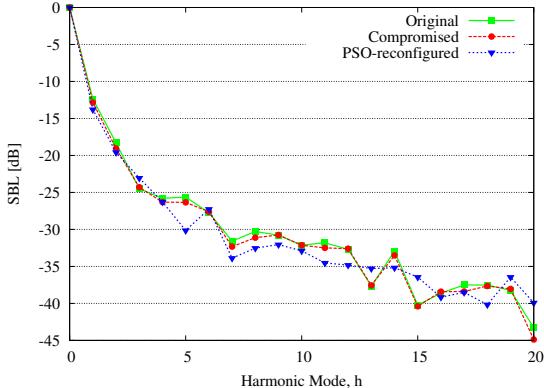


Fig. 16 - SBL - Comparison

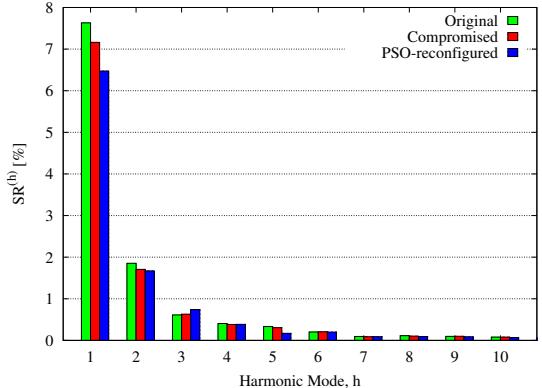
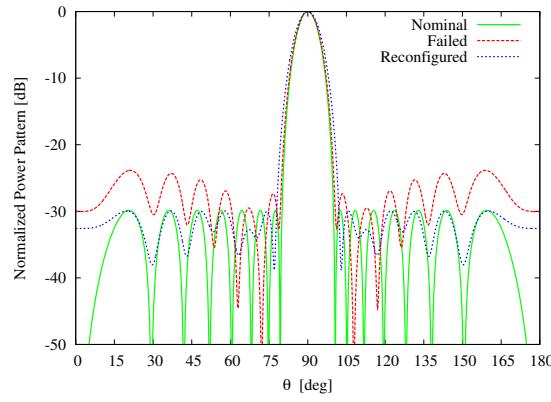


Fig. 17 - SR - Comparison



**Fig. 18 - SBL - Comparison**

	<i>SLL</i> [dB]	<i>BW</i> [deg]	<i>D</i> [dB]	<i>SBL</i> [dB]	<i>SR</i> [%]
<i>Original</i>	-29.86	7.95	8.36	-12.39	24.17
<i>Compromised</i>	-23.85	8.25	8.37	-12.84	22.79
<i>PSO – reconfigured</i>	-29.96	9.16	7.96	-13.79	21.20

**Tab. II - Patterns features: Sidelobe Level (*SLL*), -3dB Beamwidth (*BW*), Directivity (*D*), Sideband Level (*SBL*) and Sideband Radiation (*SR*)**

## TEST CASE 1.c - $N = 16$ , Single Failure (Internal Pulse)

### Goal

Reconfigure the radiated pattern through a *PSO*-based optimization strategy according to the feature of the pattern before the failure occurred to the *RF* switches.

### Differences wrt previous test case

- Previous: Failure occurred at the element  $n = 2$
- Current: Failure occurred at the element  $n = 8$

### Description

- Number of Elements  $N = 16$
- Elements Spacing:  $d = 0.5\lambda$
- Static Array Excitations: Uniform,  $I_n = 1, n = 1, , N$
- Averaged Time-Modulated Array Excitations: *Dolph-Chebyshev*,  $SLL = -30 \text{ dB}$ ,  $BW = 7.95 \text{ deg}$
- Failure occurred at the element  $n = 8$

### Optimization Approach: PSO [1]

- Number of Variables:  $X = 16 (\tau_n, n = 1, \dots, N)$
- Number of Particles:  $S = N$
- Number of Iterations:  $M = 1000$
- Inertial Weight:  $I_w = 0.4$
- Cost Function:  $SLL$  weight:  $w_{SLL} = 100$ ,  $BW$  weight:  $w_{BW} = 1$ ,  $SR$  weight:  $w_{SR} = 1$

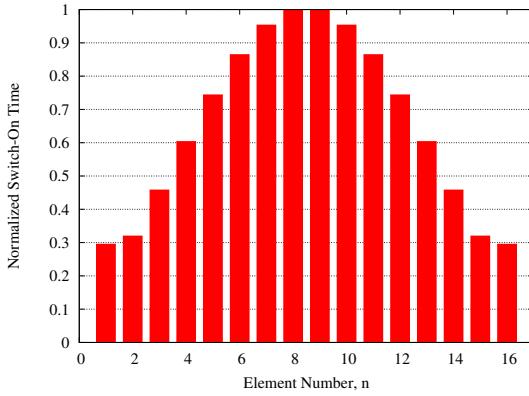


Fig. 19 - Pulse Sequence - Original

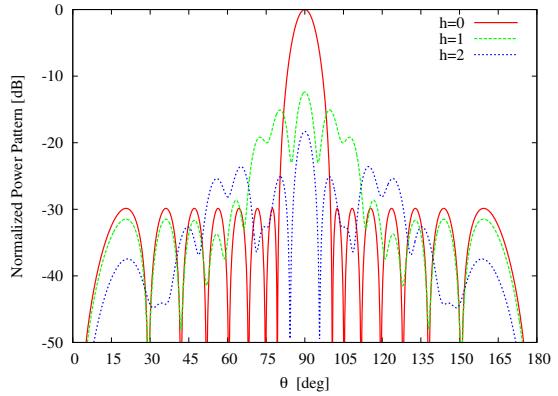


Fig. 20 - Patterns - Original

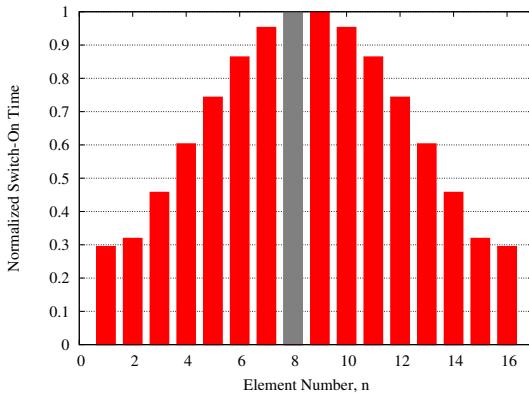


Fig. 21 - Pulse Sequence - Compromised

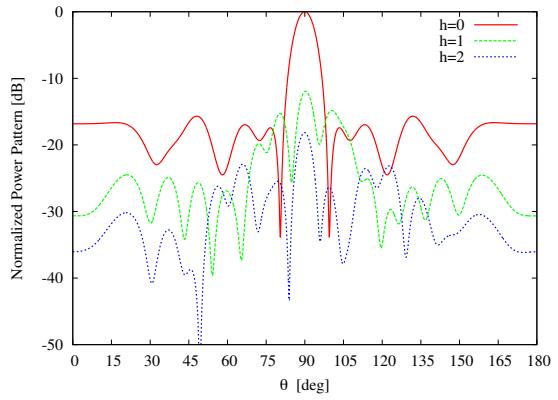


Fig. 22 - Patterns - Compromised

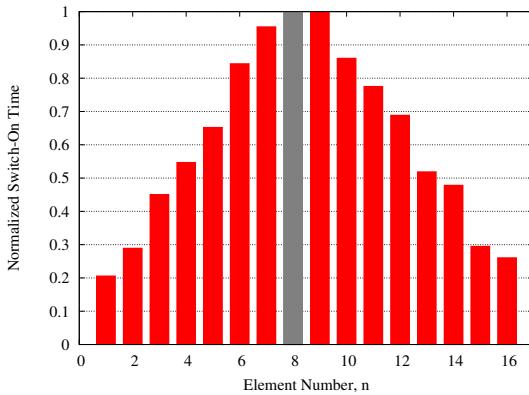


Fig. 23 - Pulse Sequence - PSO-reconfigured

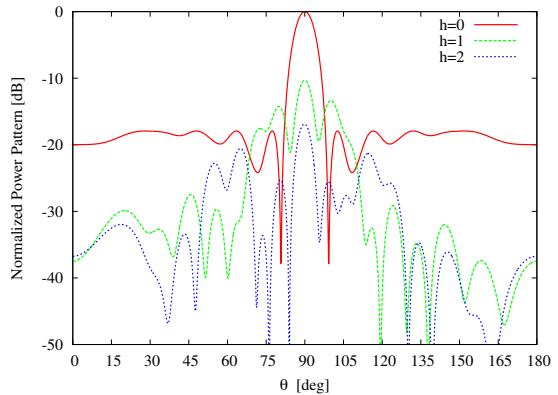


Fig. 24 - Patterns - PSO-reconfigured

	<i>SLL</i> [dB]	<i>BW</i> [deg]	<i>D</i> [dB]	<i>SBL</i> [dB]	<i>SR</i> [%]
<i>Original</i>	-29.86	7.95	8.36	-12.39	24.17
<i>Compromised</i>	-15.68	7.80	7.77	-11.94	25.28
<i>PSO - reconfigured</i>	-17.93	7.65	7.15	-10.33	30.35

Tab. III - Patterns features: Sidelobe Level (*SLL*), -3dB Beamwidth (*BW*), Directivity (*D*), Sideband Level (*SBL*) and Sideband Radiation (*SR*)

## TEST CASE 1.d - $N = 16$ , Double Failure (External Pulses)

### Goal

Reconfigure the radiated pattern through a *PSO*-based optimization strategy according to the feature of the pattern before the failure occurred to the *RF* switches.

### Differences wrt previous test case

- Previous: Failure occurred at the element  $n = 8$
- Current: Failures occurred at the elements  $n = 2, 14$

### Description

- Number of Elements  $N = 16$
- Elements Spacing:  $d = 0.5\lambda$
- Static Array Excitations: Uniform,  $I_n = 1, n = 1, , N$
- Averaged Time-Modulated Array Excitations: *Dolph-Chebyshev*,  $SLL = -30 \text{ dB}$ ,  $BW = 7.95 \text{ deg}$
- Failures occurred at the elements  $n = 2, 14$

### Optimization Approach: PSO [1]

- Number of Variables:  $X = 16 (\tau_n, n = 1, \dots, N)$
- Number of Particles:  $S = N$
- Number of Iterations:  $M = 1000$
- Inertial Weight:  $I_w = 0.4$
- Cost Function:  $SLL$  weight:  $w_{SLL} = 100$ ,  $BW$  weight:  $w_{BW} = 1$ ,  $SR$  weight:  $w_{SR} = 1$

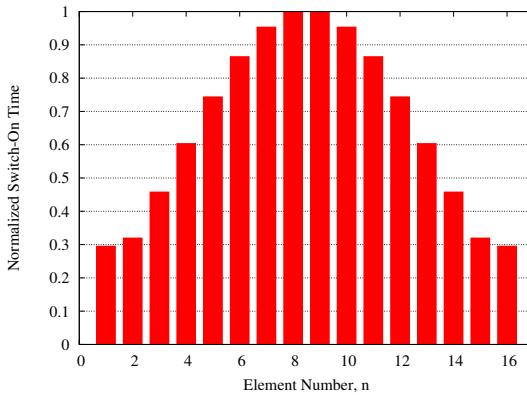


Fig. 25 - Pulse Sequence - Original

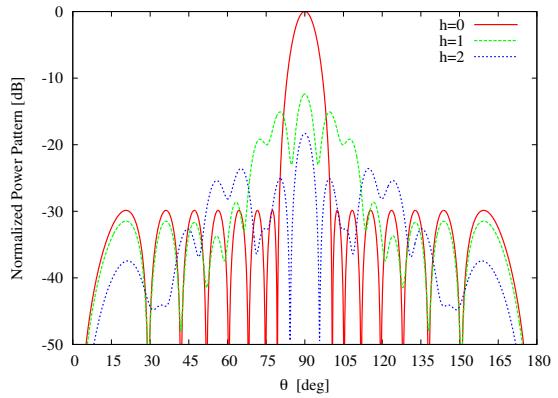


Fig. 26 - Patterns - Original

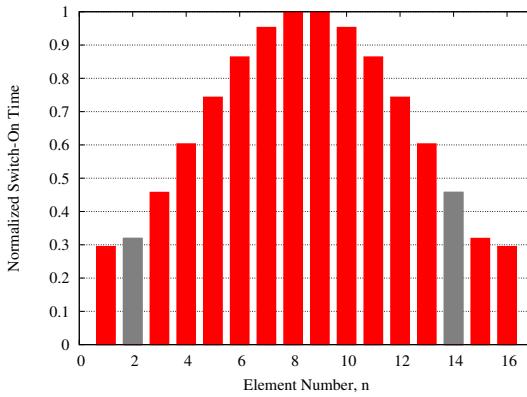


Fig. 27 - Pulse Sequence - Compromised

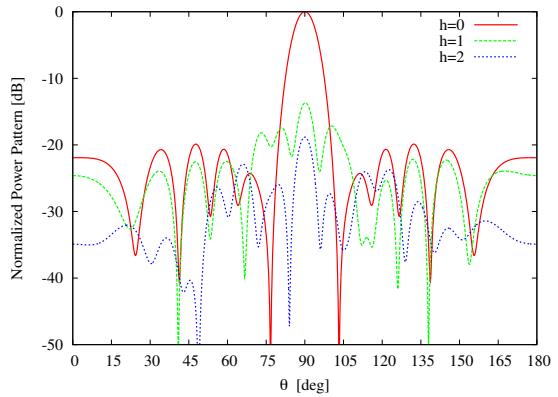


Fig. 28 - Patterns - Compromised

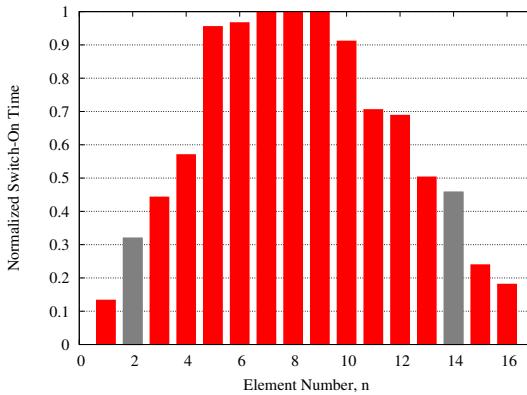


Fig. 29 - Pulse Sequence - PSO-reconfigured

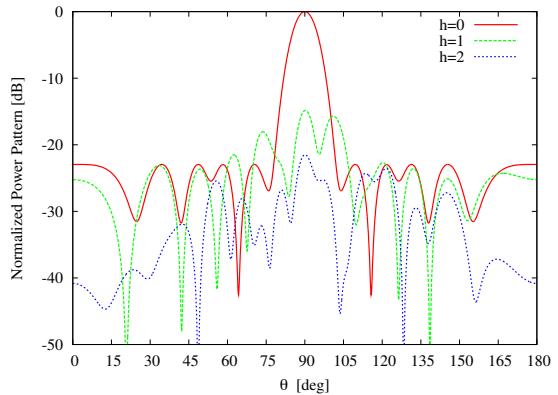


Fig. 30 - Patterns - PSO-reconfigured

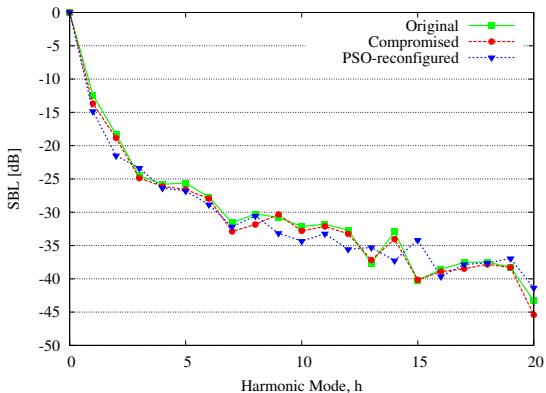


Fig. 31 - Pulse Sequence - PSO-reconfigured

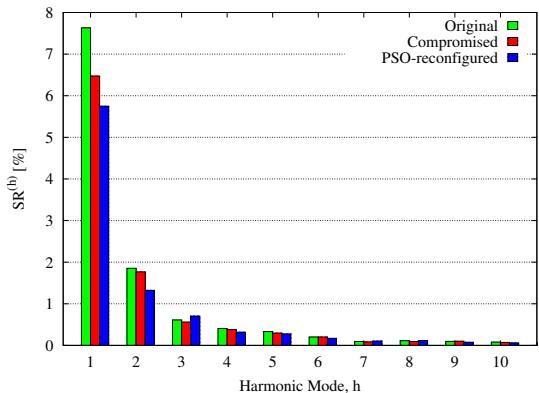
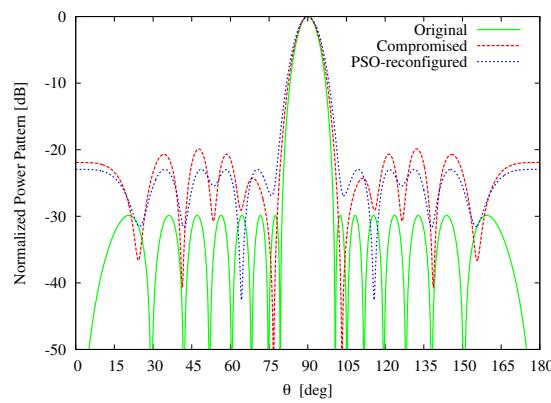


Fig. 32 - Patterns - PSO-reconfigured



**Fig. 33 - Pattern Comparison**

	<i>SLL</i> [dB]	<i>BW</i> [deg]	<i>D</i> [dB]	<i>SBL</i> [dB]	<i>SR</i> [%]
<i>Original</i>	-29.86	7.95	8.36	-12.39	24.17
<i>Compromised</i>	-19.88	8.55	8.27	-13.68	21.30
<i>PSO – reconfigured</i>	-22.95	9.25	7.91	-14.85	19.00

**Tab. IV - Patterns features: Sidelobe Level (*SLL*), -3dB Beamwidth (*BW*), Directivity (*D*), Sideband Level (*SBL*) and Sideband Radiation (*SR*)**

## TEST CASE 1.e - $N = 16$ , Double Failure (External Pulses)

### Goal

Reconfigure the radiated pattern through a *PSO*-based optimization strategy according to the feature of the pattern before the failure occurred to the *RF* switches.

### Differences wrt previous test case

- Previous: *BW* weight:  $w_{BW} = 1$
- Current: *BW* weight:  $w_{BW} = 0$  (*SLL*-only required matching)

### Description

- Number of Elements  $N = 16$
- Elements Spacing:  $d = 0.5\lambda$
- Static Array Excitations: Uniform,  $I_n = 1, n = 1, , N$
- Averaged Time-Modulated Array Excitations: *Dolph-Chebyshev*,  $SLL = -30 \text{ dB}$ ,  $BW = 7.95 \text{ deg}$
- Failures occurred at the element  $n = 2, 14$

### Optimization Approach: PSO [1]

- Number of Variables:  $X = 16$  ( $\tau_n, n = 1, \dots, N$ )
- Number of Particles:  $S = N$
- Number of Iterations:  $M = 1000$
- Inertial Weight:  $I_w = 0.4$
- Cost Function: *SLL* weight:  $w_{SLL} = 100$ , *BW* weight:  $w_{BW} = 0$ , *SR* weight:  $w_{SR} = 1$

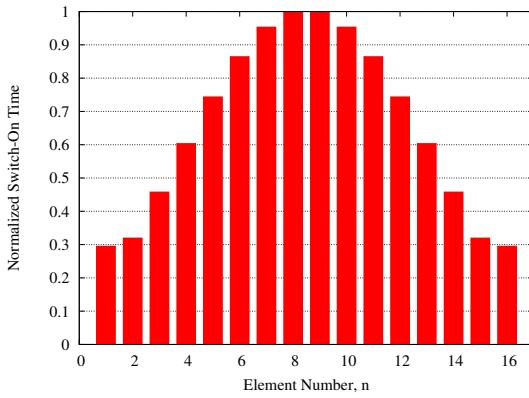


Fig. 34 - Pulse Sequence - Original

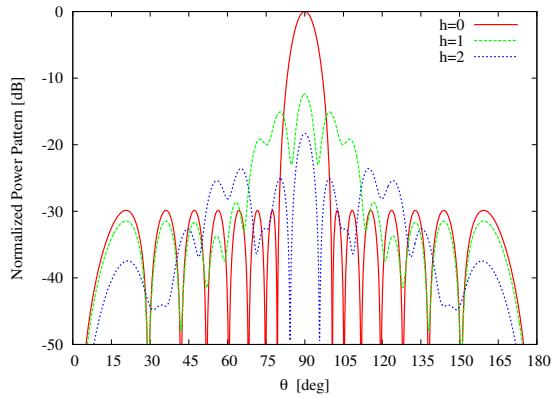


Fig. 35 - Patterns - Original

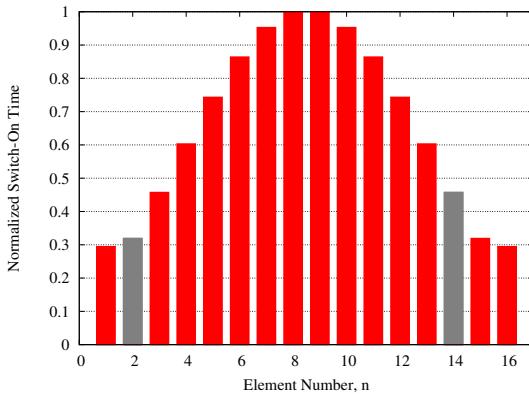


Fig. 36 - Pulse Sequence - Compromised

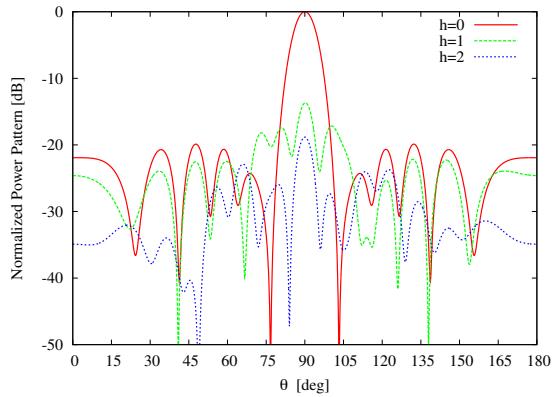


Fig. 37 - Patterns - Compromised

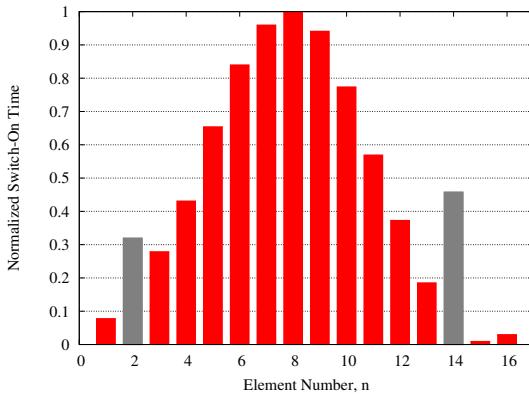


Fig. 38 - Pulse Sequence - PSO-reconfigured

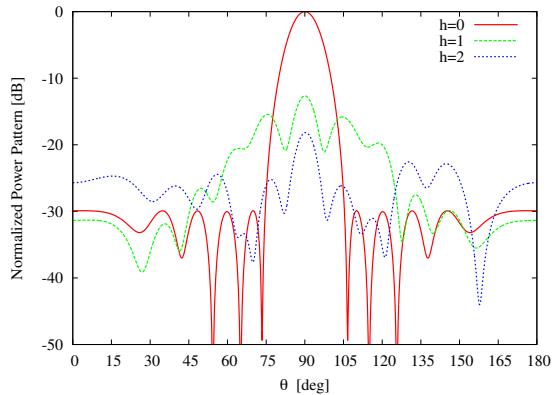


Fig. 39 - Patterns - PSO-reconfigured

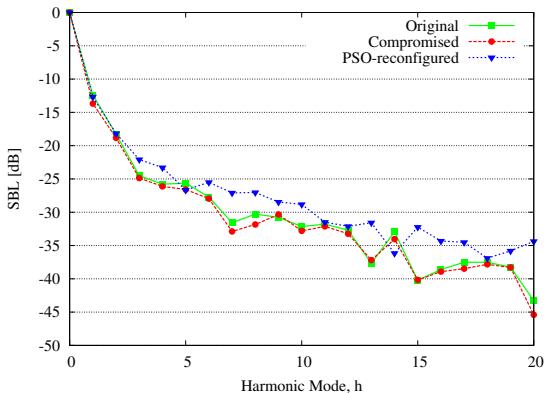


Fig. 40 - Pulse Sequence - PSO-reconfigured

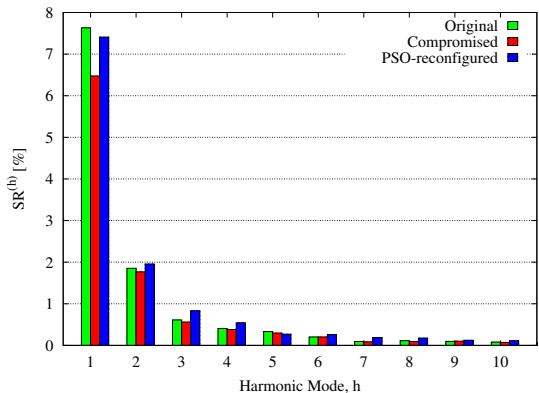
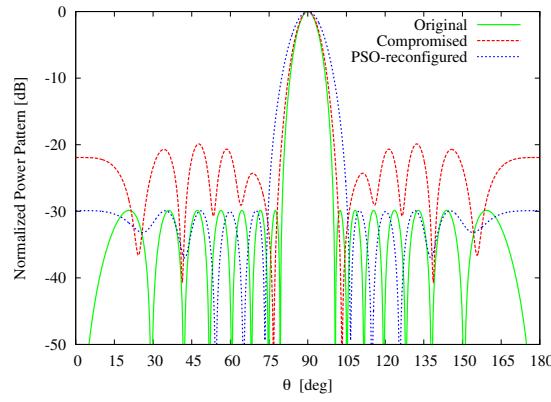


Fig. 41 - Patterns - PSO-reconfigured



**Fig. 42 - Pattern Comparison**

	<i>SLL</i> [dB]	<i>BW</i> [deg]	<i>D</i> [dB]	<i>SBL</i> [dB]	<i>SR</i> [%]
<i>Original</i>	-29.86	7.95	8.36	-12.39	24.17
<i>Compromised</i>	-19.88	8.55	8.27	-13.68	21.30
<i>PSO – reconfigured</i>	-29.90	11.39	5.59	-12.66	25.50

**Tab. V - Patterns features: Sidelobe Level (*SLL*), -3dB Beamwidth (*BW*), Directivity (*D*), Sideband Level (*SBL*) and Sideband Radiation (*SR*)**

## TEST CASE 2.a - $N = 32$ , Single Failure (External Pulse)

### Goal

Reconfigure the radiated pattern through a *PSO*-based optimization strategy according to the feature of the pattern before the failure occurred to the *RF* switches.

### Differences wrt previous test case

- Previous: Number of Elements  $N = 16$ ; Failures occurred at the elements  $n = 2, 14$
- Current: Number of Elements  $N = 32$ ; Failure occurred at the element  $n = 29$

### Description

- Number of Elements  $N = 32$
- Elements Spacing:  $d = 0.5\lambda$
- Static Array Excitations: Uniform,  $I_n = 1, n = 1, , N$
- Averaged Time-Modulated Array Excitations: *Dolph-Chebyshev*,  $SLL = -30 \text{ dB}$ ,  $BW = 3.88 \text{ deg}$
- Failure occurred at the element  $n = 29$

### Optimization Approach: PSO [1]

- Number of Variables:  $X = 32$  ( $\tau_n, n = 1, \dots, N$ )
- Number of Particles:  $S = N$
- Number of Iterations:  $M = 1000$
- Inertial Weight:  $I_w = 0.4$
- Cost Function:  $SLL$  weight:  $w_{SLL} = 100$ ,  $BW$  weight:  $w_{BW} = 1$ ,  $SR$  weight:  $w_{SR} = 1$

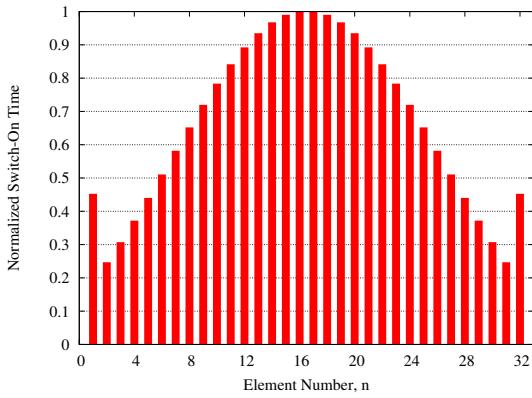


Fig. 43 - Pulse Sequence - Original

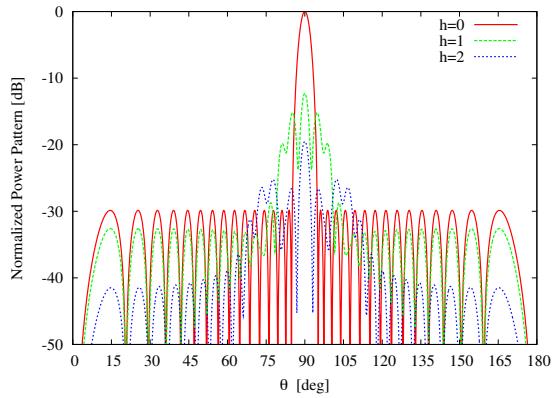


Fig. 44 - Patterns - Original

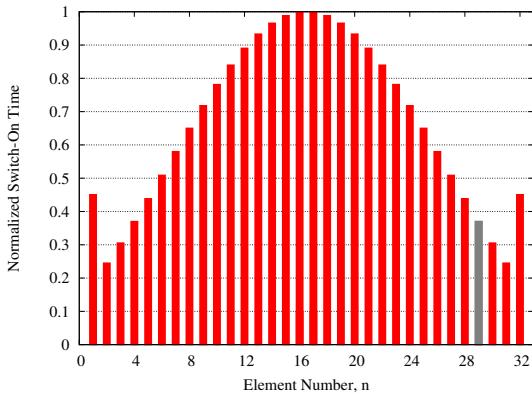


Fig. 45 - Pulse Sequence - Compromised

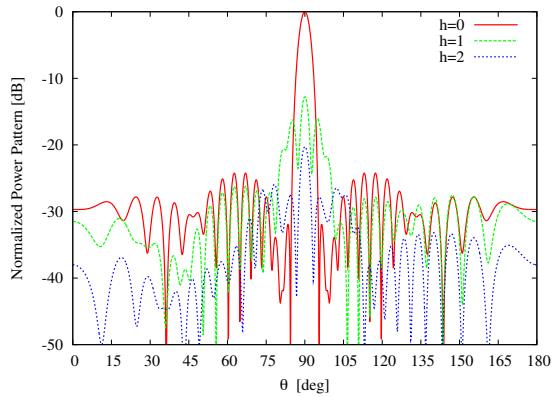


Fig. 46 - Patterns - Compromised

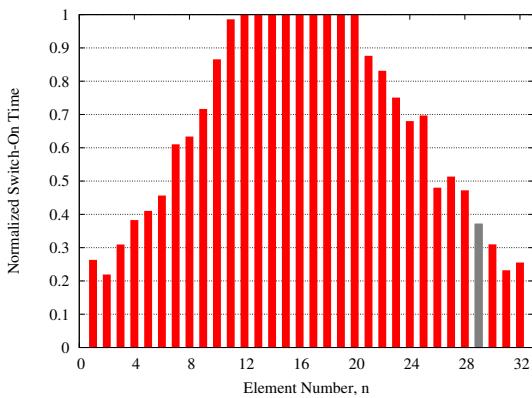


Fig. 47 - Pulse Sequence - PSO-reconfigured

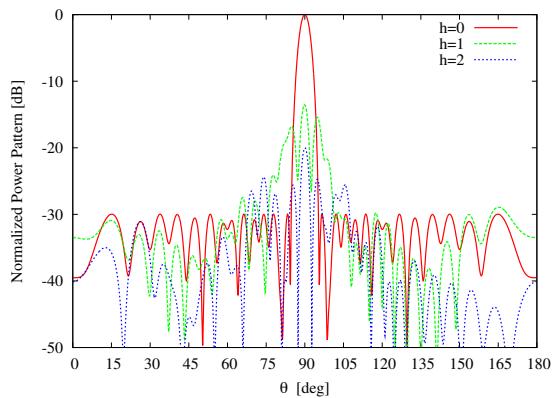


Fig. 48 - Patterns - PSO-reconfigured

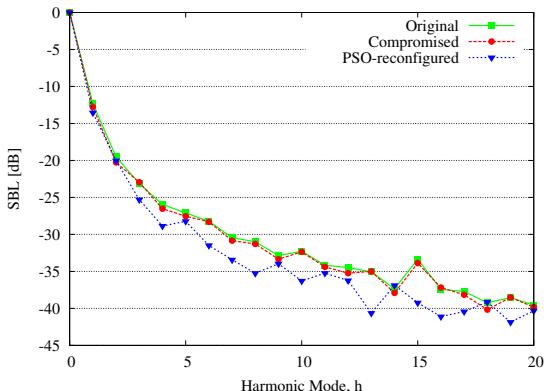


Fig. 49 - SBL - Comparison

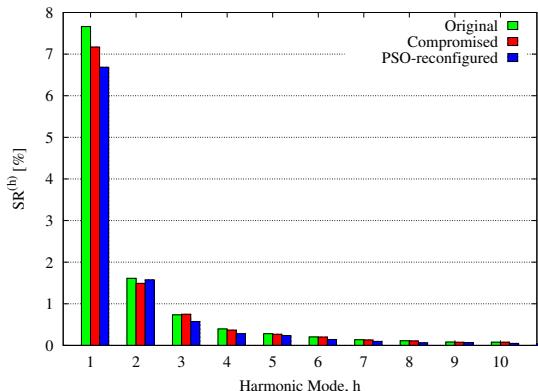
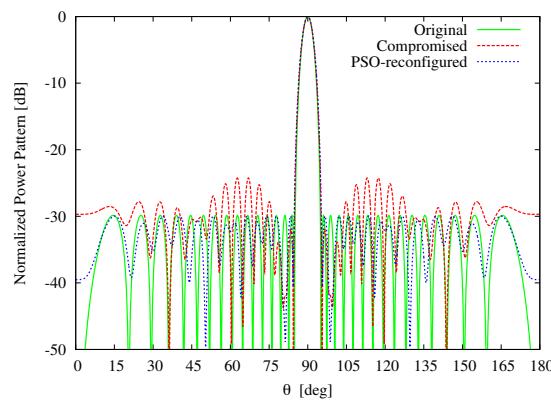


Fig. 50 - SR - Comparison



**Fig. 51 - SBL - Comparison**

	<i>SLL</i> [ <i>dB</i> ]	<i>BW</i> [ <i>deg</i> ]	<i>D</i> [ <i>dB</i> ]	<i>SBL</i> [ <i>dB</i> ]	<i>SR</i> [%]
<i>Original</i>	-29.86	3.88	11.53	-12.29	23.95
<i>Compromised</i>	-24.24	4.02	11.53	-12.77	22.58
<i>PSO – reconfigured</i>	-29.97	4.13	11.50	-13.54	20.59

**Tab. VI - Patterns features: Sidelobe Level (*SLL*), -3dB Beamwidth (*BW*), Directivity (*D*), Sideband Level (*SBL*) and Sideband Radiation (*SR*)**

## TEST CASE 2.b - $N = 32$ , Single Failure (Internal Pulse)

### Goal

Reconfigure the radiated pattern through a *PSO*-based optimization strategy according to the feature of the pattern before the failure occurred to the *RF* switches.

### Differences wrt previous test case

- Previous: Failure occurred at the element  $n = 29$
- Current: Failure occurred at the element  $n = 18$

### Description

- Number of Elements  $N = 32$
- Elements Spacing:  $d = 0.5\lambda$
- Static Array Excitations: Uniform,  $I_n = 1, n = 1, , N$
- Averaged Time-Modulated Array Excitations: *Dolph-Chebyshev*,  $SLL = -30 \text{ dB}$ ,  $BW = 3.88 \text{ deg}$
- Failure occurred at the element  $n = 18$

### Optimization Approach: PSO [1]

- Number of Variables:  $X = 32$  ( $\tau_n, n = 1, \dots, N$ )
- Number of Particles:  $S = N$
- Number of Iterations:  $M = 1000$
- Inertial Weight:  $I_w = 0.4$
- Cost Function:  $SLL$  weight:  $w_{SLL} = 100$ ,  $BW$  weight:  $w_{BW} = 1$ ,  $SR$  weight:  $w_{SR} = 1$

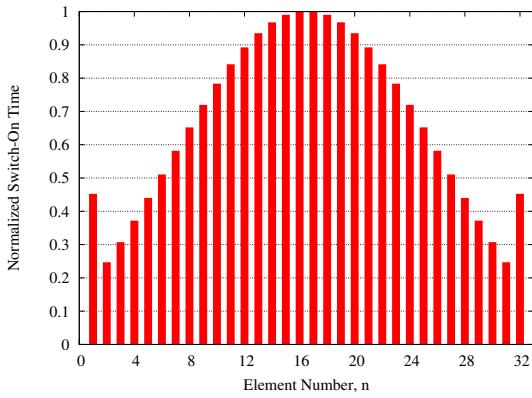


Fig. 52 - Pulse Sequence - Original

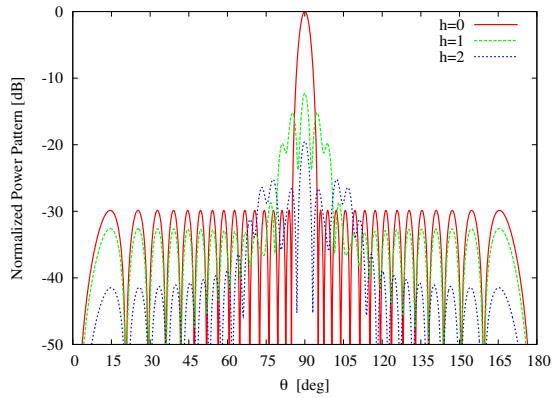


Fig. 53 - Patterns - Original

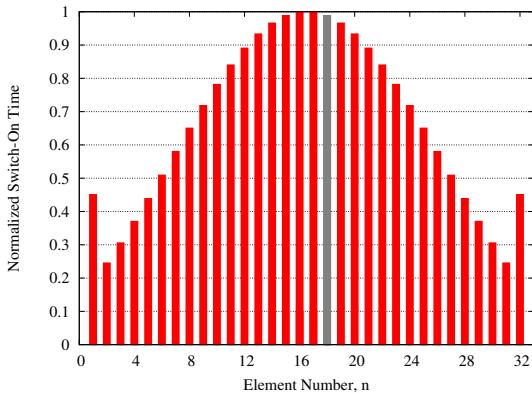


Fig. 54 - Pulse Sequence - Compromised

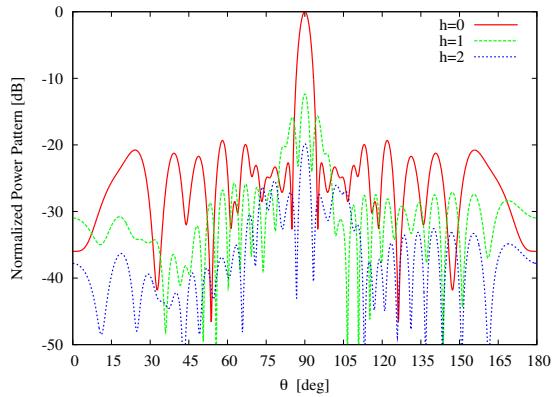


Fig. 55 - Patterns - Compromised

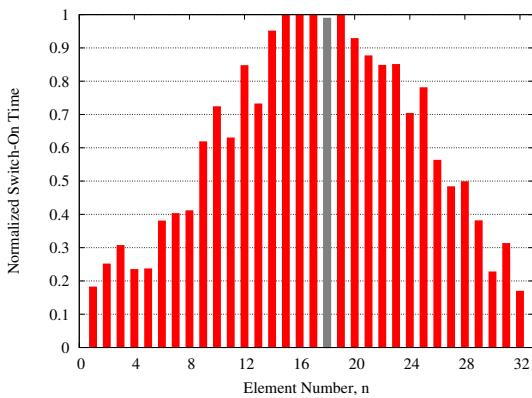


Fig. 56 - Pulse Sequence - PSO-reconfigured

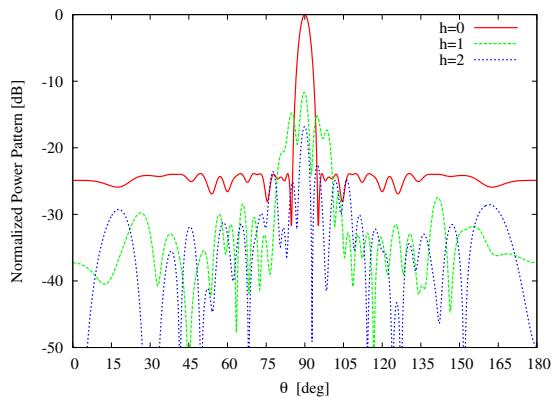


Fig. 57 - Patterns - PSO-reconfigured

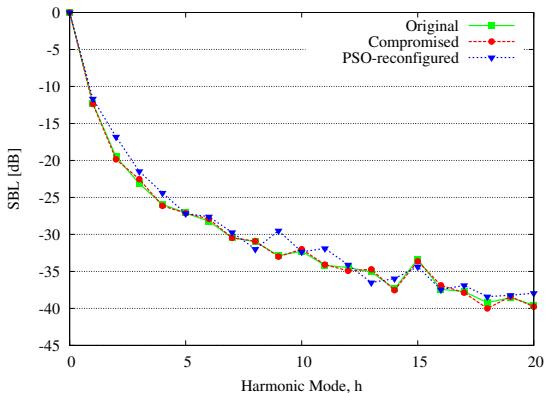


Fig. 58 - SBL - Comparison

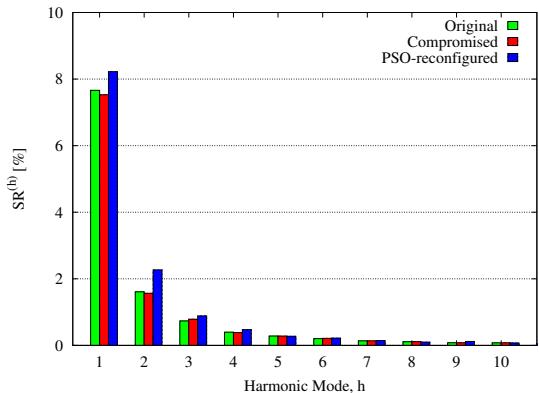
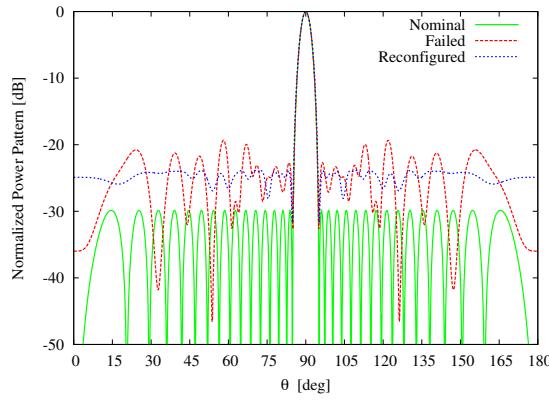


Fig. 59 - SR - Comparison



**Fig. 60 - SBL - Comparison**

	<i>SLL</i> [dB]	<i>BW</i> [deg]	<i>D</i> [dB]	<i>SBL</i> [dB]	<i>SR</i> [%]
<i>Original</i>	-29.86	3.88	11.53	-12.29	23.95
<i>Compromised</i>	-19.34	3.91	11.26	-12.35	23.66
<i>PSO – reconfigured</i>	-23.87	4.02	10.44	-11.68	27.00

**Tab. VII - Patterns features: Sidelobe Level (*SLL*), -3dB Beamwidth (*BW*), Directivity (*D*), Sideband Level (*SBL*) and Sideband Radiation (*SR*)**

## TEST CASE 2.c - $N = 32$ , Double Failure (External Pulses)

### Goal

Reconfigure the radiated pattern through a *PSO*-based optimization strategy according to the feature of the pattern before the failure occurred to the *RF* switches.

### Differences wrt previous test case

- Previous: Failure occurred at the element  $n = 18$
- Current: Failures occurred at the elements  $n = 2, 29$

### Description

- Number of Elements  $N = 32$
- Elements Spacing:  $d = 0.5\lambda$
- Static Array Excitations: Uniform,  $I_n = 1, n = 1, , N$
- Averaged Time-Modulated Array Excitations: *Dolph-Chebyshev*,  $SLL = -30 \text{ dB}$ ,  $BW = 3.88 \text{ deg}$
- Failures occurred at the elements  $n = 2, 29$

### Optimization Approach: PSO [1]

- Number of Variables:  $X = 32$  ( $\tau_n, n = 1, \dots, N$ )
- Number of Particles:  $S = N$
- Number of Iterations:  $M = 1000$
- Inertial Weight:  $I_w = 0.4$
- Cost Function:  $SLL$  weight:  $w_{SLL} = 100$ ,  $BW$  weight:  $w_{BW} = 1$ ,  $SR$  weight:  $w_{SR} = 1$

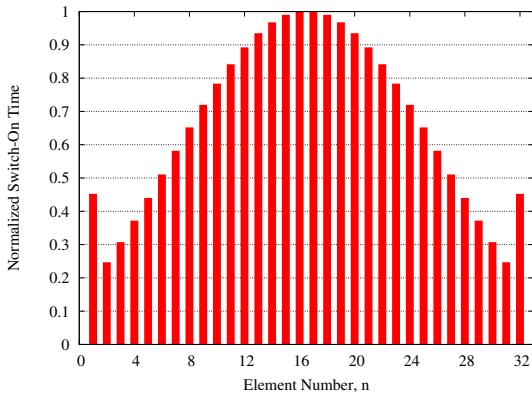


Fig. 61 - Pulse Sequence - Original

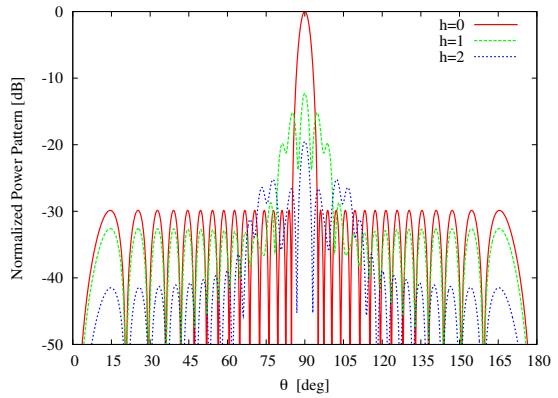


Fig. 62 - Patterns - Original

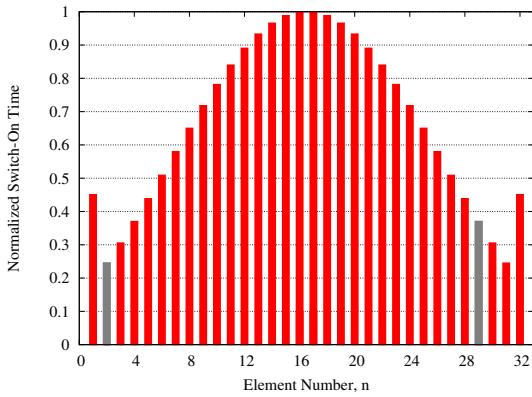


Fig. 63 - Pulse Sequence - Compromised

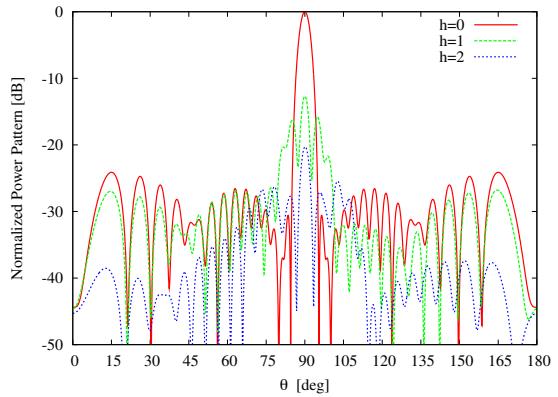


Fig. 64 - Patterns - Compromised

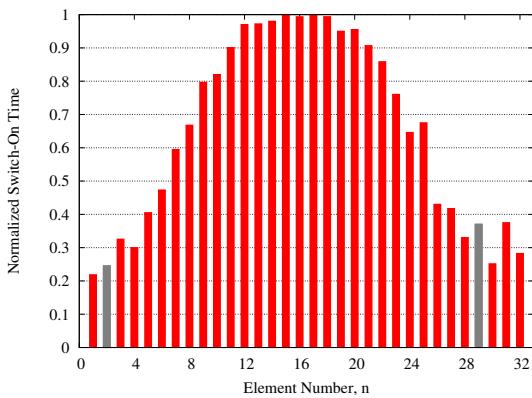


Fig. 65 - Pulse Sequence - PSO-reconfigured

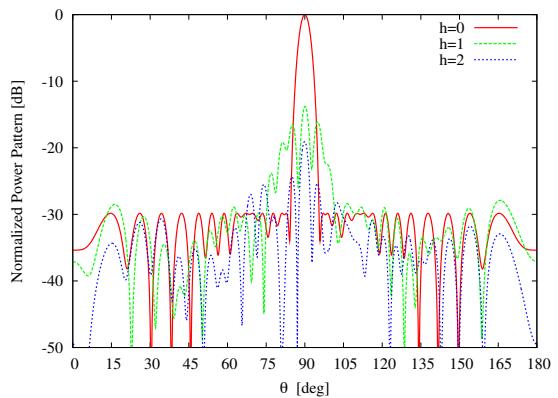


Fig. 66 - Patterns - PSO-reconfigured

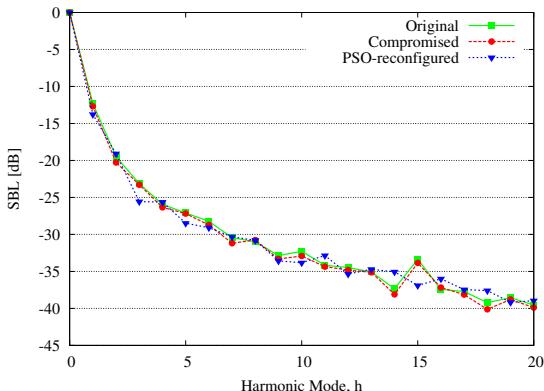


Fig. 67 - SBL - Comparison

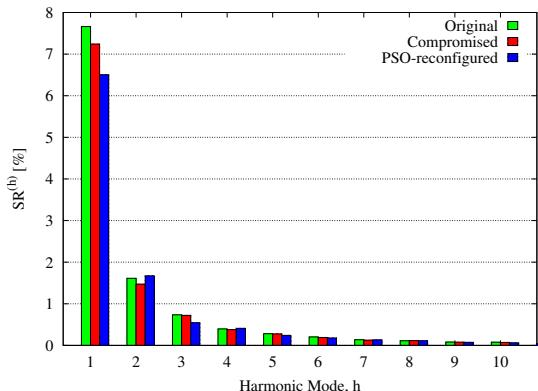
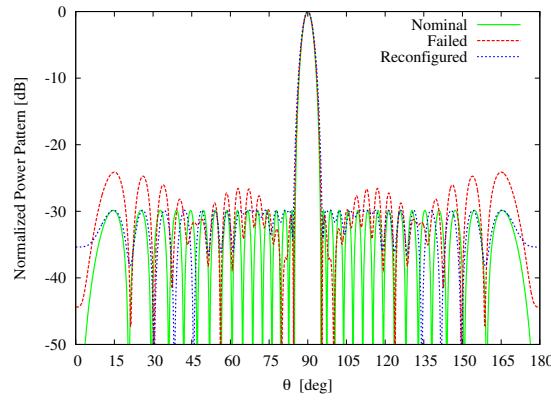


Fig. 68 - SR - Comparison



**Fig. 69 - SBL - Comparison**

	<i>SLL</i> [dB]	<i>BW</i> [deg]	<i>D</i> [dB]	<i>SBL</i> [dB]	<i>SR</i> [%]
<i>Original</i>	-29.86	3.88	11.53	-12.29	23.95
<i>Compromised</i>	-24.12	4.01	11.56	-12.69	22.64
<i>PSO – reconfigured</i>	-29.84	4.21	11.36	-13.78	21.23

**Tab. VIII - Patterns features: Sidelobe Level (*SLL*), -3dB Beamwidth (*BW*), Directivity (*D*), Sideband Level (*SBL*) and Sideband Radiation (*SR*)**

## TEST CASE 2.d - $N = 32$ , Double Failure (Internal/External Pulses)

### Goal

Reconfigure the radiated pattern through a *PSO*-based optimization strategy according to the feature of the pattern before the failure occurred to the *RF* switches.

### Differences wrt previous test case

- Previous: Failure occurred at the elements  $n = 2, 29$
- Current: Failures occurred at the elements  $n = 2, 18$

### Description

- Number of Elements  $N = 32$
- Elements Spacing:  $d = 0.5\lambda$
- Static Array Excitations: Uniform,  $I_n = 1, n = 1, , N$
- Averaged Time-Modulated Array Excitations: *Dolph-Chebyshev*,  $SLL = -30 \text{ dB}$ ,  $BW = 3.88 \text{ deg}$
- Failures occurred at the elements  $n = 2, 18$

### Optimization Approach: PSO [1]

- Number of Variables:  $X = 32$  ( $\tau_n, n = 1, \dots, N$ )
- Number of Particles:  $S = N$
- Number of Iterations:  $M = 1000$
- Inertial Weight:  $I_w = 0.4$
- Cost Function:  $SLL$  weight:  $w_{SLL} = 100$ ,  $BW$  weight:  $w_{BW} = 1$ ,  $SR$  weight:  $w_{SR} = 1$

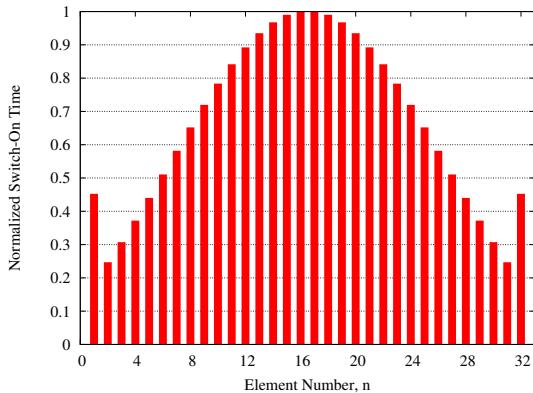


Fig. 70 - Pulse Sequence - Original

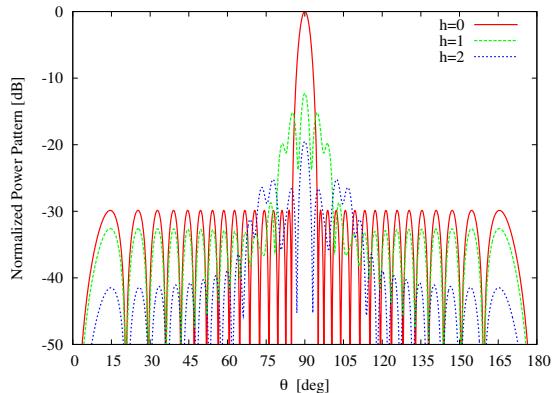


Fig. 71 - Patterns - Original

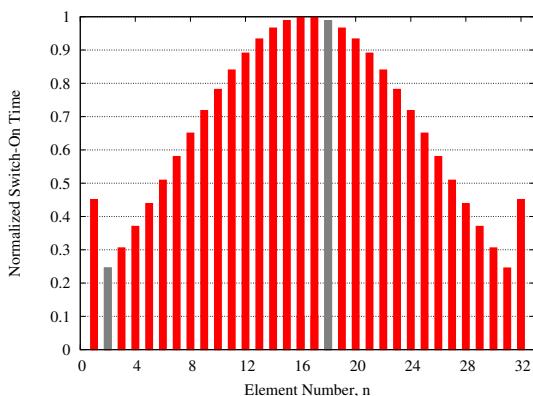


Fig. 72 - Pulse Sequence - Compromised

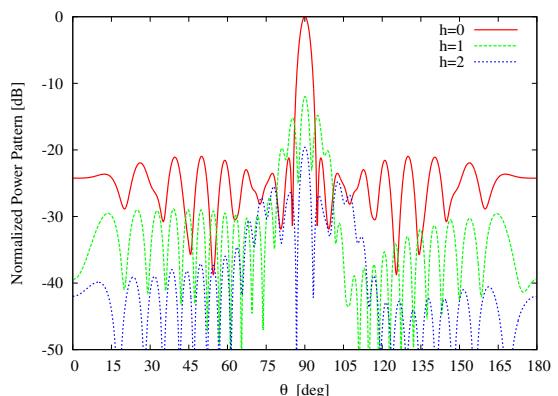


Fig. 73 - Patterns - Compromised

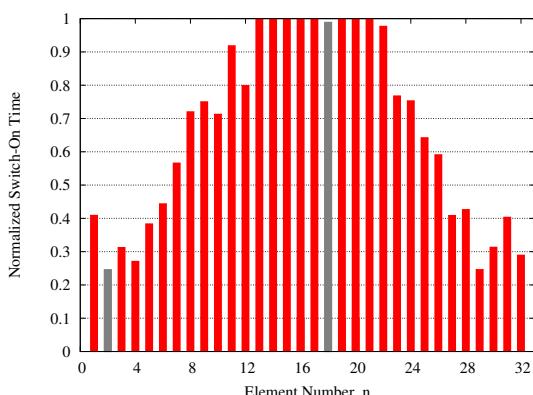


Fig. 74 - Pulse Sequence - PSO-reconfigured

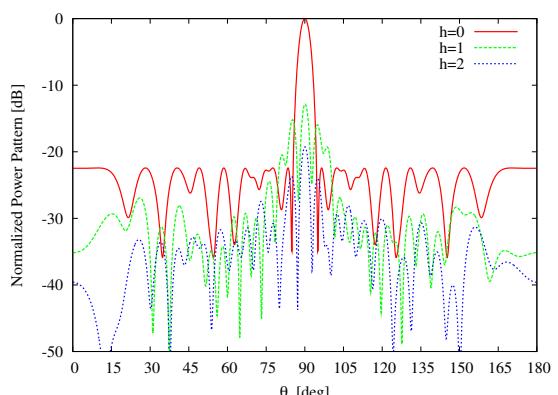


Fig. 75 - Patterns - PSO-reconfigured

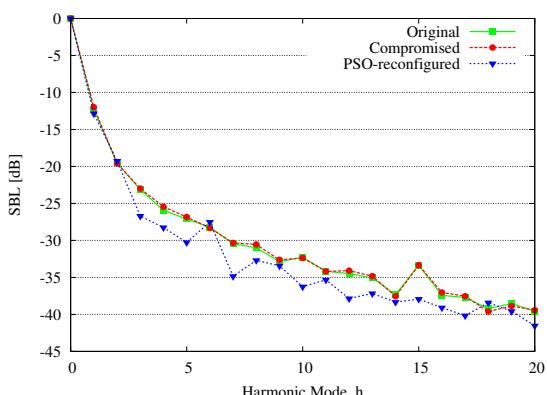


Fig. 76 - SBL - Comparison

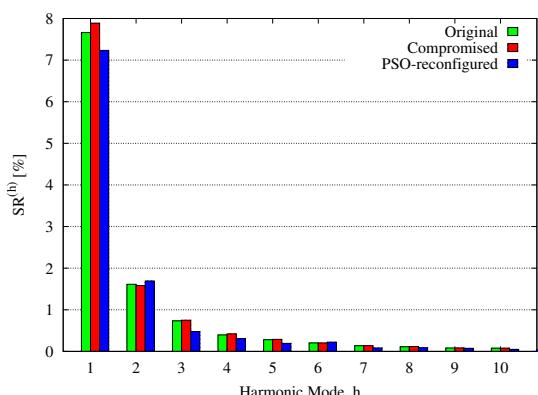
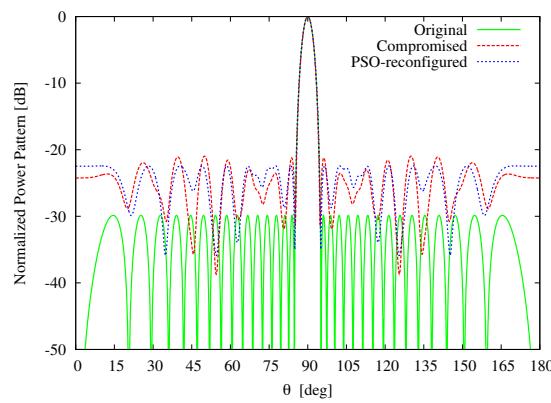


Fig. 77 - SR - Comparison



**Fig. 78 - SBL - Comparison**

	<i>SLL</i> [dB]	<i>BW</i> [deg]	<i>D</i> [dB]	<i>SBL</i> [dB]	<i>SR</i> [%]
<i>Original</i>	-29.86	3.88	11.53	-12.29	23.95
<i>Compromised</i>	-20.97	3.84	11.26	-11.99	24.44
<i>PSO - reconfigured</i>	-22.43	3.95	11.29	-12.85	21.90

**Tab. IX - Patterns features: Sidelobe Level (*SLL*), -3dB Beamwidth (*BW*), Directivity (*D*), Sideband Level (*SBL*) and Sideband Radiation (*SR*)**

## TEST CASE 3.a - $N = 30$ , Single Failure (External Pulse)

### Goal

Reconfigure the radiated pattern through a *PSO*-based optimization strategy according to the feature of the pattern before the failure occurred to the *RF* switches.

### Differences wrt previous test case

- Previous: Number of Elements  $N = 32$ ; Failures occurred at the element  $n = 2, 29$
- Current: Number of Elements  $N = 30$ ; Failure occurred at the elements  $n = 28$

### Description

- Number of Elements  $N = 30$
- Elements Spacing:  $d = 0.7\lambda$
- Static Array Excitations: Uniform,  $I_n = 1, n = 1, , N$
- Averaged Time-Modulated Array Excitations: Optimized to synthesize a pattern with  $SLL = -20 \text{ dB}$  with minimum  $SR$
- Failure occurred at the element  $n = 28$

### Optimization Approach: PSO [1]

- Number of Variables:  $X = 30 (\tau_n, n = 1, \dots, N)$
- Number of Particles:  $S = N$
- Number of Iterations:  $M = 1000$
- Inertial Weight:  $I_w = 0.4$
- Cost Function:  $SLL$  weight:  $w_{SLL} = 100$ ,  $BW$  weight:  $w_{BW} = 1$ ,  $SR$  weight:  $w_{SR} = 1$

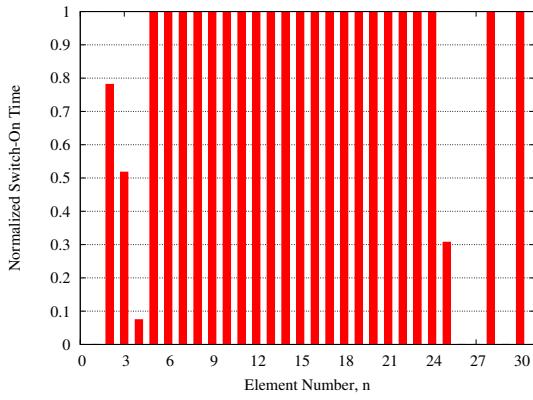


Fig. 79 - Pulse Sequence - Original

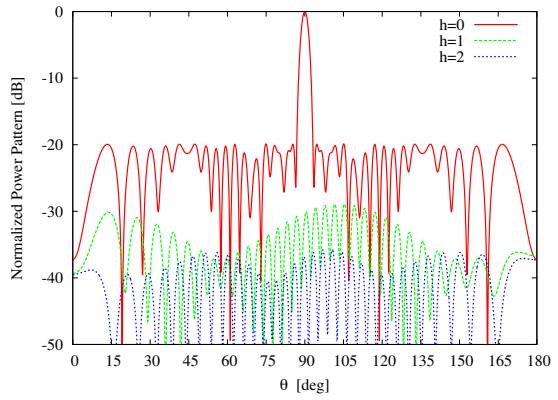


Fig. 80 - Patterns - Original

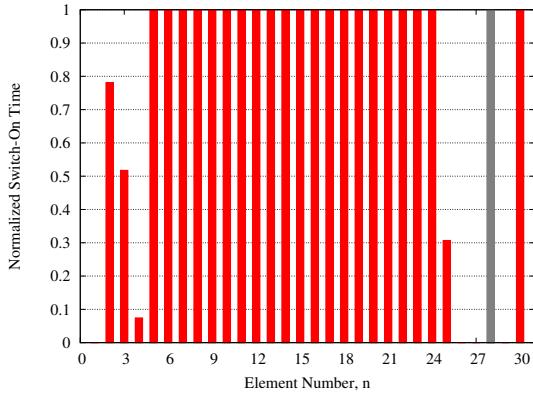


Fig. 81 - Pulse Sequence - Compromised

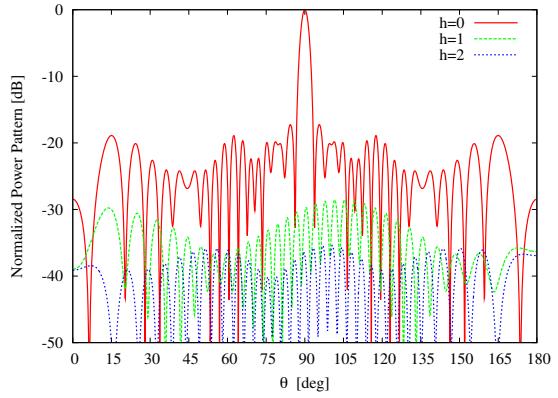


Fig. 82 - Patterns - Compromised

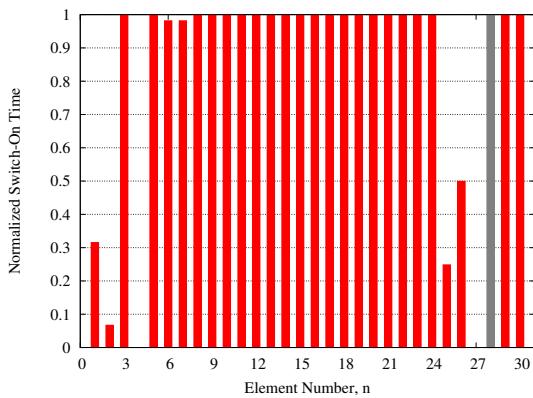


Fig. 83 - Pulse Sequence - PSO-reconfigured

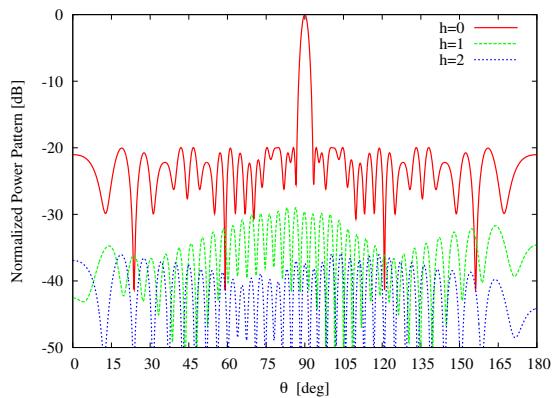


Fig. 84 - Patterns - PSO-reconfigured

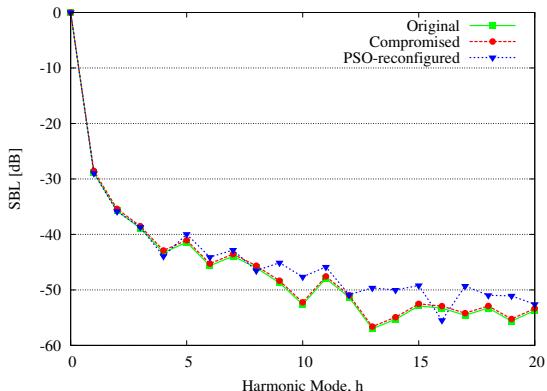


Fig. 85 - SBL - Comparison

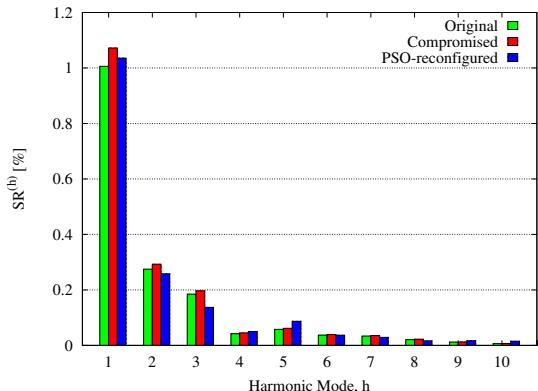
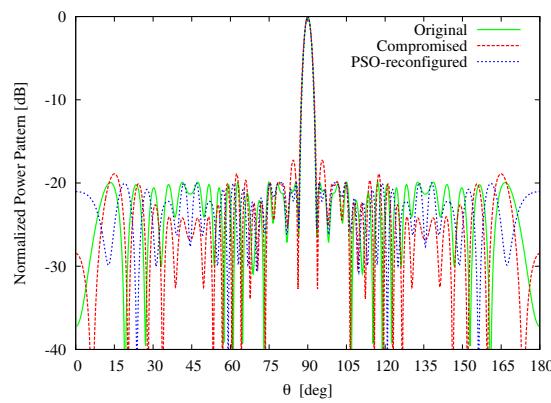


Fig. 86 - SR - Comparison



**Fig. 87 - SBL - Comparison**

	<i>SLL</i> [dB]	<i>BW</i> [deg]	<i>D</i> [dB]	<i>SBL</i> [dB]	<i>SR</i> [%]
<i>Original</i>	-19.88	2.84	13.91	-28.91	3.57
<i>Compromised</i>	-17.26	2.99	13.77	-28.54	3.81
<i>PSO – reconfigured</i>	-19.97	2.78	14.25	28.97	3.68

**Tab. X - Patterns features: Sidelobe Level (*SLL*), -3dB Beamwidth (*BW*), Directivity (*D*), Sideband Level (*SBL*) and Sideband Radiation (*SR*)**

## TEST CASE 3.b - $N = 30$ , Double Failure (External/Semi-External Pulses)

### Goal

Reconfigure the radiated pattern through a *PSO*-based optimization strategy according to the feature of the pattern before the failure occurred to the *RF* switches.

### Differences wrt previous test case

- Previous: Failure occurred at the element  $n = 28$
- Current: Failures occurred at the elements  $n = 7, 28$

### Description

- Number of Elements  $N = 30$
- Elements Spacing:  $d = 0.7\lambda$
- Static Array Excitations: Uniform,  $I_n = 1, n = 1, , N$
- Averaged Time-Modulated Array Excitations: Optimized to synthesize a pattern with  $SLL = -20 \text{ dB}$  with minimum  $SR$
- Failures occurred at the elements  $n = 7, 28$

### Optimization Approach: PSO [1]

- Number of Variables:  $X = 30$  ( $\tau_n, n = 1, \dots, N$ )
- Number of Particles:  $S = N$
- Number of Iterations:  $M = 1000$
- Inertial Weight:  $I_w = 0.4$
- Cost Function:  $SLL$  weight:  $w_{SLL} = 100$ ,  $BW$  weight:  $w_{BW} = 1$ ,  $SR$  weight:  $w_{SR} = 1$

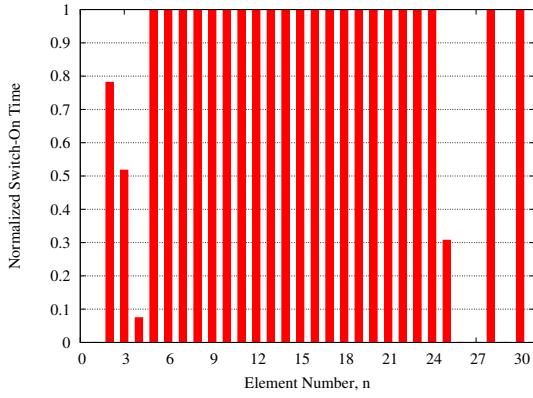


Fig. 88 - Pulse Sequence - Original

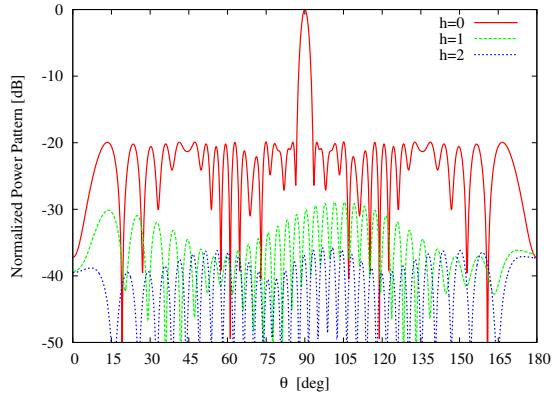


Fig. 89 - Patterns - Original

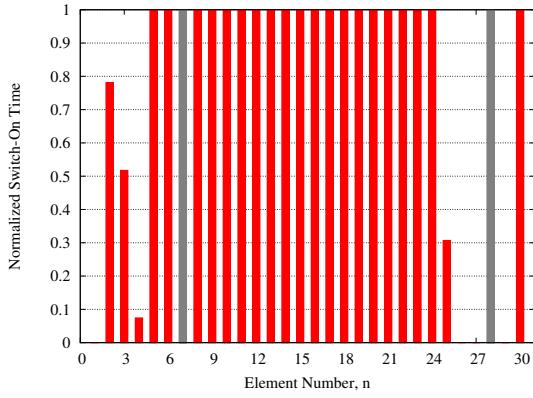


Fig. 90 - Pulse Sequence - Compromised

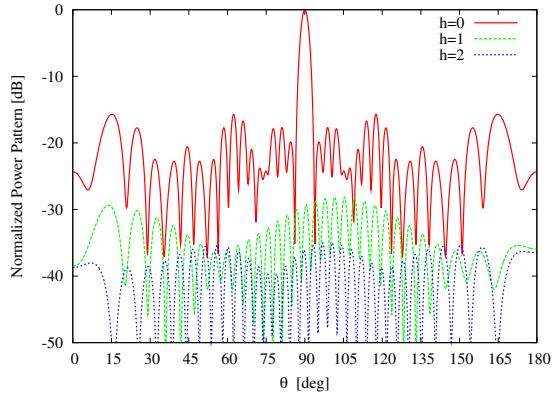


Fig. 91 - Patterns - Compromised

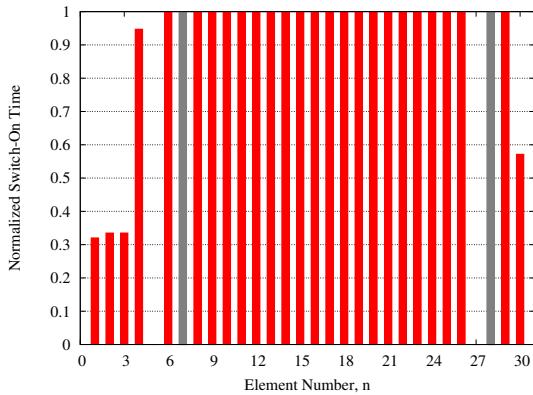


Fig. 92 - Pulse Sequence - PSO-reconfigured

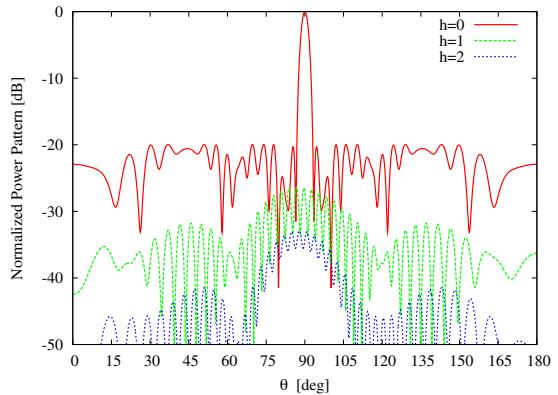


Fig. 93 - Patterns - PSO-reconfigured

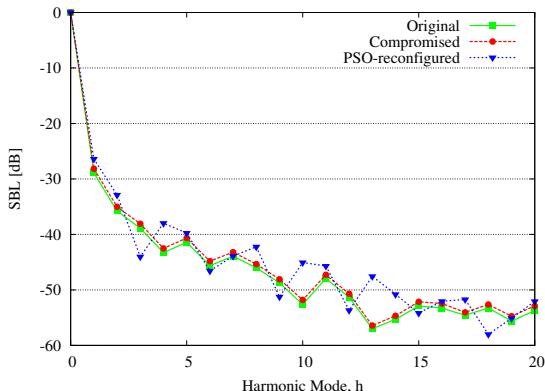


Fig. 94 - SBL - Comparison

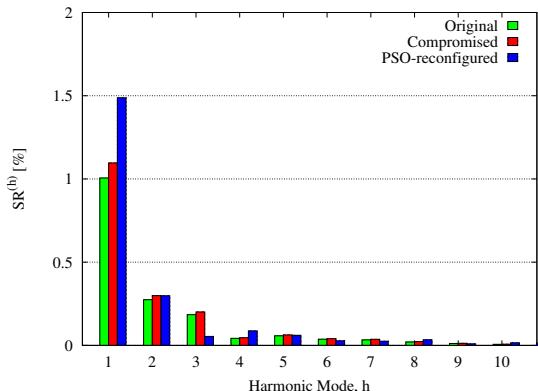
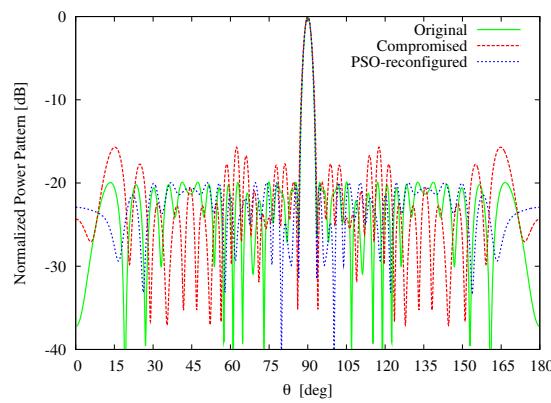


Fig. 95 - SR - Comparison



**Fig. 96 - SBL - Comparison**

	<i>SLL</i> [dB]	<i>BW</i> [deg]	<i>D</i> [dB]	<i>SBL</i> [dB]	<i>SR</i> [%]
<i>Original</i>	-19.88	2.84	13.91	-28.91	3.57
<i>Compromised</i>	-15.70	3.01	13.43	-28.16	3.89
<i>PSO – reconfigured</i>	-19.96	2.84	14.15	-26.40	4.45

**Tab. XI - Patterns features: Sidelobe Level (*SLL*), -3dB Beamwidth (*BW*), Directivity (*D*), Sideband Level (*SBL*) and Sideband Radiation (*SR*)**

## TEST CASE 3.c - $N = 30$ , Triple Failure (External/External/Semi-External Pulses)

### Goal

Reconfigure the radiated pattern through a *PSO*-based optimization strategy according to the feature of the pattern before the failure occurred to the *RF* switches.

### Differences wrt previous test case

- Previous: Failures occurred at the elements  $n = 7, 28$
- Current: Failures occurred at the elements  $n = 2, 7, 28$

### Description

- Number of Elements  $N = 30$
- Elements Spacing:  $d = 0.7\lambda$
- Static Array Excitations: Uniform,  $I_n = 1, n = 1, , N$
- Averaged Time-Modulated Array Excitations: Optimized to synthesize a pattern with  $SLL = -20 \text{ dB}$  with minimum  $SR$
- Failures occurred at the element  $n = 2, 7, 28$

### Optimization Approach: PSO [1]

- Number of Variables:  $X = 30 (\tau_n, n = 1, \dots, N)$
- Number of Particles:  $S = N$
- Number of Iterations:  $M = 1000$
- Inertial Weight:  $I_w = 0.4$
- Cost Function:  $SLL$  weight:  $w_{SLL} = 100$ ,  $BW$  weight:  $w_{BW} = 1$ ,  $SR$  weight:  $w_{SR} = 1$

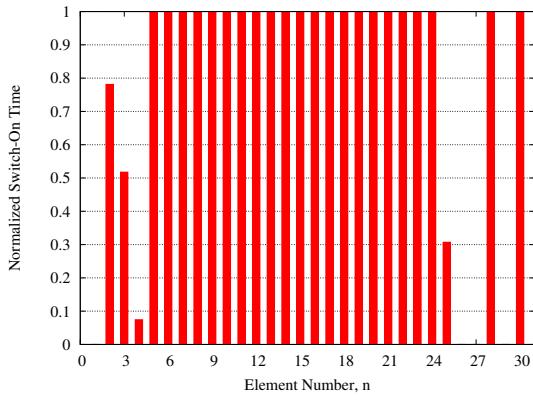


Fig. 97 - Pulse Sequence - Original

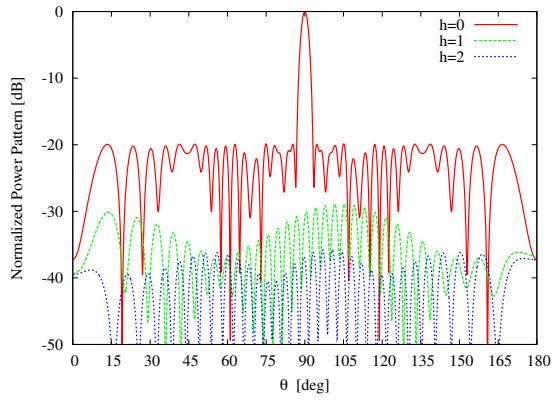


Fig. 98 - Patterns - Original

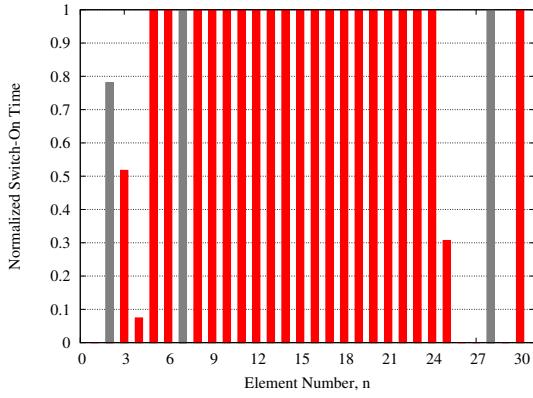


Fig. 99 - Pulse Sequence - Compromised

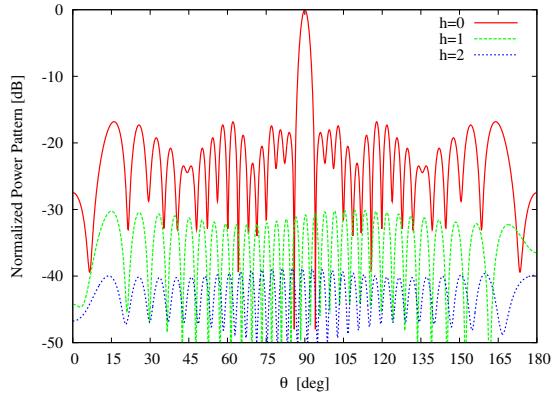


Fig. 100 - Patterns - Compromised

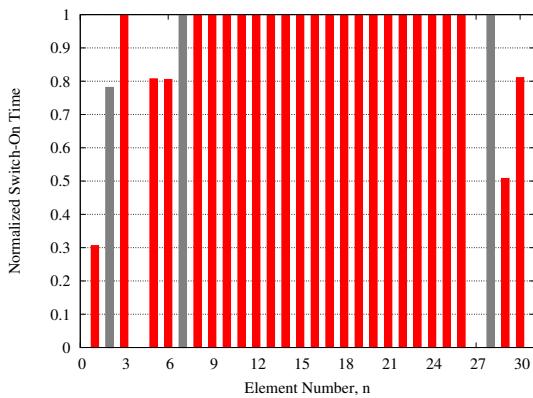


Fig. 101 - Pulse Sequence - PSO-reconfigured

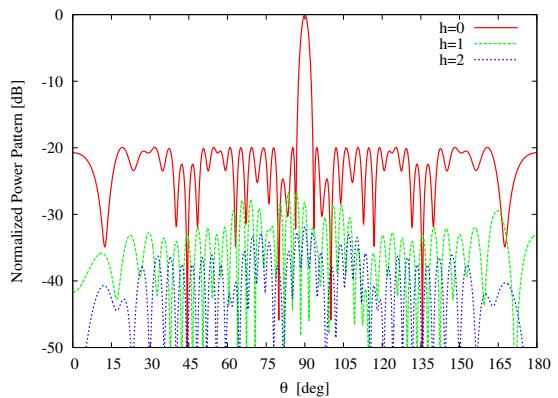


Fig. 102 - Patterns - PSO-reconfigured

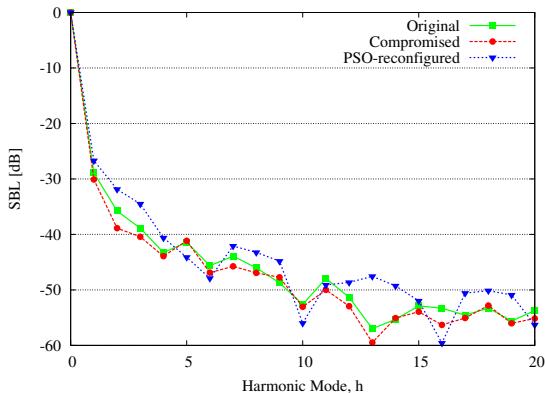


Fig. 103 - SBL - Comparison

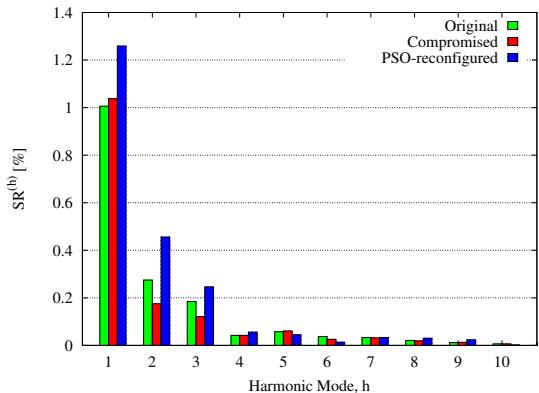
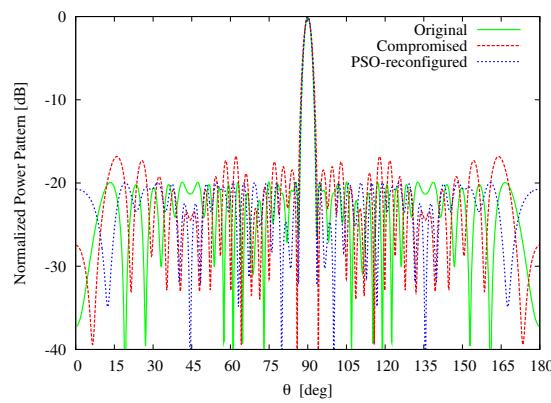


Fig. 104 - SR - Comparison



**Fig. 105 - SBL - Comparison**

	<i>SLL</i> [dB]	<i>BW</i> [deg]	<i>D</i> [dB]	<i>SBL</i> [dB]	<i>SR</i> [%]
<i>Original</i>	-19.88	2.84	13.91	-28.91	3.57
<i>Compromised</i>	-16.82	3.16	13.27	-30.11	3.24
<i>PSO – reconfigured</i>	-19.95	2.88	14.20	-26.70	4.58

**Tab. XII - Patterns features: Sidelobe Level (*SLL*), -3dB Beamwidth (*BW*), Directivity (*D*), Sideband Level (*SBL*) and Sideband Radiation (*SR*)**

## TEST CASE 3.d - $N = 30$ , Triple Failure (External/Semi-External/Internal Pulses)

### Goal

Reconfigure the radiated pattern through a *PSO*-based optimization strategy according to the feature of the pattern before the failure occurred to the *RF* switches.

### Differences wrt previous test case

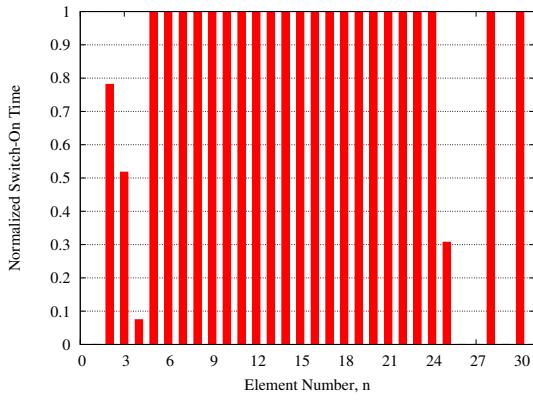
- Previous: Failures occurred at the elements  $n = 2, 7, 28$
- Current: Failures occurred at the elements  $n = 7, 20, 28$

### Description

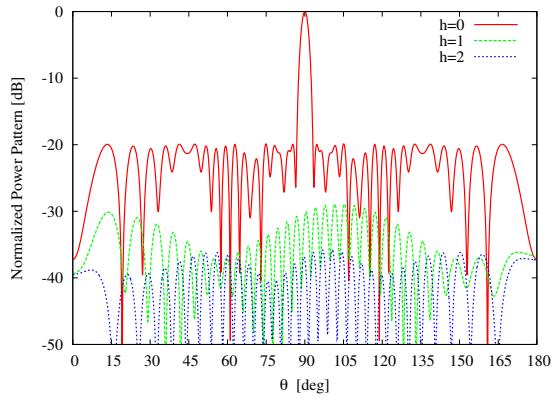
- Number of Elements  $N = 30$
- Elements Spacing:  $d = 0.7\lambda$
- Static Array Excitations: Uniform,  $I_n = 1, n = 1, , N$
- Averaged Time-Modulated Array Excitations: Optimized to synthesize a pattern with  $SLL = -20 dB$
- Failures occurred at the element  $n = 7, 20, 28$

### Optimization Approach: PSO [1]

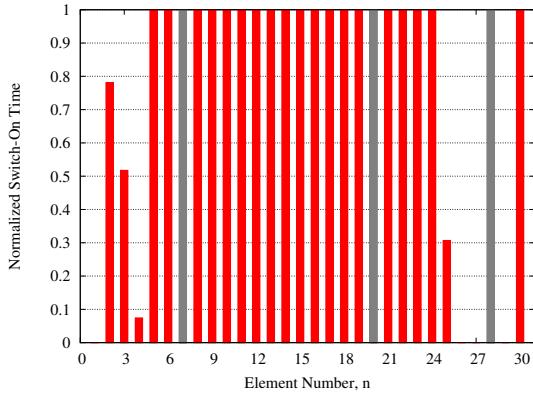
- Number of Variables:  $X = 30 (\tau_n, n = 1, \dots, N)$
- Number of Particles:  $S = N$
- Number of Iterations:  $M = 1000$
- Inertial Weight:  $I_w = 0.4$
- Cost Function:  $SLL$  weight:  $w_{SLL} = 100$ ,  $BW$  weight:  $w_{BW} = 1$ ,  $SR$  weight:  $w_{SR} = 1$



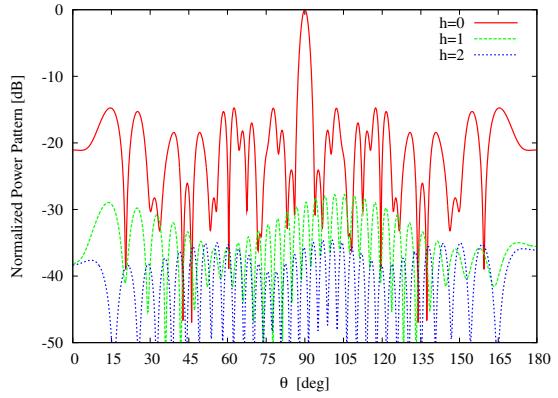
**Fig. 106 - Pulse Sequence - Original**



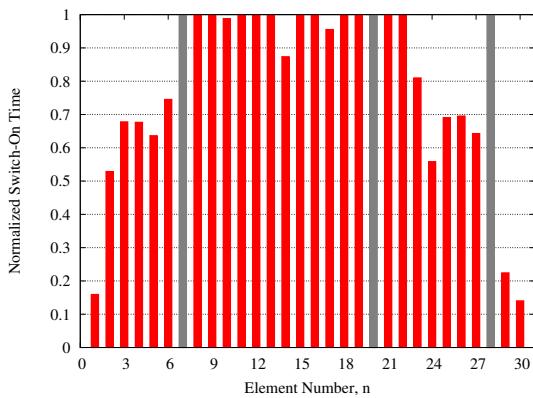
**Fig. 107 - Patterns - Original**



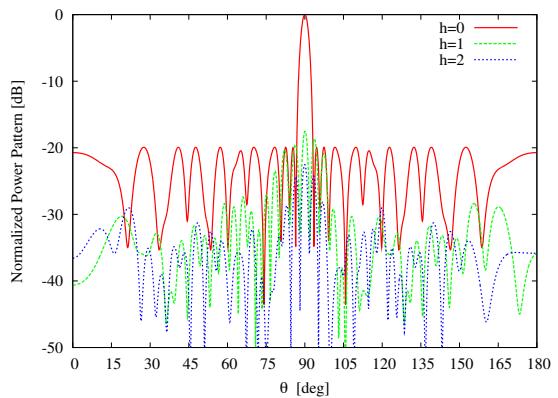
**Fig. 108 - Pulse Sequence - Compromised**



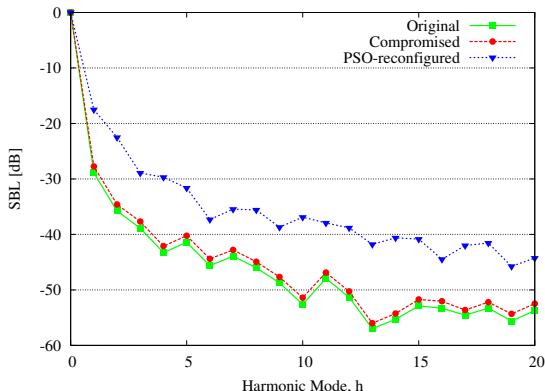
**Fig. 109 - Patterns - Compromised**



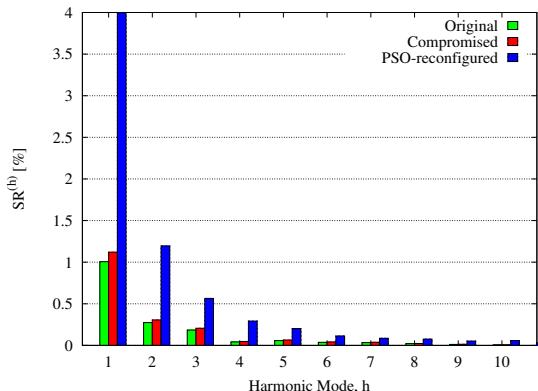
**Fig. 110 - Pulse Sequence - PSO-reconfigured**



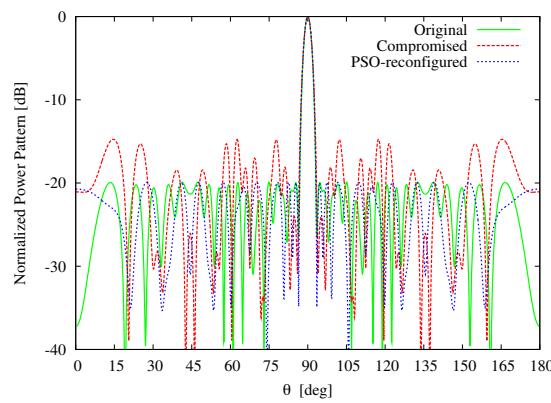
**Fig. 111 - Patterns - PSO-reconfigured**



**Fig. 112 - SBL - Comparison**



**Fig. 113 - SR - Comparison**



**Fig. 114 - SBL - Comparison**

	<i>SLL</i> [dB]	<i>BW</i> [deg]	<i>D</i> [dB]	<i>SBL</i> [dB]	<i>SR</i> [%]
<i>Original</i>	-19.88	2.84	13.91	-28.91	3.57
<i>Compromised</i>	-14.74	2.98	13.07	-27.75	3.97
<i>PSO – reconfigured</i>	-19.92	2.91	13.35	-17.51	14.23

**Tab. XIII - Patterns features: Sidelobe Level (*SLL*), -3dB Beamwidth (*BW*), Directivity (*D*), Sideband Level (*SBL*) and Sideband Radiation (*SR*)**

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