# On the Multiscale Design of Task-Oriented Reflectarrays

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# 1 Phoenix Patch Reflectarray: 30x30 SLL=-25dB



### **1.1 Optimization target**

Figure 1: Phoenix Patch Reflectarray  $30 \times 30$  SLL=-25 dB - Optimization target: SLL on the wanted polarization(a), mask on the unwanted polarization (b).

#### **1.2 Optimization results**

#### 1.2.1 Cost Function



Figure 2: Phoenix Patch Reflectarray  $30 \times 30$  SLL=-25 dB - Optimization: Cost function behavior.

# 1.2.2 Geometrical Design



Figure 3: Phoenix Patch Reflectarray  $30 \times 30$  SLL=-25 dB - Optimization: Starting reflectarray configuration(a) and optimized reflectarray configuration (b).



Figure 4: Phoenix Patch Reflectarray 30 × 30 SLL=-25 dB - Optimization - Reflection Coefficients: predicted(a)(b)(e)(f)(i)(j)(m)(n) vs. full-wave simulation (c)(d)(g)(h)(k)(l)(o)(p) of the magnitude(a)(c)(e)(g)(i)(k)(m)(o) and phase (b)(d)(f)(h)(j)(l)(n)(p) of  $S_{\theta\theta}(a)(b)(c)(d), S_{\theta\phi}(e)(f)(g)(h), S_{\phi\theta}(i)(j)(k)(l) and S_{\phi\phi}(m)(n)(o)(p).$ 

#### 1.2.4 Superficial Currents



Figure 5: Phoenix Patch Reflectarray  $30 \times 30$  SLL=-25 dB - Optimization - Superficial Currents: predicted(a)(b)(e)(f) vs. full-wave simulation (c)(d)(g)(h) of the magnitude(a)(c)(e)(g) and phase (b)(d)(f)(h) of  $J_x(a)(b)(c)(d)$  and  $J_y(e)(f)(g)(h)$ .

#### 1.2.5 Fields



Figure 6: Phoenix Patch Reflectarray  $30 \times 30$  SLL=-25 dB - Optimization - Radiated Fields: predicted(a)(b)(e)(f) vs. full-wave simulation of R (c)(g) vs. full-wave simulation of the entire structure (d)(h) of the magnitude of  $E_{\chi}(a)(b)(c)(d)$  and  $E_{\psi}(e)(f)(g)(h)$ .

### 1.2.6 Fields Cut



Figure 7: Phoenix Patch Reflectarray  $30 \times 30$  SLL=-25 dB - Optimization - Radiated Field Cut with the comparison.

# 2 Phoenix Patch Reflectarray: 35x35 SLL=-25dB



## 2.1 Optimization target

Figure 8: Phoenix Patch Reflectarray  $35 \times 35$  SLL=-25 dB - Optimization target: SLL on the wanted polarization(a), mask on the unwanted polarization (b).

## 2.2 Optimization results

#### 2.2.1 Cost Function



Figure 9: Phoenix Patch Reflectarray  $35 \times 35$  SLL=-25 dB - Optimization: Cost function behavior.

# 2.2.2 Geometrical Design



Figure 10: Phoenix Patch Reflectarray  $35 \times 35$  SLL=-25 dB - Optimization: Starting reflectarray configuration(a) and optimized reflectarray configuration (b).



Figure 11: Phoenix Patch Reflectarray 35 × 35 SLL=-25 dB - Optimization - Reflection Coefficients: predicted(a)(b)(e)(f)(i)(j)(m)(n) vs. full-wave simulation (c)(d)(g)(h)(k)(l)(o)(p) of the magnitude(a)(c)(e)(g)(i)(k)(m)(o) and phase (b)(d)(f)(h)(j)(l)(n)(p) of  $S_{\theta\theta}(a)(b)(c)(d)$ ,  $S_{\theta\phi}(e)(f)(g)(h)$ ,  $S_{\phi\theta}(i)(j)(k)(l)$  and  $S_{\phi\phi}(m)(n)(o)(p)$ .

#### 2.2.4 Superficial Currents



Figure 12: Phoenix Patch Reflectarray  $35 \times 35$  SLL=-25 dB - Optimization - Superficial Currents: predicted(a)(b)(e)(f) vs. full-wave simulation (c)(d)(g)(h) of the magnitude(a)(c)(e)(g) and phase (b)(d)(f)(h) of  $J_x(a)(b)(c)(d)$  and  $J_y(e)(f)(g)(h)$ .

#### 2.2.5 Fields



Figure 13: Phoenix Patch Reflectarray  $35 \times 35$  SLL=-25 dB - Optimization - Radiated Fields: predicted(a)(b)(e)(f) vs. full-wave simulation of R (c)(g) vs. full-wave simulation of the entire structure (d)(h) of the magnitude of  $E_{\chi}(a)(b)(c)(d)$  and  $E_{\psi}(e)(f)(g)(h)$ .

### 2.2.6 Fields Cut



Figure 14: Phoenix Patch Reflectarray  $35 \times 35$  SLL=-25 dB - Optimization - Radiated Field Cut with the comparison.

# **3** Double Layer Square Patch Reflectarray: 29x29

# 3.1 Unit cell geometry



Figure 15: Square Patch Dual Layer unit cell, front (a) and side (b) view.

# 3.2 Optimization target



Figure 16: Double Layer Square Patch Reflectarray  $29 \times 29 \alpha_{\beta} = \alpha_{\Gamma} = 1.0$  - Optimization target: SLL on the wanted polarization(a), mask on the unwanted polarization (b).

# 3.3 Optimization results

#### 3.3.1 Cost Function



Figure 17: Double Layer Square Patch Reflectarray  $29 \times 29 \alpha_{\beta} = \alpha_{\Gamma} = 1.0$ - Optimization: Cost function behavior.

#### 3.3.2 Geometrical Design



Figure 18: Double Layer Square Patch Reflectarray  $29 \times 29 \alpha_{\beta} = \alpha_{\Gamma} = 1.0$ - Optimization: Starting reflectarray configuration(a)(c), optimized reflectarray configuration (b)(d) for layer one (a)(b) and layer two (c)(d).



Figure 19: Double Layer Square Patch Reflectarray  $29 \times 29 \alpha_{\beta} = \alpha_{\Gamma} = 1.0$  - Optimization - Reflection Coefficients: predicted(a)(b)(e)(f)(i)(j)(m)(n) vs. full-wave simulation (c)(d)(g)(h)(k)(l)(o)(p) of the magnitude(a)(c)(e)(g)(i)(k)(m)(o) and phase (b)(d)(f)(h)(j)(l)(n)(p) of  $S_{\theta\theta}(a)(b)(c)(d), S_{\theta\phi}(e)(f)(g)(h), S_{\phi\theta}(i)(j)(k)(l) and S_{\phi\phi}(m)(n)(o)(p).$ 

#### 3.3.4 Superficial Currents



Figure 20: Double Layer Square Patch Reflectarray  $29 \times 29 \alpha_{\beta} = \alpha_{\Gamma} = 1.0$  - Optimization - Superficial Currents: predicted(a)(b)(e)(f) vs. full-wave simulation (c)(d)(g)(h) of the magnitude(a)(c)(e)(g) and phase (b)(d)(f)(h) of  $J_x(a)(b)(c)(d)$ and  $J_y(e)(f)(g)(h)$ .



#### 3.3.5 Fields

Figure 21: Double Layer Square Patch Reflectarray  $29 \times 29 \alpha_{\beta} = \alpha_{\Gamma} = 1.0$  - Optimization - Radiated Fields: predicted(a)(b)(e)(f) vs. full-wave simulation of R (c)(g) vs. full-wave simulation of the entire structure (d)(h) of the magnitude of  $E_{\chi}(a)(b)(c)(d)$  and  $E_{\psi}(e)(f)(g)(h)$ .



### 3.3.6 Fields Cut





# 4 Double Layer Square Patch Reflectarray: 29x29, Similarity Weight=10

#### P×Q=29×29, "Square" Patch Dual Layer, SLL<sub>y</sub>=-30 dB, $M_{\psi}$ =-40 dB P×Q=29×29, "Square" Patch Dual Layer, SLL<sub>y</sub>=-30 dB, $M_w$ =-40 dB 0 0 1 1 normalized -10 -100.5 0.5 -20 -20 0 0 M<sub>v</sub>(u,v) [dB] "(u,v) [dB] .30 -30 -0.5 -0.5 40 40 -50 -1 -1 -50 -0.5 0 0.5 -0.5 0 0.5 \_1 1 -1 1 u u *(a) (b)*

### 4.1 Optimization target

Figure 23: Double Layer Square Patch Reflectarray  $29 \times 29 \alpha_{\beta} = 1.0$ ,  $\alpha_{\Gamma} = 10.0$  - Optimization target: SLL on the wanted polarization(a), mask on the unwanted polarization (b).

# 4.2 **Optimization results**

#### 4.2.1 Cost Function



Figure 24: Double Layer Square Patch Reflectarray  $29 \times 29 \alpha_{\beta} = 1.0, \alpha_{\Gamma} = 10.0$ - Optimization: Cost function behavior.

#### 4.2.2 Geometrical Design



Figure 25: Double Layer Square Patch Reflectarray  $29 \times 29 \alpha_{\beta} = 1.0$ ,  $\alpha_{\Gamma} = 10.0$ - Optimization: Starting reflectarray configuration(a)(c), optimized reflectarray configuration (b)(d) for layer one (a)(b) and layer two (c)(d).



Figure 26: Double Layer Square Patch Reflectarray  $29 \times 29 \alpha_{\beta} = 1.0$ ,  $\alpha_{\Gamma} = 10.0$  - Optimization - Reflection Coefficients: predicted(a)(b)(e)(f)(i)(j)(m)(n) vs. full-wave simulation (c)(d)(g)(h)(k)(l)(o)(p) of the magnitude(a)(c)(e)(g)(i)(k)(m)(o) and phase (b)(d)(f)(h)(j)(l)(n)(p) of  $S_{\theta\theta}(a)(b)(c)(d)$ ,  $S_{\theta\phi}(e)(f)(g)(h)$ ,  $S_{\phi\phi}(i)(j)(k)(l)$  and  $S_{\phi\phi}(m)(n)(o)(p)$ .

#### 4.2.4 Superficial Currents



Figure 27: Double Layer Square Patch Reflectarray  $29 \times 29 \alpha_{\beta} = 1.0$ ,  $\alpha_{\Gamma} = 10.0$  - Optimization - Superficial Currents: predicted(a)(b)(e)(f) vs. full-wave simulation (c)(d)(g)(h)of the magnitude(a)(c)(e)(g) and phase (b)(d)(f)(h) of  $J_x(a)(b)(c)(d)$  and  $J_y(e)(f)(g)(h)$ .



#### 4.2.5 Fields

Figure 28: Double Layer Square Patch Reflectarray  $29 \times 29\alpha_{\beta} = 1.0$ ,  $\alpha_{\Gamma} = 10.0$  - Optimization - Radiated Fields: predicted(a)(b)(e)(f) vs. full-wave simulation of R (c)(g) vs. full-wave simulation of the entire structure (d)(h) of the magnitude of  $E_{\chi}(a)(b)(c)(d)$  and  $E_{\psi}(e)(f)(g)(h)$ .

### 4.2.6 Fields Cut



Figure 29: Double Layer Square Patch Reflectarray  $29 \times 29 \alpha_{\beta} = 1.0$ ,  $\alpha_{\Gamma} = 10.0$  - Optimization - Radiated Field Cut with the comparison .

More information on the topics of this document can be found in the following list of references.

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